Local vs. Global Illumination & Radiosity



An early application of radiative heat transfer in stables.

Announcements: Final Projects

- Everyone should post one or more ideas for a final project on LMS ("due" this Monday 3/18 @ 11:59pm)
- Connect with potential teammates (teams of 2 strongly recommended)
- Start finding & reading background papers
- Proposal & summary of background research are due April 4th (see final_project.html for details on proposal/project requirements)

Ray Casting & Ray-Object Intersection Recursive Ray Tracing Distributed Ray Tracing

Today

- Local Illumination
 - BRDF
 - Ideal Diffuse Reflectance
 - Ideal Specular Reflectance
 - The Phong Model
- Why is Global Illumination Important?
- · Radiosity Matrix
- Calculating the Form Factors
- Advanced Radiosity

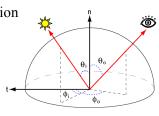
BRDF

- Ratio of light coming from one direction that gets reflected in another direction
- Bidirectional Reflectance Distribution Function

-4D

 $-\,R(\theta_i\,,\!\varphi_i\,;\theta_o,\,\varphi_o)$

-Note: BRDF for *isotropic* materials is 3D

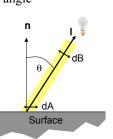


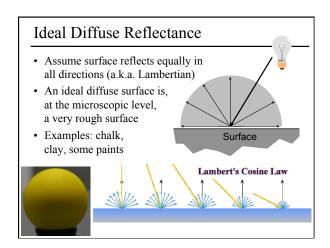
Incoming Radiance

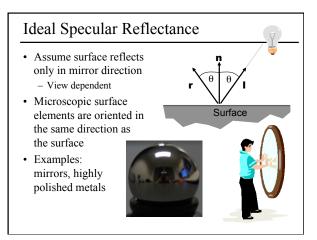
- The amount of light received by a surface depends on incoming angle
 - Bigger at normal incidence (Winter/Summer difference)

• By how much?

- $-dB = dA \cos \theta$
- Same as: I · n (dot product with normal)







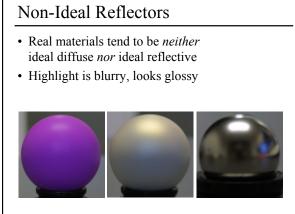
• Most light reflects in the ideal reflected direction

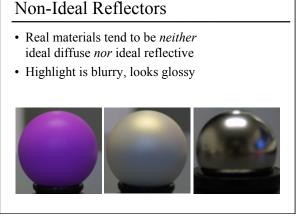
• Microscopic surface variations will reflect light

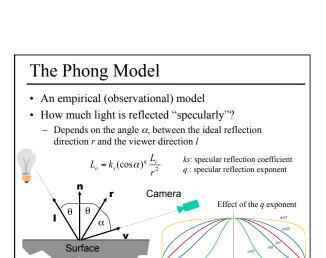
Non-Ideal Reflectors

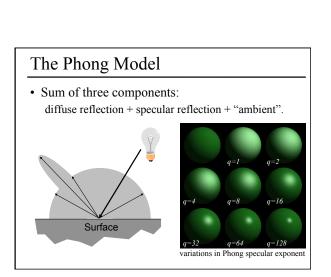
• How much light is reflected?

just slightly offset



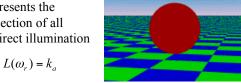






Ambient Illumination

- In a typical room, everything receives at least a little bit of light
- Ambient illumination represents the reflection of all indirect illumination



• This is a total hack!

Questions?



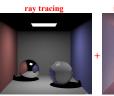
Lightscape http://www.lightscape.com

Today

- Local Illumination
- Why is Global Illumination Important?
 - The Cornell Box
 - Radiosity vs. Ray Tracing
- Radiosity Matrix
- Calculating the Form Factors
- · Advanced Radiosity

Why Global Illumination?

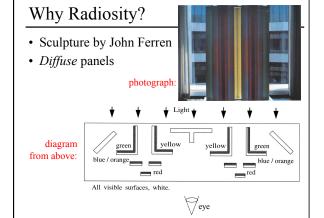
- Simulate all light inter-reflections (indirect lighting)
 - in a room, a lot of the light is indirect: it is reflected by walls.
- How have we dealt with this so far?
 - Ambient term to fake some uniform indirect light

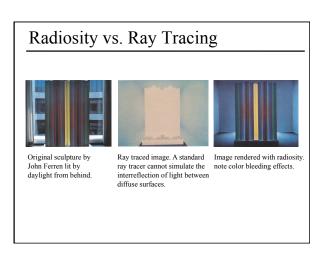


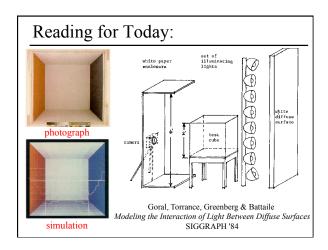


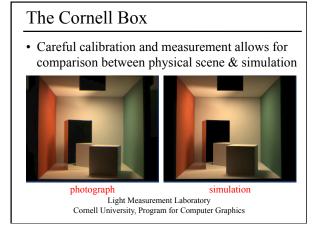


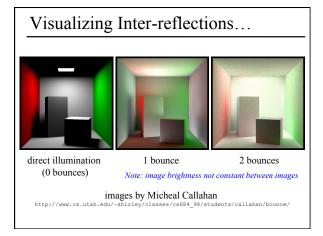
Henrik Wann Jensen







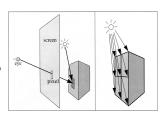




Radiosity vs. Ray Tracing

- Ray tracing is an *image-space* algorithm

 If the camera is moved, we have to start over
- Radiosity is computed in *object-space*
 - View-independent (just don't move the light)
 - Can pre-compute complex lighting to allow interactive walkthroughs

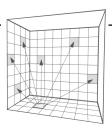


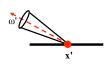
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Radiosity Overview

- Surfaces are assumed to be perfectly Lambertian (diffuse)
 reflect incident light in all
 - reflect incident light in all directions with equal intensity
- The scene is divided into a set of small areas, or patches.
- The radiosity, B_i, of patch i is the total rate of energy leaving a surface. The radiosity over a patch is constant.
- Units for radiosity: Watts / steradian * meter²





Discrete Radiosity Equation

Discretize the scene into n patches, over which the radiosity is constant



light leaving patch
$$i$$
 reflectivity
$$B_i = E_i + \rho_i \sum_{j=1}^n F_{ij} B_j$$
light emitted from patch i

The equation is recursive, but it can be solved iteratively

Radiosity in Matrix Form

$$B_i = E_i + \rho_i \sum_{j=1}^n F_{ij} B_j$$

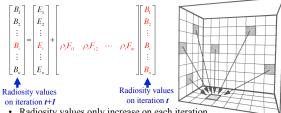
n simultaneous equations with n unknown B_i values can be written in matrix form:

$$\begin{bmatrix} 1 - \rho_1 F_{11} & -\rho_1 F_{12} & \cdots & -\rho_1 F_{1n} \\ -\rho_2 F_{21} & 1 - \rho_2 F_{22} & & & & \\ \vdots & & \ddots & & & \\ -\rho_n F_{n1} & \cdots & \cdots & 1 - \rho_n F_{nn} \end{bmatrix} \begin{bmatrix} \mathbf{b}_1 \\ \mathbf{b}_2 \\ \vdots \\ \mathbf{b}_n \end{bmatrix} = \begin{bmatrix} E_1 \\ E_2 \\ \vdots \\ E_n \end{bmatrix}$$

A solution yields a single radiosity value B_i for each patch in the environment, a view-independent solution.

Solving the Radiosity Matrix

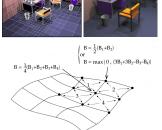
- Initialize all radiosity values to 0
- Each iteration, update the radiosity of each patch by gathering the contribution of radiosities from all other patches:



- · Radiosity values only increase on each iteration
- · This method is fundamentally a Gauss-Seidel relaxation

Interpolating Vertex Radiosities

- · B_i radiosity values are constant over the extent of a patch.
- How are they mapped to the vertex radiosities (intensities) needed by the renderer?
 - Average the radiosities of patches that contribute to the vertex
 - Vertices on the edge of a surface are assigned values extrapolation



Questions?



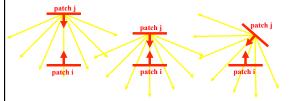
Factory simulation. Program of Computer Graphics, Cornell University. 30,000 patches.

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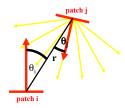
Calculating the Form Factor F_{ij}

- F_{ij} = fraction of light energy leaving patch j that arrives at patch i
- · Takes account of both:
 - geometry (size, orientation & position)
 - visibility (are there any occluders?)



Calculating the Form Factor F_{ij}

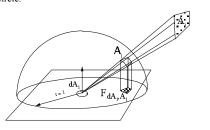
• F_{ii} = fraction of light energy leaving patch j that arrives at patch i



$$F_{ij} = \; \frac{1}{A_i} \; \int\limits_{A_i} \int\limits_{A_j} \frac{\cos \theta_i \cos \theta_j}{\pi \; r^2} \; \; V_{ij} \, dA_j \; dA_i \label{eq:Fij}$$

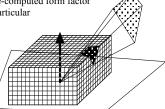
Form Factor Determination

The Nusselt analog: the form factor of a patch is equivalent to the fraction of the unit circle that is formed by taking the projection of the patch onto the hemisphere surface and projecting it down onto the circle.



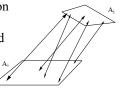
Hemicube Algorithm

- A hemicube is constructed around the center of each patch
- · Faces of the hemicube are divided into "pixels"
- Each patch is projected (rasterized) onto the faces of the hemicube
- Each pixel stores its pre-computed form factor. The form factor for a particular patch is just the sum of the pixels it overlaps
- Patch occlusions are handled similar to z-buffer rasterization



Form Factor from Ray Casting

- Cast *n* rays between the two patches
 - Compute visibility (what fraction of rays do not hit an occluder)
 - Integrate the point-to-point form factor
- Permits the computation of the patch-to-patch form factor, as opposed to point-to-patch



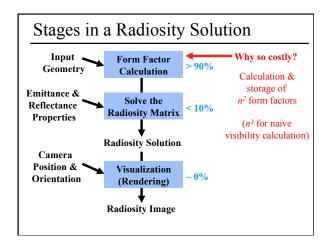
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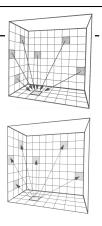
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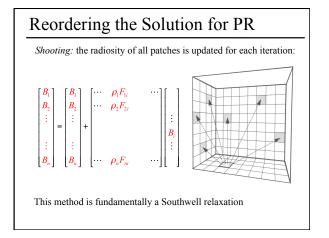
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 - Progressive Radiosity
 - Adaptive Subdivision
 - Discontinuity Meshing
 - Hierarchical Radiosity

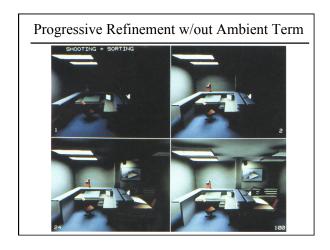


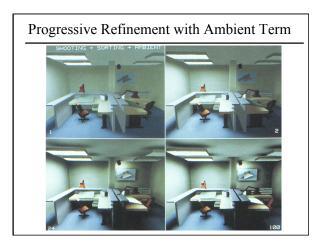
Progressive Refinement

- Goal: Provide frequent and timely updates to the user during computation
- Key Idea: Update the entire image at every iteration, rather than a single patch
- How? Instead of summing the light received by one patch, distribute the radiance of the patch with the most undistributed radiance.









Questions?



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Increasing the Accuracy of the Solution

What's wrong with this picture?



- Image quality is a function of patch size
- Compute a solution on a uniform initial mesh, then refine the mesh in areas that exceed some error tolerance:
 - shadow boundaries
 - other areas with a high radiosity gradient

Adaptive Subdivision of Patches











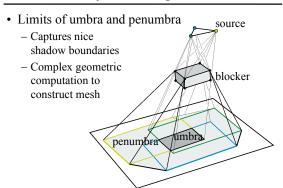


Coarse patch solution (145 patches)

Improved solution (1021 subpatches)

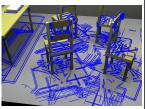
Adaptive subdivision

Discontinuity Meshing



Discontinuity Meshing



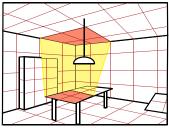


"Fast and Accurate Hierarchical Radiosity Using Global Visibility" Durand, Drettakis, & Puech 1999

Hierarchical Radiosity

- Group elements when the light exchange is not important
 - Breaks the quadratic complexity
 - Control non trivial, memory cost

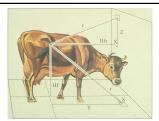




Practical Problems with Radiosity

- Meshing
 - memory
 - -robustness





Cow-cow form factor?

- Diffuse limitation
 - extension to specular takes too much memory

Questions?



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Readings for Tuesday (pick one):

- "The Rendering Equation", Kajiya, SIGGRAPH 1986 $L(x',\omega') = E(x',\omega') + \int_{P_x} (\omega,\omega') L(x,\omega) G(x,x') V(x,x') \; dA$
- "A Theoretical Framework for Physically Based Rendering", Lafortune and Willems, Computer Graphics Forum, 1994.





Figure B: An indirectly illuminated scene rendered using path tracing and bidirectional path tracing respectively. The