Voxels, Implicit Surfaces, & Collisions

Last Time?

- Spring-Mass Systems
- MILLIN MAN CANNON CANNAN • Numerical Integration (Euler, Midpoint, Runge-Kutta)
- Modeling string, hair, & cloth



Today

- More on Cloth! - Stiffness
 - Implicit Integration
- Implicit Surfaces
- Voxels
- Collisions
- · Readings for Today

The Stiffness Issue

- What relative stiffness do we want for the different springs in the network?
- Cloth is barely elastic, shouldn't stretch so much!
- Inverse relationship between stiffness & Δt
- We really want constraints (not springs)
- · Many numerical solutions
 - reduce Δt
 - use constraints
 - implicit integration
 - . . .





• Using (explicit) Euler, how many timesteps before a force propagates across the mesh?







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Detecting Collisions

- · Easy with implicit equations of surfaces
- H(x,y,z)=0 at surface
- H(x,y,z)<0 inside surface
- So just compute H and you know that you're inside if it's negative
- More complex with other surface definitions





Collision Detection for Solids

- How to detect collision between 2 polyhedra?
- · Need an inside/outside test
- Test if a vertex is inside the other polyhedron
- But treat also edge-edge intersection



Reading for Today

• "I-COLLIDE: An Interactive and Exact Collision Detection System for Large-scaled Environments", Cohen, Lin, Manocha, & Ponamgi, I3D 1995.



Cost of Detection?

- Test each edge with each face? $O(N^2)$
- How would you detect collision between two bunnies?
 - $O(N^2)$ is too expensive!
 - Use spatial hierarchy





Overlap test

• Overlap between two axis-aligned boxes? - Check if the intervals along the 3 dimensions overlap



General Collision Detection

- Put a hierarchy around your objects
- Use the fast overlap test recursively
- Handle exact case at the leaves (when necessary)
- More difficult for self-collision (e.g. cloth)



Collision Pruning via Uniform Grid • Primitives that overlap multiple cells?













