



Types, conclusion

Read: Scott, Chapters 7.1-7.2 and 8

Announcements

- Quiz 8
- Welcome back!
- Check your Rainbow grades
 - Exam 1-2, Quiz 1-7, HW 1-5
- HW 6 due Wednesday at midnight
- HW 7 out

Quiz 8 Q1 to Q3

Combinators:

$$\text{tru} = \lambda x. \lambda y. x$$

$$\text{pair} = \lambda f. \lambda s. \lambda b. b f s$$

$$\text{fst} = \lambda p. p \text{tru}$$

Q1: $\text{tru } v \ w = ((\text{tru } v) \ w) =$

$$\underline{(\lambda x. \lambda y. x) \ v \ w} \rightarrow_{\beta} (\lambda y. v) \ w \rightarrow_{\beta} \boxed{v}$$

Q2: $\text{pair } v \ w =$

$$\underline{(\lambda f. \lambda s. \lambda b. b f s) \ v \ w} \rightarrow_{\beta} (\lambda s. \lambda b. b \ v \ s) \ w \rightarrow \boxed{\lambda b. b \ v \ w}$$

Q3: $\text{fst} (\text{pair } v \ w) \rightarrow_{*} \text{fst} (\lambda b. b \ v \ w) =$

$$\underline{(\lambda p. p \ \text{tru}) \ (\lambda b. b \ v \ w)} \rightarrow_{\beta}$$

$$\underline{(\lambda b. b \ v \ w) \ \text{tru}} \rightarrow_{\beta} \text{tru } \ v \ w \rightarrow_{*} \boxed{v}$$

(Q1 reduction)

Rules:

1) A combinator is a Lambda abstraction with no free variables. Top-level term is Abstraction.

2) When replacing abbreviation (e.g. pair) with corresponding λ -expression, always parenthesize!

3) Keep abbreviation as long as possible, until it is in some head position and we need to expand to λ -expression.

Lecture Outline

- Types (last time)
- Type systems (last time)
 - Type checking
 - Type safety
- Type equivalence (last time)
- Types in C

- Primitive types
- Composite types

Type Equivalence

- Two ways of defining type equivalence
 - **Structural equivalence**: based on “shape”
 - Roughly, two types are the same if they consists of the same components, put together in the same way
 - **Name equivalence**: based on lexical occurrence of the type definition
 - Strict name equivalence: aliased types are distinct
 - Loose name equivalence: aliased types are same

T1 **x**; ...

T2 **y**;

x = **y**; ✓ ✗

Exercise: Structural Equivalence

`type cell = ... // record type`

`typealink = pointer to cell`

`type blink =alink`

`p,q : pointer to cell`

`r :alink`

`s :blink`

`t : pointer to cell`

`u :alink`

`p,q,r,s,t,u`

Exercise: Loose Name Equivalence

```
type cell = ... // record type
```

```
typealink = pointer to cell
```

```
typeblink =alink
```

```
p,q : pointer to cell
```

```
r :alink
```

```
s :blink
```

```
t : pointer to cell
```

```
u :alink
```

p, q

r, s, u

t

Exercise: Strict Name Equivalence

```
type cell = ... // record type
```

```
typealink = pointer to cell
```

```
typeblink =alink
```

```
p, q : pointer to cell
```

```
r :alink
```

```
s :blink
```

```
t : pointer to cell
```

```
u :alink
```

p, q

r, u

s

t

Example: Type Equivalence in C

- First, in the Algol family, **field names are part** of the record/struct constructed type. E.g., the record types below are NOT even structurally equivalent

```
type A = record
```

```
  x,y : real
```

```
end;
```

```
type B = record
```

```
  z,w : real
```

```
end;
```

Type Equivalence in C

- Compiler assigns internal (compiler-generated) names to anonymous types

This **struct** is of type anon1.

```
struct RecA
{ char x;
  int y;
} a;
```

```
typedef struct
{ char x;
  int y;
} RecB;
```

```
struct
{ char x;
  int y;
} c;
```

```
RecB b;
```

Each one is of distinct type.

What variables are of **equivalent type** according to the rules in C?

a **b** **c**

Type Equivalence in C

- C uses structural equivalence for everything, except unions and structs, for which it uses loose name equivalence

```
struct A          struct B
{ char x;        { char x;
  int y;         int y;
}                }
typedef struct A C;
typedef C *P;
typedef struct B *Q;
typedef struct A *R;
typedef int Age;
typedef int (*F) (int);
typedef Age (*G) (Age);
```

Struct B

Struct A, C

P, R

Q

int, Age

F, G

Type Equivalence in C

```
struct B { char x; int y; };
```

```
typedef struct B A;
```

```
struct { A a; A *next; } aa;
```

```
struct { struct B a; struct B *next; } bb;
```

```
struct { struct B a; struct B *next; } cc;
```

```
A a;
```

```
struct B b;
```

```
a = b; ✓
```

```
aa = bb; ✗
```

```
bb = cc; ✗
```

Which of the above assignments pass the type checker?

Question

- Structural equivalence for record types is considered a bad idea. Can you think of a reason why?

LOOSE NAME IS A BETTER CHOICE!

Lecture Outline

- Types
- Type systems
 - Type checking
 - Type safety
- Type equivalence
- **Types in C**

- Primitive types
- Composite types

Pointers and Arrays in C

- Pointers and arrays are **interoperable**:

```
int n;  
int *a;  
int b[10];
```

1. `a = b;` ✓
2. `n = a[3];` ✓
3. `n = *(a+3);` ✓
4. `n = b[3];` ✓
5. `n = *(b+3);` ✓

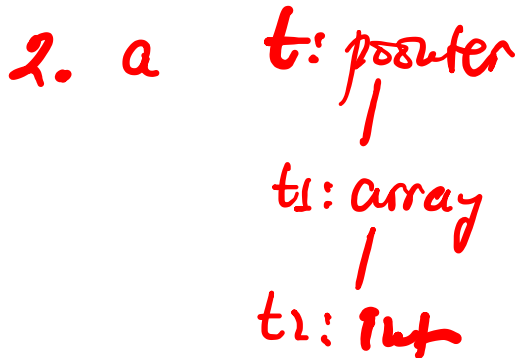
Declarations in C

- What is the meaning of the following declaration in C? Draw the type trees.

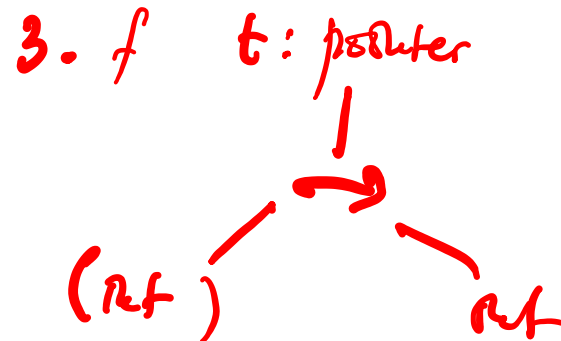
1. `int *a[n]`



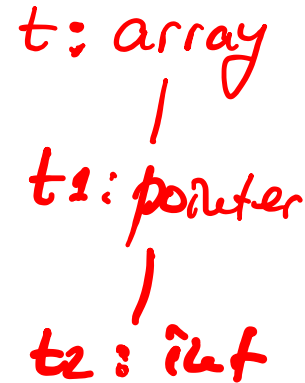
2. `int (*a)[n]`



3. `int (*f)(int)`



1. `a`



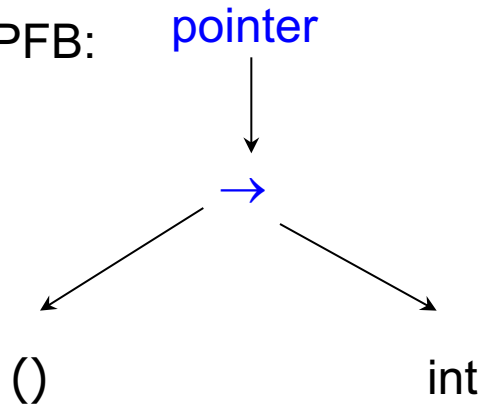
Declarations in C

```
typedef int (*PFB)(); // Type variable PFB: what type?
struct parse_table { // Type struct parse_table: what type?
    char *name;
    PFB func; };
int func1() { ... } // Function func1: what type?
int func2() { ... }

struct parse_table table[] = { // Variable table: what type?
    {"name1", &func1},
    {"name2", &func2}
};
PFB find_p_func(char *s) { // Function find_p_func: what type?
    for (i=0; i<num_func; i++)
        if (strcmp(table[i].name,s)==0) return table[i].func;
    return NULL; }
int main(int argc,char *argv[]) {
    ... }
```

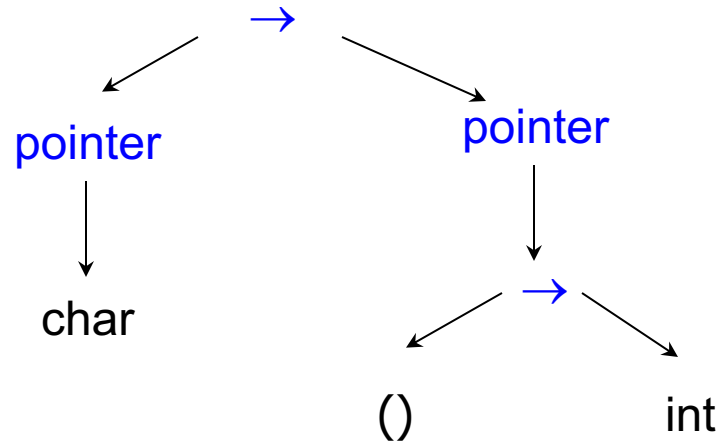
Declarations in C

Type tree for PFB:



Type tree for type of find_p_func:

English: a function that takes a pointer to char as argument, and returns a pointer to a function that takes void as argument and returns int.



Exercise

```
struct _chunk {
    char name[10];
    int id; };
struct obstack {
    struct _chunk *chunk;
    struct _chunk *(*chunkfun)();
    void (*freefun) (); };

void chunk_fun(struct obstack *h, void *f) {
    h->chunkfun = (struct _chunk *(*()) f; }
void free_fun(struct obstack *h, void *f) {
    h->freefun = (void (*)() f; }

int main() {
    struct obstack h;
    chunk_fun(&h,&xmalloc);
    free_fun(&h,&xfree); ... }
```

// Type struct_chunk: what type?

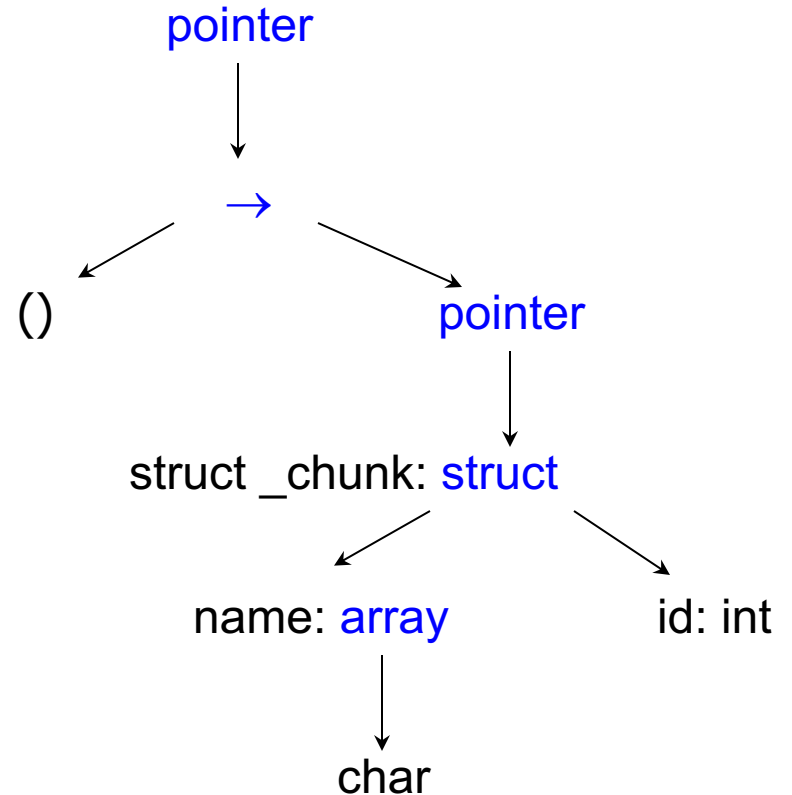
// Type struct_obstack: what type?

// Function chunk_fun: what type?

// Function free_fun: what type?

Declarations in C

Type tree for type of field `chunkfun`:



Lecture Outline

- Types
- Type systems
 - Type checking
 - Type safety
- Type equivalence
- Types in C

- Primitive types
- Composite types

Primitive Types

- A small collection of built-in types
 - integer, float/real, etc.
- Design issues: e.g., boolean
 - Use integer non-0/0 vs. true/false?
- Implementation issues: representation in the machine
 - Integer
 - Length fixed by standards or implementation (portability issues)
 - Multiple lengths (C: short, int, long)
 - Signs
 - Float/real
 - All issues of integers and more

Composite Types: Record (Struct)

- Collection of heterogeneous fields
- Operations
 - Selection through field names (**s.num**, **p->next**)
 - Assignment
 - Example: structures in C

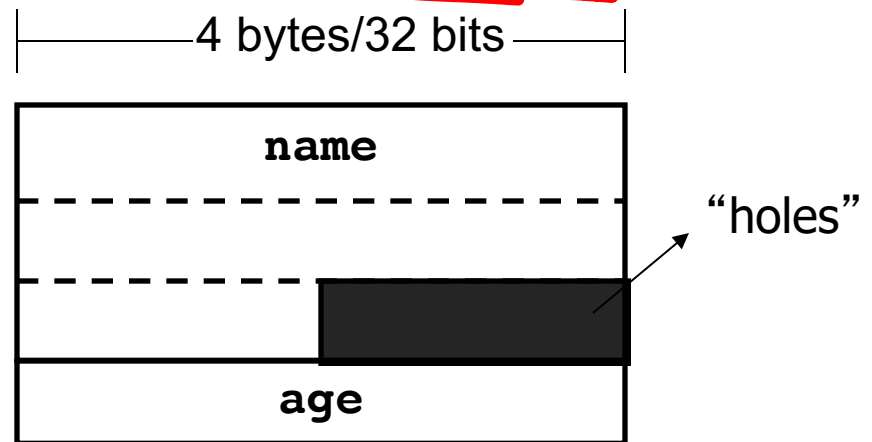
```
typedef struct cell listcell;
struct cell {
    int num;
    listcell *next;
} s, t;
s.num = 0;
s.next = 0;
t = s;
```

Record (Struct)

- Definition of type. What is part of the type?
 - order and type of fields (but not the name)
 - name and type of fields
 - **order, name and type of fields**
- Implementation issues: memory layout
 - Successive memory locations at offset from first byte. Usually, word-aligned, but sometimes **packed**

```
typedef struct {  
    char name[10];  
    int age;  
} Person;
```

```
Person p;
```



Composite Types: Variant (Union)

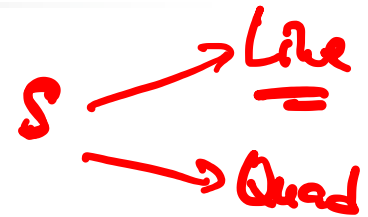
- Allow a collection of alternative fields; only one alternative is valid during execution
 - Fortran: equivalence
 - Algol68 and C: unions
 - Pascal: variant records
- Problem: how can we assure type-safety?
 - Pascal and C are not type-safe
 - Algol68 is type-safe! Uses run-time checks
- Usually, alternatives use same storage
 - Mutually exclusive value access

Variants (Unions)

■ Example: unions in C

```
union data {  
    int k;  
    char c;  
} d1, d2;
```

d1: 



■ Operations

- Selection through field names, Assignment:

```
d1.k = 3; d2 = d1; d2.c = 'b';
```

■ What about type safety?

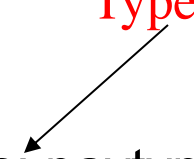
```
if (n>0) d1.k=5 else d1.c='a';
```

```
... d1.k << 2 ... // What is the problem?
```

Pascal's Variant Record

```
program main(input,output);
type paytype = (salaried,hourly);
var employee : record
  id : integer;
  dept: integer;
  age : integer;
  case payclass: paytype of
    salaried:
      (monthlyrate : real;
       startdate : integer);
    hourly:
      (rateperhour : real;
       reghours : integer;
       overtime : integer);
  end;
```

Type tag



```
begin
employee.id:=001234;
employee.dept:=12;
employee.age:=38;
employee.payclass:=hourly;
employee.rateperhour:=2.75;
employee.reghours:=40;
employee.overtime:=3;
writeln(employee.rateperhour,
         employee.reghours,
         employee.overtime);
{this should bomb as there is no
 monthlyrate because
 payclass=hourly}
writeln(employee.monthlyrate);
```

Output:

```
2.750000E+00      40      3
2.750000E+00
```

Pascal Variant Record

```
type paytype = (salaried, hourly);
var employee : record
  id : integer;
  dept: integer;
  age : integer;
  case payclass: paytype of
    salaried:(
      monthlyrate : real;
      startdate : integer);
    hourly: (
      rateperhour : real;
      reghours : integer;
      overtime : integer);
  end;
```

```
employee.payclass:=salaried;
employee.monthlyrate:=575.0;
employee.startdate:=13085;
{this should bomb as there are no
 rateperhour, etc. because
 payclass=salaried}
writeln(employee.rateperhour,
employee.reghours
employee.overtime);
writeln(employee.monthlyrate);
end.
```

Output:

```
5.750000E+02    13085    3
5.750000E+02
```

Composite Types: Array

- Homogeneous, indexed collection of values
- Access to individual elements through subscript

- There are many design choices
 - Subscript syntax
 - Subscript type, element type
 - When to set bounds, compile time or run time?
 - How to initialize?
 - What built-in operations are allowed?

Array

- Definition of type. What is part of the type?
 - bounds/dimension/element type
 - Pascal
 - dimension/element type
 - C, FORTRAN, Algol68
- What is the lifetime of the array?
 - Global lifetime, static shape (in static memory)
 - Local lifetime (in stack memory)
 - Static shape (stored in fixed-length portion of stack frame)
 - Shape bound when control enters a scope
 - (e.g., Ada, Fortran allow definition of array bounds when function is entered; stored in variable-length portion of stack frame)
 - “Global” lifetime, dynamic shape (in heap memory)

Example: Algol68 Arrays

- Array type includes dimension and element type; it does not include bounds

`[1:12] int month; [1:7] int day; row int`

`[0:10,0:10] real matrix;`

`[-4:10,6:9] real table; (row,row) real`

Example - `[1:10] [1:5,1:5] int kinglear;`

- What is the type of `kinglear`? *row (row,row) int*
- What is the type of `kinglear[j]`? *(row,row) int*
- What is the type of `kinglear[j][1,2]`? *int*
- `kinglear[1,2,3]`? *X ERROR*

Array Addressing

- One dimensional array
 - $\mathbf{x}[\mathbf{low}:\mathbf{high}]$ each element is E bytes
 - Assuming that elements are stored into consecutive memory locations, starting at address $\mathbf{addr}(\mathbf{x}[\mathbf{low}])$, what is the address of $\mathbf{x}[\mathbf{j}]$?

$$\mathbf{addr}(\mathbf{x}[\mathbf{low}]) + (\mathbf{j} - \mathbf{low}) * E$$

- E.g, let $\mathbf{x}[\mathbf{0}:\mathbf{10}]$ be an array of reals (4 bytes)
 - $\mathbf{x}[\mathbf{3}]$? is $\mathbf{addr}(\mathbf{x}[\mathbf{0}]) + (\mathbf{3} - \mathbf{0}) * \mathbf{4} = \mathbf{addr}(\mathbf{x}) + \mathbf{12}$
 - $\mathbf{x}[\mathbf{1}]$ is at address $\mathbf{addr}(\mathbf{x}[\mathbf{0}]) + \mathbf{4}$
 - $\mathbf{x}[\mathbf{2}]$ is at address $\mathbf{addr}(\mathbf{x}[\mathbf{0}]) + \mathbf{8}$, etc

Array Addressing

- Memory is a sequence of contiguous locations
- Two memory layouts for two-dimensional arrays:
 - Row-major order and column-major order
- Row-major order:
 - $y[0,0], y[0,1], y[0,2], \dots, y[0,n], y[1,*], y[2,*], \dots$



- $y[\text{low1}:\text{hi1}, \text{low2}:\text{hi2}]$ in Algol68, location $y[j, k]$ is

$$\text{addr}(y[\text{low1}, \text{low2}]) + (\text{hi2} - \text{low2} + 1) * E * (j - \text{low1}) + (k - \text{low2}) * E$$

#locs per row #rows in front # elements in row j in
of row j front of element $[j, k]$

Array Addressing

Consider `y[0:2, 0:5] int matrix`.

Assume row-major order and find the address of `y[1, 3]`.

address of `y[1, 3]` = $\text{addr}(y[0, 0]) + (5-0+1)*4*(1-0) + (3-0)*4$

6 elements per row

1 row before row 1

3 elements in row 1 before 3

$$= \text{addr}(y[0, 0]) + 24 + 12$$

$$= \text{addr}(y[0, 0]) + 36$$



- Analogous formula holds for column-major order
- Row-major and column-major layouts generalize to n-dimensional arrays

Composite Types: Pointers

- A variable or field whose value is a reference to some memory location
 - In C: **int *p;**
- Operations
 - Allocation and deallocation of objects on heap
 - **p = malloc(sizeof(int));** **free(p);**
 - Assignment of one pointer into another
 - **int *q = p; int *p = &a;**
 - Dereferencing of pointer
 - ***q = 1;**
 - Pointer arithmetic
 - **p + 2**

Pointers: Recursive Types

- **A recursive type** is a type whose objects may contain objects of the same type
 - Necessary to build linked structures such as linked lists
- **Pointers** are necessary to define recursive types in languages that use the value model for variables:

```
struct cell {  
    int num;  
    struct cell  next;  
} 
```

Pointers: Recursive Types

- Recursive types are defined naturally in languages that use the reference model for variables:

```
class Cell {  
    int num;  
    Cell next;  
  
    Cell() { ... }  
    ...  
}
```