23. Assembly Mechanics of Manipulation

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Outline.

- Role of assembly
- Assembly sequence planning
- Jamming and wedging
- Compliance

Role of assembly in manufacturing

- Most assembly still manual?
- Assembly automation has a big impact.
- Example: SONY Smart cell
- High volume production uses more specialized machinery.
- Low volume production is usually manual.

Role of assembly, more generally

Assembly is an application of manipulation. It is also a fundamental manipulation technique.

Consider Smart cell again:

- 1. Part is oriented in APOS machine. (By assembling it with pallet nests!)
- 2. Part is grasped by SCARA gripper. (Another assembly.)
- 3. Part is placed in product. (Assembly again.)
- 4. Part is released. (*Not* assembly! Disassembly.)

Even placing an object on a table is an assembly. If assembly is defined to be bringing one shape into a desired configuration relative to another shape, then it is obvious that assembly pervades manipulation.

Issues in assembly

- Assembly sequence. What order to put things together?
- Local constraint analysis. What motions to join two objects?
- Path planning and grasp planning. Finding a free path.
- *Gripper and fixture design.* Being able to apply the desired forces without interfering with the assembly.
- Stable subassembly. Partial assemblies must be stable.
- Assemblability. Even if path exists, parts might be virtually impossible to assemble, due to jamming.
- Tolerances. All issues must also address variations in shape.
- *Design for assembly.* Product design must be integrated with automation design.

Assembly sequence





Assume *two-handed* assembly.

Look at all possible partitions of the parts.

Result is an *and/or* tree.

Every subtree with one and-arc per node is a possible assembly.

Local constraint analysis

To decide if an assembly motion exists,

- 1. Reverse time, consider disassembly problem.
- 2. Look at contact constraints, identify all motion freedoms.
- 3. First order form analysis often is sufficient.

Remember the refrigerator problem?

Jamming and wedging

One of the earliest papers on the mechanics of manipulation was by Simunovic, in 1974, studying assembly of peg in hole. This was part of a larger project studying manufacturing issues at the Draper Labs, supervised by Nevins and Whitney.

- Study of several assemblies showed that just a few operations dominate manufacturing. Assembly, joining, etc.
- Also, just a few directions of motion dominate all assemblies. Mostly vertical.
- Simunovic defined jamming and wedging:

Jamming. An assembly force in equilibrium with the contact forces.

Wedging. A configuration such that *every* possibly force is in equilibrium with the contact forces. I.e. force closure.

Jamming and wedging



Simunovic's analysis of wedging anticipated Nguyen's approach to planar force closure.

Simunovic's analysis of jamming anticipated the moment labeling method. Jamming may occur if the applied force makes positive moment at *P*.

Analysis of wedging



Analysis of jamming





Compliance



Compliance elements rubber/steel sandwiches stiff in compression soft in sheer

Compliance center

- Active force control is an option.
- Remote Center Compliance is a passive mechanism.
- Compliance Center: behaves like decoupled translational and rotational springs.
- Put compliance center at tip of peg or at lip of hole.

Lecture 23.

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