

Robotics II Final, Spring 2011.

T/F 4 points each

1. In all friction form closure grasps, every contact point can at least one other contact point in its friction cone.
2. Unit quaternions have 4 elements, but only three degrees of freedom.
3. Some LCPs arising in the Stewart-Trinkle time stepping method have non unique solutions.
4. A* search with cost-to-come = 0 is equivalent to Best-First search
5. Sample-based methods are preferred in motion planning, because the number of samples needed for a given resolution is independent of the dimension

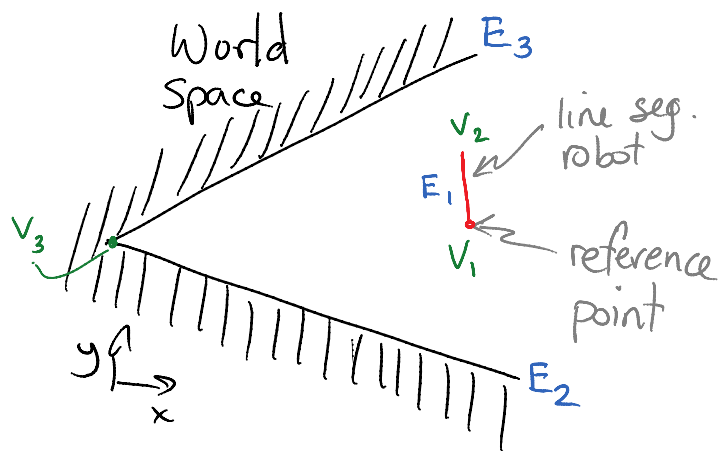
of C -space.

6. A robot with 7 joints and a position-controlled parallel-jaw gripper has an 8-dimensional C -space.

8 points each

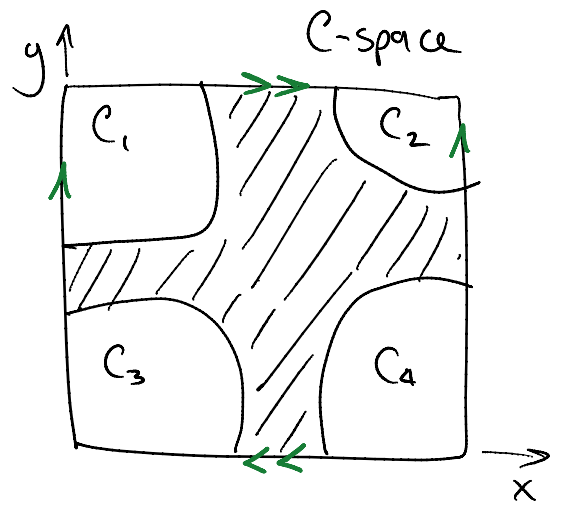
Short Answer Questions

1. Sketch the curves in the workspace when the radio plots change qualitatively (these are known as critical curves). Label the curves (E_1, V_1), etc

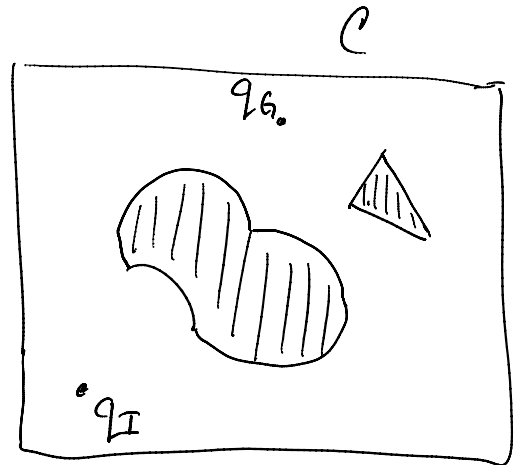


2. Describe how a randomized potential field method works and how it escapes local minima. Under what circumstances does it fail?

3. Let \mathcal{C} be the "disk" shown on the right. Without the identifications shown, \mathcal{C} has 4 components. How many components exist with the identifications shown?

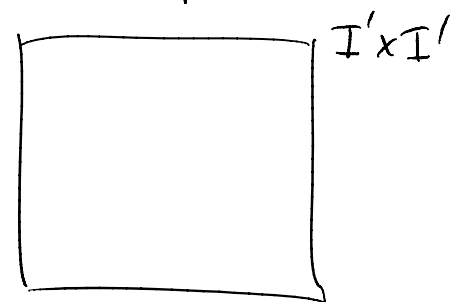


4. For the \mathcal{C} -space shown on the right, extend the idea of a visibility graph to curved objects.



Draw the graph for the obstacles and q_I and q_G .

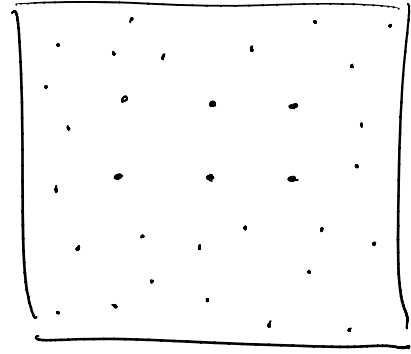
5. Give pseudo-code defining a van der Corput sequence on a disc in \mathbb{R}^2 .



6. Find the points of maximum dispersion in the region shown

dispersion in the region shown on the right.

Compare results for two metrics: L_1 and L_∞



7. Describe the main differences between sampling-based and combinatorial motion planning methods.

Analysis Questions (10 points each)

1. Let X be a ^{vector} space and let $x \neq x'$ be points in X .

Prove that $\rho(x, x') = \text{abs}(x - x')$ is or is not a metric.

Note that $\text{abs} = \text{absolute value}$, which applies to each element of a vector.

2. Define the most impressive analysis problem you prepared for, but I didn't ask. Then solve it.