
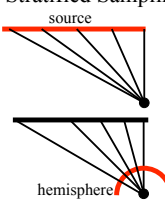
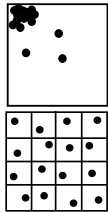


# Irradiance Caching & Photon Mapping

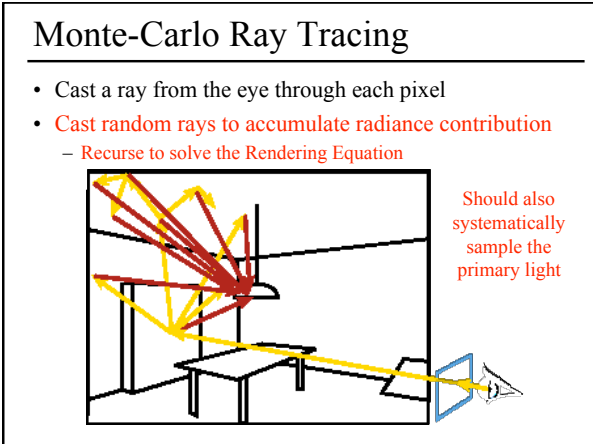
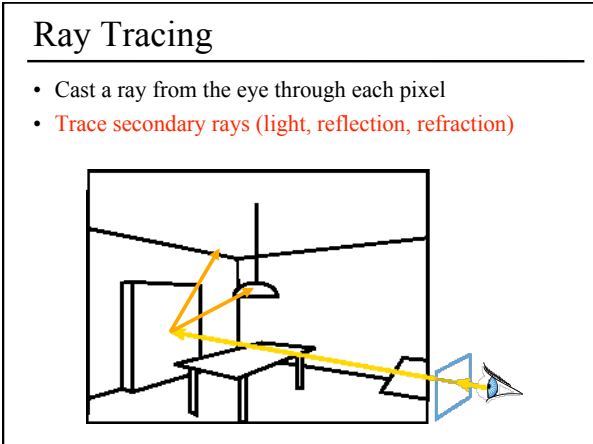
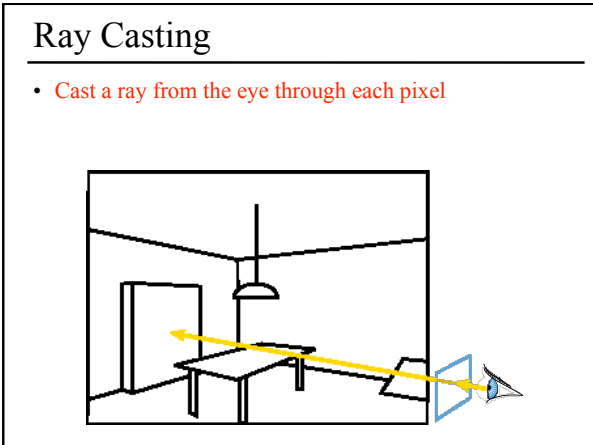
## Last Time?

$$L(x', \omega') = E(x', \omega') + \int_{\rho, (\omega, \omega')} L(x, \omega) G(x, x') V(x, x') dA$$

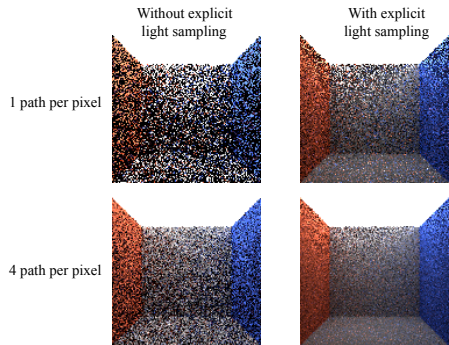
- Rendering Equation
- Monte-Carlo Integration
- Monte Carlo Rendering
- Forward Ray Tracing
- Stratified Sampling

- ## Today
- Monte-Carlo Ray Tracing vs. Path Tracing
  - Irradiance Caching
  - Photon Mapping
  - Acceleration Data Structures
  - Ray Grammar

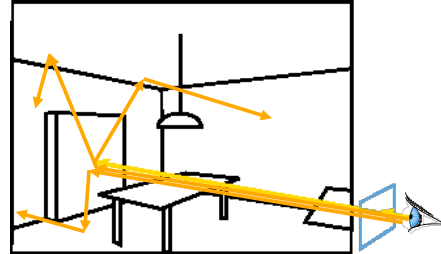


## Importance of Sampling the Light

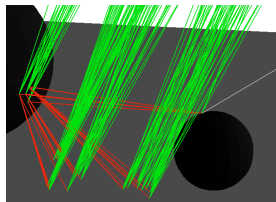


## Monte Carlo Path Tracing

- Trace only one secondary ray per recursion
- But send many primary rays per pixel (performs antialiasing as well)



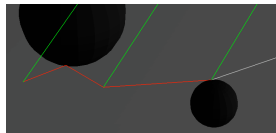
## Ray Tracing vs. Path Tracing



2 bounces  
5 glossy samples  
5 shadow samples

How many rays cast per pixel?

1 main ray + 5 shadow rays +  
5 glossy rays + 5x5 shadow rays +  
5\*5 glossy rays + 5x5x5 shadow rays  
= 186 rays



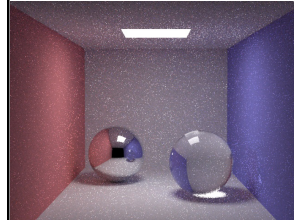
How many 3 bounce paths can we trace per pixel for the same cost?

186 rays / 8 ray casts per path  
= ~23 paths

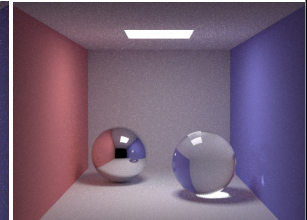
Which will probably have less error?

## Questions?

10 paths/pixel



100 paths/pixel



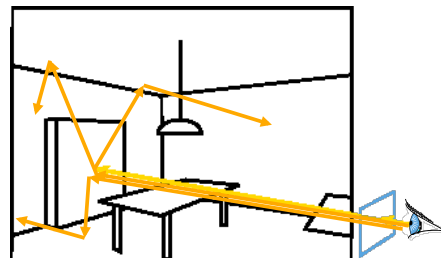
Images from Henrik Wann Jensen

## Today

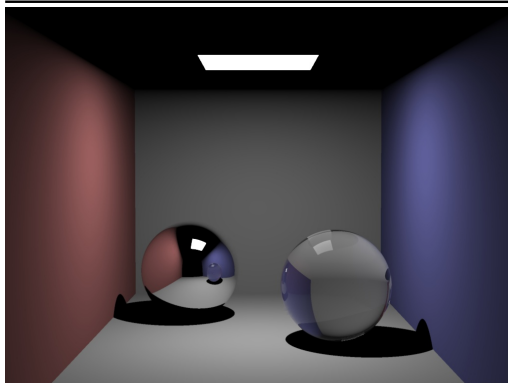
- Monte-Carlo Ray Tracing vs. Path Tracing
- Irradiance Caching
- Photon Mapping
- Acceleration Data Structures
- Ray Grammar

## Path Tracing is costly

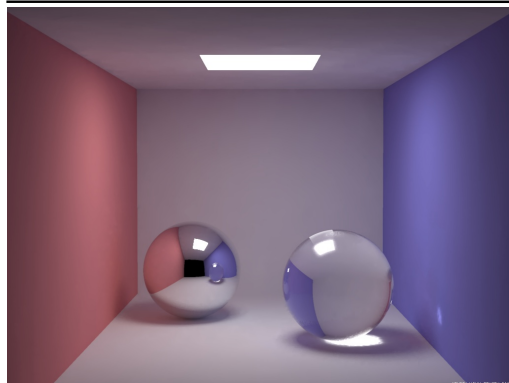
- Needs tons of rays per pixel



### Direct Illumination



### Global Illumination

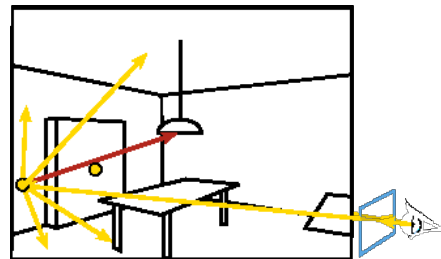


### Indirect Illumination: smooth



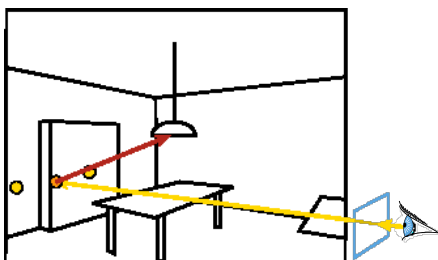
### Irradiance Cache

- The indirect illumination is smooth
- Store the indirect illumination

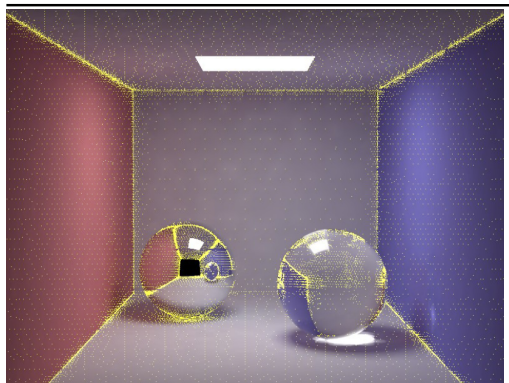


### Irradiance Cache

- Interpolate nearby cached values
- But do full calculation for direct lighting

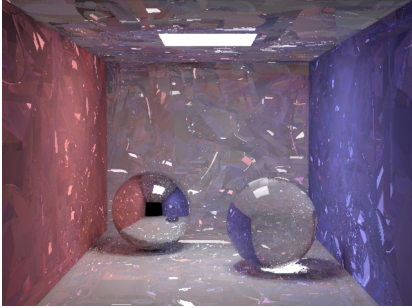


### Irradiance Cache



## Questions?

- Why do we need “good” random numbers?
  - With a fixed random sequence, we see the structure in the error

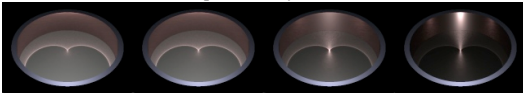


## Today

- Monte-Carlo Ray Tracing vs. Path Tracing
- Irradiance Caching
- **Photon Mapping**
- Acceleration Data Structures
- Ray Grammar

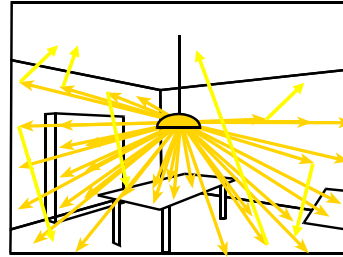
## Readings for Today (*pick one*)

- “Rendering Caustics on Non-Lambertian Surfaces”,  
Henrik Wann Jensen, *Graphics Interface* 1996.
- “Global Illumination using Photon Maps”,  
Henrik Wann Jensen, *Rendering Techniques* 1996.



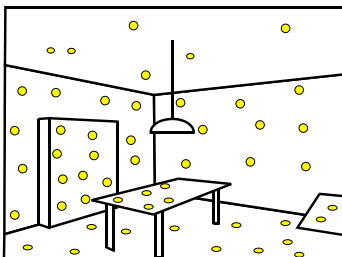
## Photon Mapping

- Preprocess: cast rays from light sources
  - independent of viewpoint



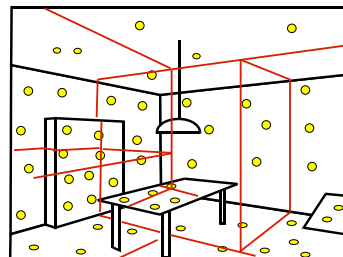
## Photon Mapping

- Store photons
  - position + light power + incoming direction



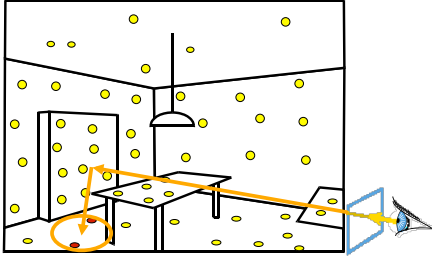
## Photon Map

- Efficiently store photons for fast access
- Use hierarchical spatial structure (kd-tree)

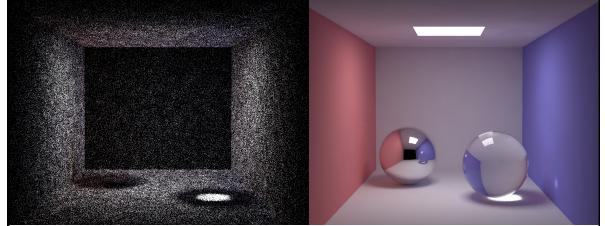


## Rendering with Photon Map

- Cast primary rays
- For secondary rays
  - reconstruct irradiance using  $k$  closest photons
- Combine with irradiance caching and other techniques

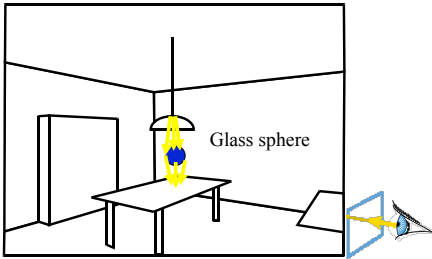


## Photon Map Results



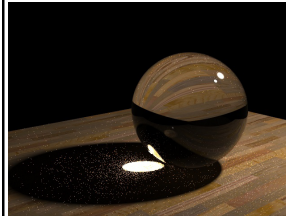
## Photon Mapping - Caustics

- Special photon map for specular reflection and refraction

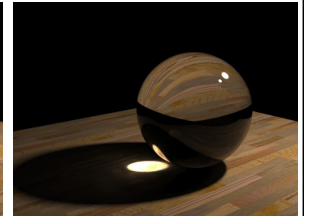


## Comparison

Path Tracing  
1000 paths/pixel



Photon mapping

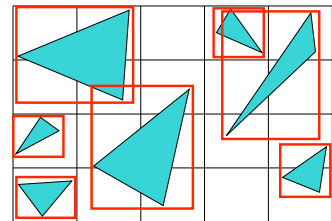


## Today

- Monte-Carlo Ray Tracing vs. Path Tracing
- Irradiance Caching
- Photon Mapping
- **Acceleration Data Structures**
- Ray Grammar

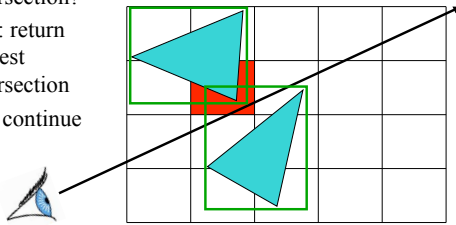
## Regular Grid

- Primitives that overlap multiple cells?
- Insert into multiple cells (use pointers)



## For Each Cell Along a Ray

- Does the cell contain an intersection?
- Yes: return closest intersection
- No: continue

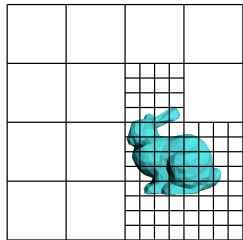


## Regular Grid Discussion

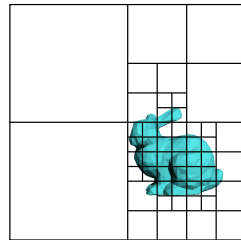
- Advantages?
  - easy to construct
  - easy to traverse
- Disadvantages?
  - may be only sparsely filled
  - geometry may still be clumped

## Adaptive Grids

- Subdivide until each cell contains no more than  $n$  elements, or maximum depth  $d$  is reached



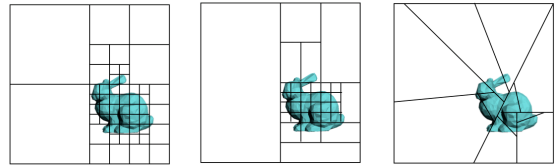
Nested Grids



Octree/(Quadtree)

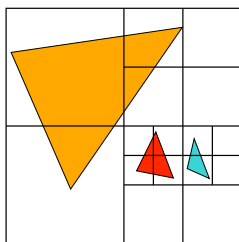
## Variations of Adaptive Grids

- **When to split?** When a cell contains “lots” of geometry, but has not yet reached the max tree depth
- **Where to split?**
  - Quadtree/Octree: split *every* dimension in half, always axis aligned
  - kd-tree: choose *one* dimension (often the largest dimension) and split it axis aligned (but not necessarily at the midpoint)
  - Binary Space Partition (BSP): choose a *arbitrary* cut plane
- **Which one is best?** It depends.... Often they are all equally good!

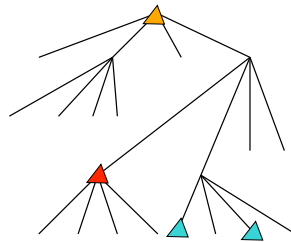


## Primitives in an Adaptive Grid

- Can live at intermediate levels, or be pushed to lowest level of grid

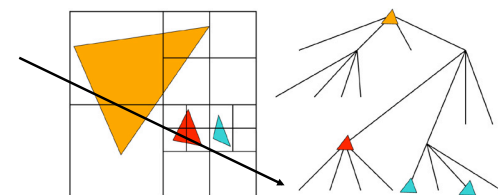


Octree/(Quadtree)



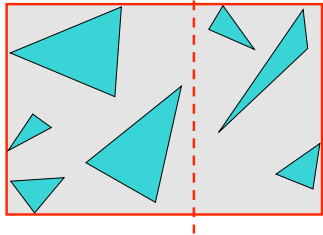
## Adaptive Grid Discussion

- Advantages?
  - grid complexity matches geometric density
- Disadvantages?
  - more expensive to traverse (binary tree, lots of pointers)



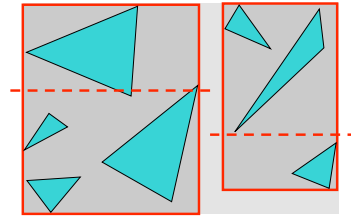
## Bounding Volume Hierarchy

- Find bounding box of objects
- Split objects into two groups
- Recurse



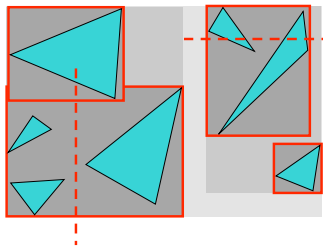
## Bounding Volume Hierarchy

- Find bounding box of objects
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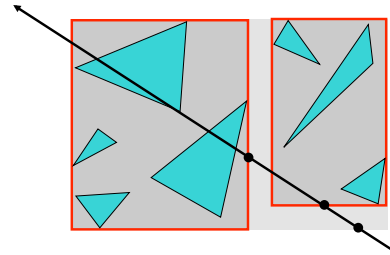
## Where to split objects?

- At midpoint *OR*
- Sort, and put half of the objects on each side *OR*
- Use modeling hierarchy



## Intersection with BVH

- Check sub-volume with closer intersection first



## Bounding Volume Hierarchy Discussion

- Advantages
  - easy to construct
  - easy to traverse
  - binary
- Disadvantages
  - may be difficult to choose a good split for a node
  - poor split may result in minimal spatial pruning

## Today

- Monte-Carlo Ray Tracing vs. Path Tracing
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## Ray Grammar

- Classify local interaction:

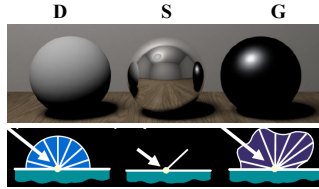
E = eye

L = light

S = perfect specular reflection or refraction

G = glossy scattering

D = diffuse scattering

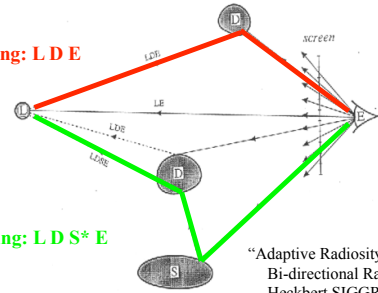


From Dutre et al.'s slides

## Classic Ray Casting/Tracing

Ray casting:  $L D E$

Ray tracing:  $L D S^* E$

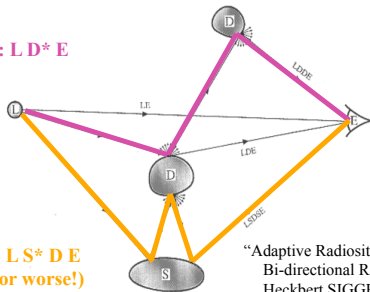


"Adaptive Radiosity Textures for Bi-directional Ray Tracing"  
Heckbert SIGGRAPH 1990

## Photon Tracing

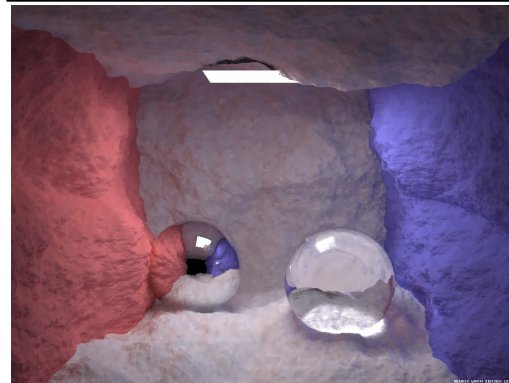
Radiosity:  $L D^* E$

Caustics:  $L S^* D E$   
(or worse!)



"Adaptive Radiosity Textures for Bi-directional Ray Tracing"  
Heckbert SIGGRAPH 1990

## Questions?



## Reading for Tuesday 3/30:

"Two Methods for the Display of High Contrast Images",  
Tumblin, Hodgins, & Guenter, ACM Trans on Graphics 1999

Truncation

Compression

"Layering"

