Ray Tracing

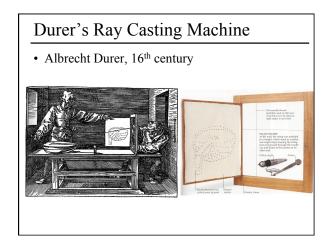
Announcements: Quiz

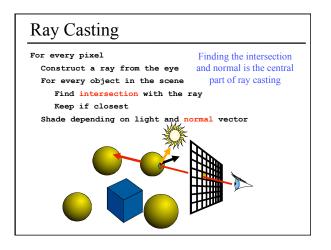
- On Friday (3/4), in class
- One 8.5x11 sheet of notes allowed
- Sample quiz (from last year) is posted online
- Focus on "reading comprehension" and material for Homeworks 0, 1, & 2

Rigid Body Finite Element Method Stress/Strain Fracture Deformation Level of Detail Haptics

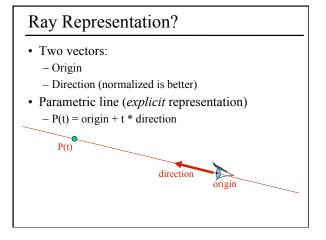
Today

- Ray Casting
 - Ray-Plane Intersection
 - Ray-Sphere Intersection
 - Point in Polygon
- Ray Tracing
- Recursive Ray Tracing
- Distribution Ray Tracing

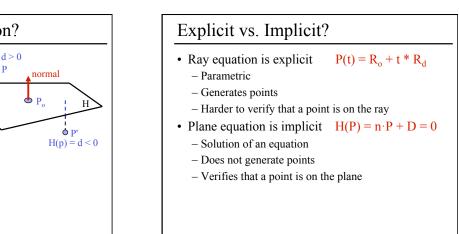


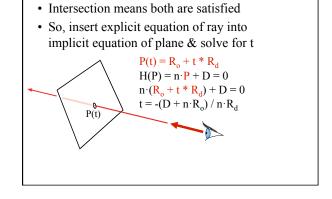


A Note on Local Shading • Surface/Scene Characteristics: - surface normal - direction to light - viewpoint • Material Properties - Diffuse (matte) - Specular (shiny) - ... • More later! Diffuse sphere Specular spheres

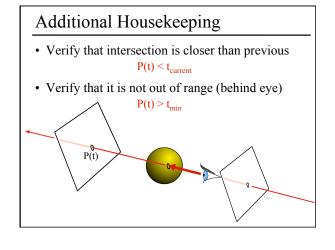


Plane Representation? Plane defined by - P_o = (x,y,z) - n = (A,B,C) Implicit plane equation - H(P) = Ax+By+Cz+D = 0 = n·P + D = 0 Point-Plane distance? If n is normalized, distance to plane, d = H(P) - d is the signed distance!



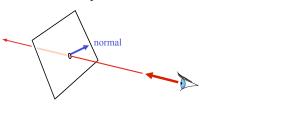


Ray-Plane Intersection



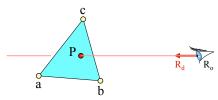
Normal

- · Needed for shading
 - diffuse: dot product between light and normal
- Normal of a plane is constant!



Ray-Triangle Intersection

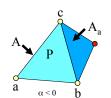
- Use barycentric coordinates:
 - $-P(\alpha, \beta, \gamma) = \alpha a + \beta b + \gamma c$ with $\alpha + \beta + \gamma = 1$
 - If $0 < \alpha < 1$ & $0 < \beta < 1$ & $0 < \gamma < 1$ then the point is inside the triangle!



How Do We Compute α , β , γ ?

- Ratio of opposite sub-triangle area to total area $-\alpha = A_a/A$ $\beta = A_b/A$ $\gamma = A_c/A$
- Use signed areas for points outside the triangle





Sut how do I know if the point is outside the triangle That's what I was trying to determine!

Using Cramer's Rule...

• Used to solve for one variable at a time in system of equations

$$\beta = \frac{\begin{vmatrix} a_x - R_{ox} & a_x - c_x & R_{dx} \\ a_y - R_{oy} & a_y - c_y & R_{dy} \\ a_z - R_{oz} & a_z - c_z & R_{dz} \end{vmatrix}}{|A|} \qquad \gamma = \frac{\begin{vmatrix} a_x - b_x & a_x - R_{ox} & R_{dx} \\ a_y - b_y & a_y - R_{oy} & R_{dy} \\ a_z - b_z & a_z - R_{oz} & R_{dz} \end{vmatrix}}{|A|}$$

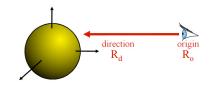
$$t = \begin{vmatrix} a_x - b_x & a_x - c_x & a_x - R_{ox} \\ a_y - b_y & a_y - c_y & a_y - R_{oy} \\ a_z - b_z & a_z - c_z & a_z - R_{oz} \\ |A| \end{vmatrix}$$

| | denotes the determinant

Can be copied mechanically into code

Sphere Representation?

- Implicit sphere equation
 - Assume centered at origin (easy to translate)
 - $-H(P) = P \cdot P r^2 = 0$



Ray-Sphere Intersection

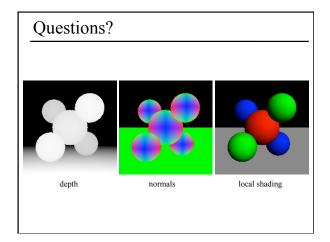
• Insert explicit equation of ray into implicit equation of sphere & solve for t

Ray-Sphere Intersection

- Quadratic: $at^2 + bt + c = 0$
 - -a = 1 (remember, $||R_d|| = 1$)
 - $-b = 2R_d \cdot R_o$
 - $-c = R_0 \cdot R_0 r^2$
- with discriminant $d = \sqrt{b^2 4ac}$
- and solutions

$$t_{\pm} = \frac{-b \pm d}{2a}$$

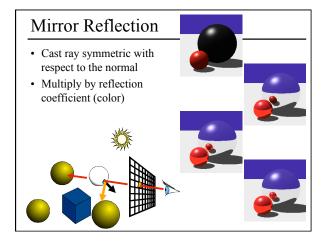
• What does it mean if there are no solutions, 1 solution, or 2 solutions?

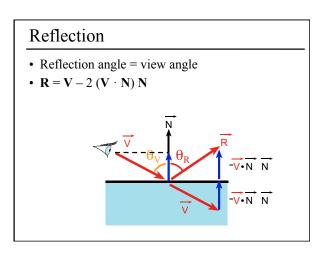


Today

- Ray Casting
- Ray Tracing
 - Shadows
 - Reflection
 - Refraction
- Recursive Ray Tracing
- Distribution Ray Tracing

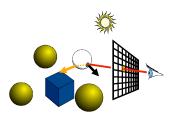
How Can We Add Shadows? Find the point to be shaded For every light, Construct ray from point to light For every object find intersection of ray with object If no objects between point and light Add contribution from light

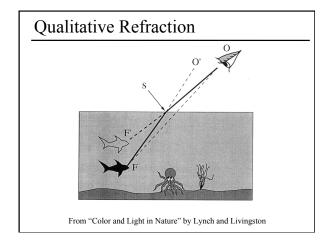


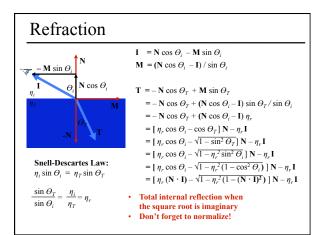


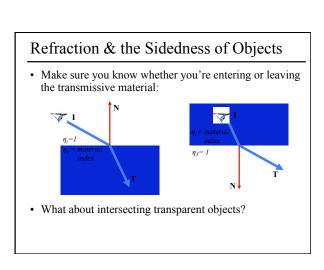
Transparency

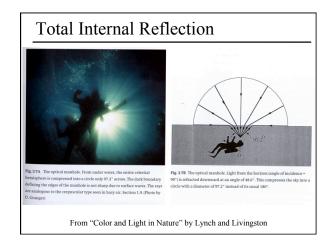
- Cast ray in refracted direction
- Multiply by transparency coefficient (color)

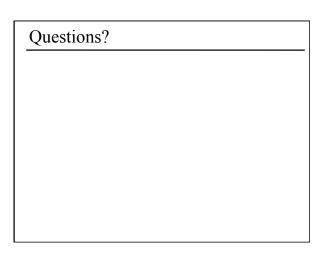






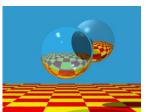






Readings for Today: (read both)

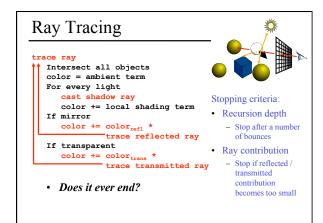
- "An improved illumination model for shaded display" Turner Whitted, 1980.
- "Distributed Ray Tracing", Cook, Porter, & Carpenter, SIGGRAPH 1984.

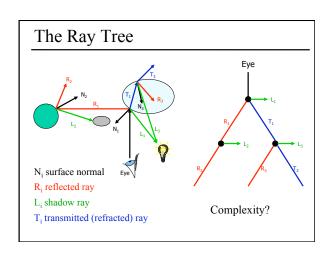


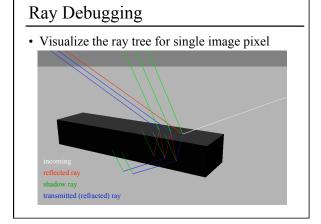


Today

- Ray Casting
- · Ray Tracing
- Recursive Ray Tracing
- Distribution Ray Tracing







Today

- · Ray Casting
- Ray Tracing
- Recursive Ray Tracing
- Distribution Ray Tracing
 - Soft shadows
 - Antialiasing (getting rid of jaggies)
 - Glossy reflection
 - Motion blur
 - Depth of field (focus)

