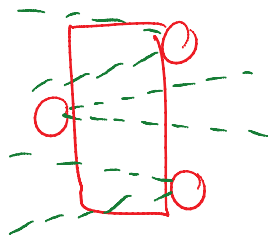


## Robotics II Final, Spring 2011.

T/F 4 points each

1. In all friction form closure grasps, every contact point see can at least one other contact point in its friction cone.

F



This has force closure.

2. Unit quaternions have 4 elements, but only three degrees of freedom.

T since there is a constraint  $h_1^2 + h_2^2 + h_3^2 + h_4^2 = 1$ 

3. Some LCPs arising in the Stewart-Trinkle time stepping method have non unique solutions.

T

4. A\* search with cost-to-come = 0 is equivalent to Best-First search

F it is equiv to Dijkstra's alg.

5. Sample-based methods are preferred in motion planning, because the number of samples needed for a given resolution is independent of the dimension of C-space.

F it is exponential in dimension

6. A robot with 7 joints and a position-controlled parallel-jaw gripper has an 8-dimensional C-space.

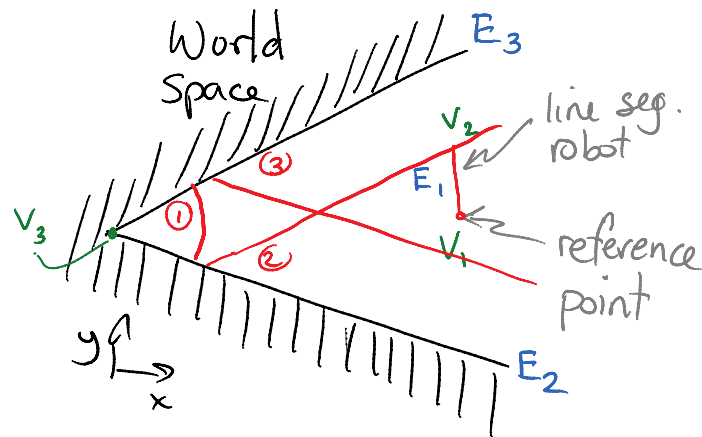
T

8 points each

Short Answer Questions

1. Sketch the curves in the workspace when the radar plots change qualitatively (these are known as critical curves).

Label the curves  $(E_1, V_1)$ , etc

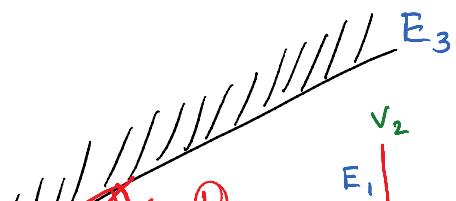


①  $(V_1, V_3) = (V_1, E_2) \cap (V_1, E_3)$

②  $(V_2, E_3)$

③  $(V_2, E_2)$

There are also two others that are harder to draw:



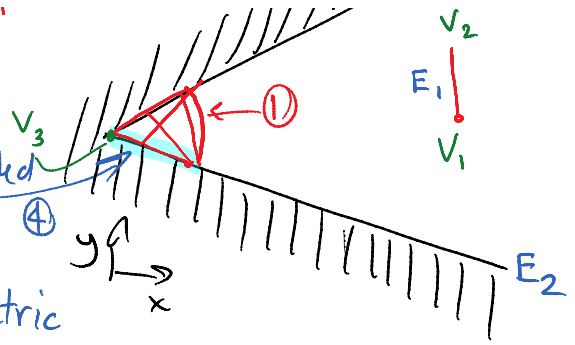
There are also two others that

are harder to draw:

$$\textcircled{4} (V_1, E_2) \wedge (V_2, E_3)$$

$$\textcircled{5} (V_1, E_3) \wedge (V_2, E_2)$$

The highlighted blue arc is  $\textcircled{4}$   
 $\textcircled{5}$  is symmetric



Critical curves  $\textcircled{4}$  &  $\textcircled{5}$  start on  $V_3$  & end on  $\textcircled{1}$ .

There are still more:

$$(V_1, E_2) \wedge (V_2, E_2)$$

also  $(V_1, E_2) \wedge (V_2, E_2)$  flipped



Similarly,  $(V_1, E_3) \wedge (V_2, E_3)$

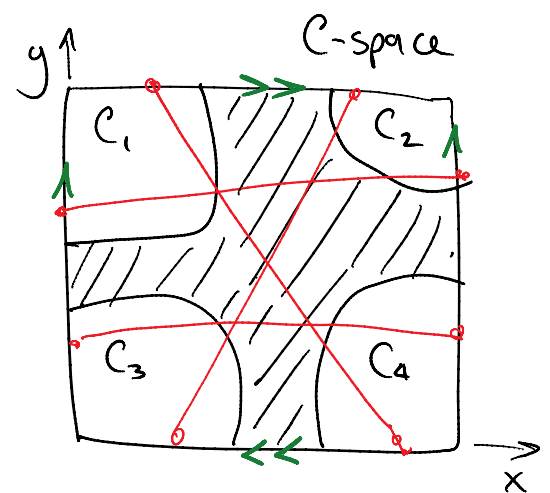
also  $(V_1, E_3) \wedge (V_2, E_3)$  flipped

2. Describe how a randomized potential field method works and how it escapes local minima. Under what circumstances does it fail?

Obstacles are assigned force fields that repel the robot. The initial and goal configs are assigned repulsive and attractive force field as well. The two are added to create a force field on C-space that hopefully makes the goal the unique global minimum, but this is typically not the case.

In the potential field method, one searches along the field's gradient until  $q_{goal}$  is reached or  $q$  is trapped. If trapped, random walk for a while. Follow gradient again. No guarantee that a random walk will escape a trap!

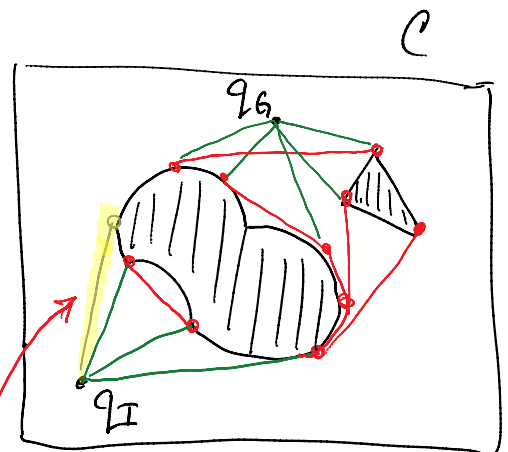
3. Let  $C$  be the "disk" shown on the right. Without the identifications shown,  $C_{free}$  has 4 components. How many components exist with the identifications shown?



1.  $C_1$  connects to  $C_4 \neq C_2$ .  $C_2$  connects to  $C_3$ .

4. For the C-space shown on the right, extend the idea of a visibility graph to curved objects.

Draw the graph for the



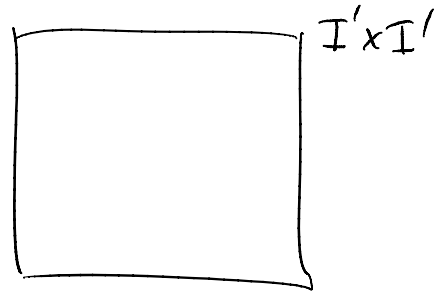
To be analogous, we



Draw the graph for the obstacles and  $q_I$  and  $q_G$ .

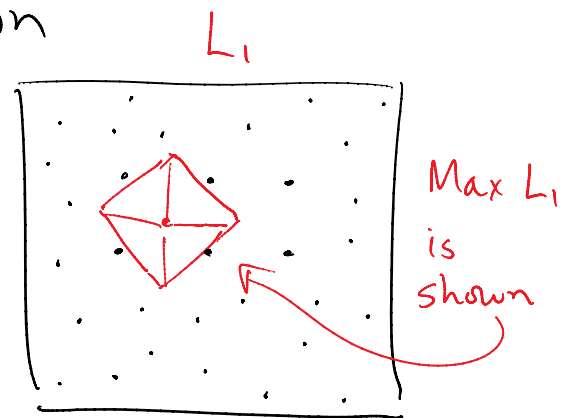
To be analogous, we should really include this extra arc & node)

5. Give pseudo-code defining a van der Corput sequence on a disc in  $\mathbb{R}^2$ .



6. Find the points of maximum dispersion in the region shown on the right.

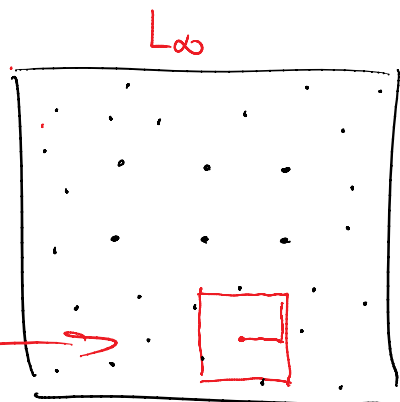
Compare results for two metrics:  $L_1$  and  $L_\infty$



$L_1 \Rightarrow$  max coord change

$L_\infty \Rightarrow$  Manhattan distance

Max  $L_\infty$  is sum of the 2 lgs from middle to corner



7. Describe the main differences between sampling-based

and combinatorial motion planning methods.

Sampling-Based

We only approx  $C_{free}$

Combinatorial

We compute  $C_{free}$  explicitly

## Analysis Questions (10 points each)

1. Let  $X$  be a <sup>vector</sup> space and let  $x \neq x'$  be points in  $X$ .

Prove that  $\rho(x, x') = \text{abs}(x - x')$  is or is not a metric.

Note that  $\text{abs} =$  absolute value, which applies to each element of a vector.

$\rho$  is a vector &  $\therefore$  not a metric.

If you considered  $x \in \mathbb{R}^1$ , then  $\text{abs}(\cdot)$  satisfies the properties required of a metric:

nonnegativity:  $\rho(x, x') \geq 0 \quad \forall x, x'$

reflexivity:  $\rho(x, x') = 0$  iff  $x = x'$

Symmetry:  $\rho(x, x') = \rho(x', x)$

Triangle ineq:  $\rho(x, x') + \rho(x', x'') \geq \rho(x, x'')$

2. Define the most impressive analysis problem you prepared for, but I didn't ask. Then solve it.