

Declarative Computation Model

Single assignment store (VRH 2.2)
Kernel language syntax (VRH 2.3)

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Sequential declarative computation model

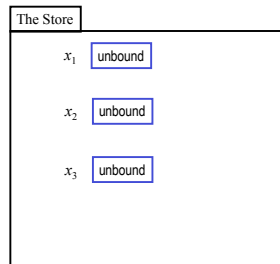
- The **single assignment store**
 - declarative (dataflow) variables
 - partial values (variables and values are also called *entities*)
- The **kernel language syntax**
- The **kernel language semantics**
 - The environment: maps textual variable names (variable identifiers) into entities in the store
 - Interpretation (execution) of the kernel language elements (statements) by the use of an abstract machine
 - Abstract machine consists of an execution stack of statements transforming the store

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Single assignment store

- A single assignment store is a store (set) of variables
- Initially the variables are unbound, i.e. do not have a defined value
- Example: a store with three variables, x_1 , x_2 , and x_3

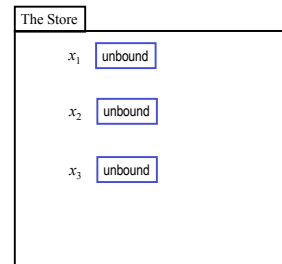


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Single assignment store (2)

- Variables in the store may be bound to values
- Example: assume we allow as values, integers and lists of integers

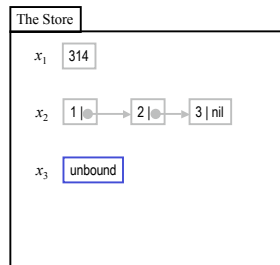


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Single assignment store (3)

- Variables in the store may be bound to values
- Assume we allow as values, integers and lists of integers
- Example: x_1 is bound to the integer 314, x_2 is bound to the list [1 2 3], and x_3 is still unbound

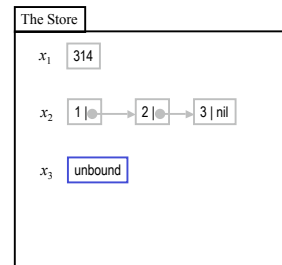


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Declarative (single-assignment) variables

- A declarative variable starts out as being unbound when created
- It can be bound to exactly one value
- Once bound it stays bound through the computation, and is indistinguishable from its value

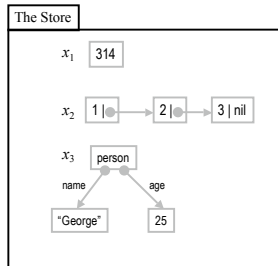


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Value store

- A store where all variables are bound to values is called a value store
- Example: a value store where x_1 is bound to integer 314, x_2 to the list [1 2 3], and x_3 to the record (labeled tree) person(name: "George" age: 25)
- Functional programming computes functions on values, needs only a value store
- This notion of value store is enough for functional programming (ML, Haskell, Scheme)



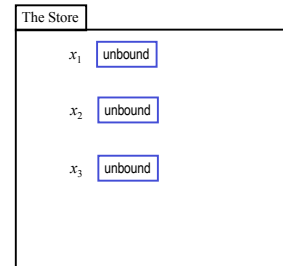
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Operations on the store (1) Single assignment

$\langle x \rangle = \langle v \rangle$

- $x_1 = 314$
- $x_2 = [1\ 2\ 3]$
- This assumes that $\langle x \rangle$ is unbound



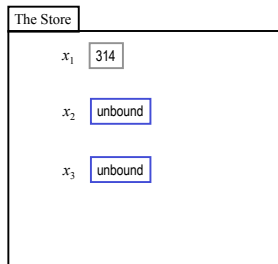
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Single-assignment

$\langle x \rangle = \langle \text{value} \rangle$

- $x_1 = 314$
- $x_2 = [1\ 2\ 3]$



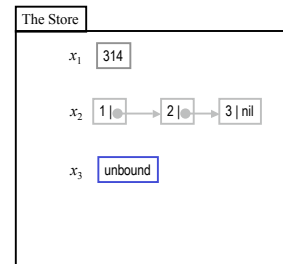
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Single-assignment (2)

$\langle x \rangle = \langle v \rangle$

- $x_1 = 314$
- $x_2 = [1\ 2\ 3]$
- The *single assignment operation* (" $=$ ") constructs the $\langle v \rangle$ in the store and binds the variable $\langle x \rangle$ to this value
- If the variable is already bound, the operation will test the compatibility of the two values
- If the test fails an error is raised

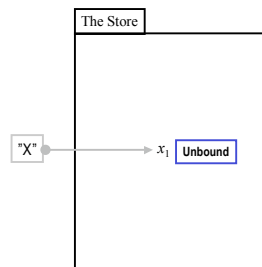


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Variable identifiers

- Variable identifiers refers to store entities (variables or values)
- The environment maps variable identifiers to variables
- declare X
- local X in ...
- "X" is a (variable) identifier
- This corresponds to 'environment' $\{ "X" \rightarrow x_1 \}$

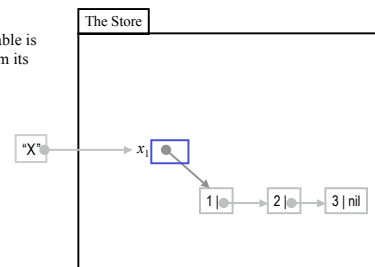


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Variable-value binding revisited (1)

- $X = [1\ 2\ 3]$
- Once bound the variable is indistinguishable from its value

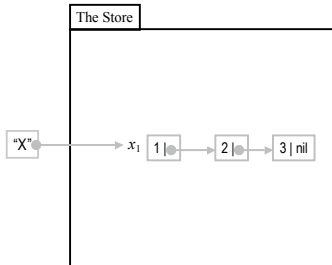


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Variable-value binding revisited (2)

- $X = [1\ 2\ 3]$
- Once bound the variable is indistinguishable from its value
- The operation of traversing variable cells to get the value is known as *dereferencing* and is invisible to the programmer

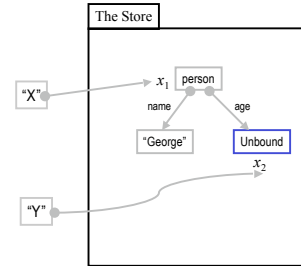


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Partial Values

- A partial value is a data structure that may contain unbound variables
- The store contains the partial value: `person(name: "George" age: x_2)`
- `declare Y X`
- `X = person(name: "George" age: Y)`
- The identifier "Y" refers to x_2



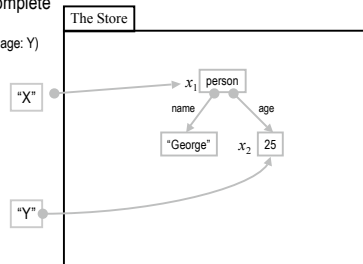
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Partial Values (2)

Partial Values may be complete

- `declare Y X`
- `X = person(name: "George" age: Y)`
- `Y = 25`



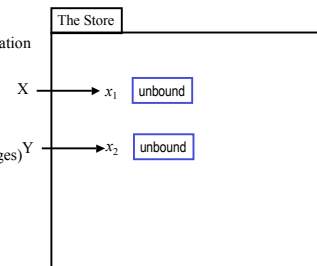
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Variable to variable binding

$\langle x_1 \rangle = \langle x_2 \rangle$

- It is to perform the bind operation between variables
- Example:
- `X = Y`
- `X = [1 2 3]`
- The operations equates (merges) Y the two variables



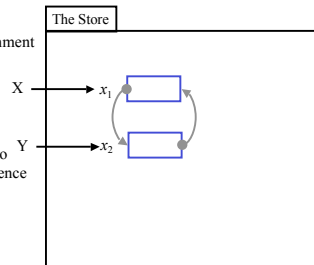
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Variable to variable binding (2)

$\langle x_1 \rangle = \langle x_2 \rangle$

- It is to perform a single assignment between variables
- Example:
- `X = Y`
- `X = [1 2 3]`
- The operations equates the two variables (forming an equivalence class)



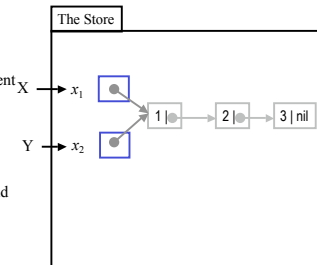
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Variable to variable binding (3)

$\langle x_1 \rangle = \langle x_2 \rangle$

- It is to perform a single assignment between variables
- Example:
- `X = Y`
- `X = [1 2 3]`
- All variables (X and Y) are bound to `[1 2 3]`



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Summary Variables and partial values

- **Declarative variable:**
 - is an entity that resides in a single-assignment store, that is initially unbound, and can be bound to exactly one (partial) value
 - it can be bound to several (partial) values as long as they are compatible with each other
- **Partial value:**
 - is a data-structure that may contain unbound variables
 - when one of the variables is bound, it is replaced by the (partial) value it is bound to
 - a complete value, or *value* for short is a data structure that does not contain any unbound variables

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Declaration and use of variables

- Assume that variables can be declared (introduced) and used separately
- What happens if we try to use a variable before it is bound?
 1. Use whatever value happens to be in the memory cell occupied by the variable (C, C++)
 2. The variable is initialized to a default value (Java), use the default
 3. An error is signaled (Prolog). Makes sense if there is a single activity running (pure sequential programs)
 4. An attempt to use the variable will wait (suspends) until another activity binds the variable (Oz/Mozart)

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Declaration and use of variables (2)

- An attempt to use the variable will wait (suspends) until another activity binds the variable (Oz/Mozart)
- Declarative (single assignment) variables that have this property are called *dataflow* variables
- It allows multiple operations to proceed concurrently giving the correct result
- Example: A = 23 running concurrently with B = A+1
- Functional (concurrent) languages do not allow the separation between declaration and binding (ML, Haskell, and Erlang)

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Kernel language syntax

The following defines the syntax of a statement, $\langle s \rangle$ denotes a statement

$\langle s \rangle ::=$	<code>skip</code>	<i>empty statement</i>
	<code>$\langle x \rangle = \langle y \rangle$</code>	<i>variable-variable binding</i>
	<code>$\langle x \rangle = \langle v \rangle$</code>	<i>variable-value binding</i>
	<code>$\langle s_1 \rangle \langle s_2 \rangle$</code>	<i>sequential composition</i>
	<code>local $\langle x \rangle$ in $\langle s_1 \rangle$ end</code>	<i>declaration</i>
	<code>if $\langle x \rangle$ then $\langle s_1 \rangle$ else $\langle s_2 \rangle$ end</code>	<i>conditional</i>
	<code>{ $\langle x \rangle \langle y_1 \rangle \dots \langle y_n \rangle$ }</code>	<i>procedural application</i>
	<code>case $\langle x \rangle$ of $\langle \text{pattern} \rangle$ then $\langle s_1 \rangle$ else $\langle s_2 \rangle$ end</code>	<i>pattern matching</i>
$\langle v \rangle ::=$	<code>...</code>	<i>value expression</i>
$\langle \text{pattern} \rangle ::=$	<code>...</code>	

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Variable identifiers

- $\langle x \rangle$, $\langle y \rangle$, $\langle z \rangle$ stand for variables
- In the concrete kernel language variables begin with uppercase letter followed by a (possibly empty) sequence of alphanumeric characters or underscore
- Any sequence of printable characters within back-quote
- Examples:
 - X
 - Y1
 - Hello_World
 - `hello this is a \$5 bill` (back-quote)

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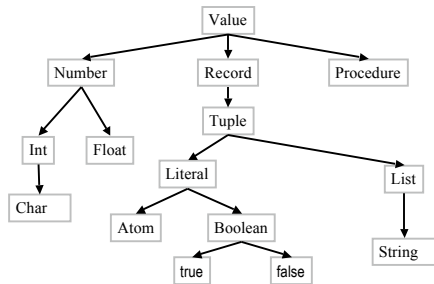
Values and types

- A *data type* is a set of values and a set of associated operations
- Example: Int is the the data type "Integer", i.e set of all integer values
- 1 is *of type* Int
- Int has a set of operations including +, -, *, div, etc
- The model comes with a set of basic types
- Programs can define other types, e.g., *abstract data types* ADT

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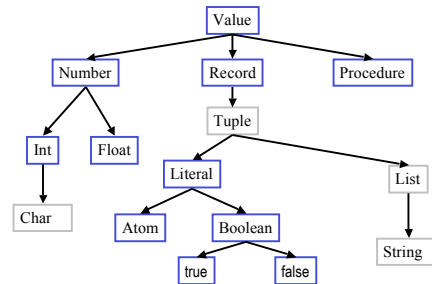
Data types



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Data types (2)



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Value expressions

```

<v> ::= <procedure> | <record> | <number>
<procedure> ::= proc {'$ <y1> ... <yn>} 's' end
<record>, <pattern> ::= <literal>
                    | <literal> [(feature1) : <x1> ... (featuren) : <xn>]
<literal> ::= <atom> | <bool>
<feature> ::= <int> | <atom> | <bool>
<bool> ::= true | false
<number> ::= <int> | <float>
  
```

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Numbers

- Integers
 - 314, 0
 - -10 (minus 10)
- Floats
 - 1.0, 3.4, 2.0e2, 2.0E2 (2×10^2)

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Atoms and booleans

- A sequence starting with a lower-case character followed by characters or digits, ...
 - person, peter
 - 'Self Haridi'
- Booleans:
 - true
 - false

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Records

- Compound representation (data-structures)
 - $\langle l \rangle (f_1) : \langle x_1 \rangle \dots (f_n) : \langle x_n \rangle$
 - $\langle l \rangle$ is a literal
- Examples
 - person(age:X1 name:X2)
 - person(1:X1 2:X2)
 - !(1:H 2:T)
 - nil
 - person

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Syntactic sugar (tuples)

- Tuples
 $\langle l \rangle \langle x_1 \rangle \dots \langle x_n \rangle$ (tuple)
- This is equivalent to the record
 $\langle l \rangle (1: \langle x_1 \rangle \dots n: \langle x_n \rangle)$
- Example:
`person('George' 25)`
- This is the record
`person(1:'George' 2:25)`

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Syntactic sugar (lists)

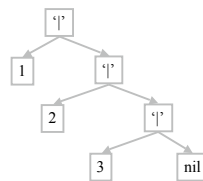
- Lists
 $\langle x_1 \rangle | \langle x_2 \rangle$ (a cons with the infix operator '|')
- This is equivalent to the tuple
 $\langle ' \rangle \langle x_1 \rangle \langle x_2 \rangle$
- Example:
`H | T`
- This is the tuple
 $\langle ' \rangle (H T)$

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Syntactic sugar (lists)

- Lists
 $\langle x_1 \rangle | \langle x_2 \rangle | \langle x_3 \rangle$
- '|' associates to the right
 $\langle x_1 \rangle | (\langle x_2 \rangle | \langle x_3 \rangle)$
- Example:
`1 | 2 | 3 | nil`
- Is
`1 | (2 | (3 | nil))`

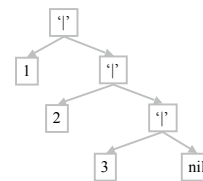


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Syntactic sugar (complete lists)

- Complete lists
- Example:
`[1 2 3]`
- Is
`1 | (2 | (3 | nil))`



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Strings

- A string is a list of character codes enclosed with double quotes
- Ex: `"E=mc^2"`
- Means the same as `[69 61 109 99 94 50]`

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Procedure declarations

- According to the kernel language
 $\langle x \rangle = \text{proc } \{ \$ \langle y_1 \rangle \dots \langle y_n \rangle \} \langle s \rangle \text{ end}$
is a legal statement
- It binds $\langle x \rangle$ to a procedure value
- This statement actually declares (introduces) a procedure
- Another syntactic variant which is more familiar is
 $\text{proc } \{ \langle x \rangle \langle y_1 \rangle \dots \langle y_n \rangle \} \langle s \rangle \text{ end}$
- This introduces (declares) the procedure $\langle x \rangle$

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Operations of basic types

- **Arithmetics**
 - Floating point numbers: +, -, *, and /
 - Integers: +, -, *, div (integer division, i.e. truncate fractional part), mod (the remainder after a division, e.g. 10 mod 3 = 1)
- **Record operations**
 - Arity, Label, and "."
 - X = person(name:"George" age:25)
 - {Arity X} = [age name]
 - {Label X} = person, X.age = 25
- **Comparisons**
 - Boolean comparisons, including ==, != (equality)
 - Numeric comparisons, =, <, >, >=, compares integers, floats, and atoms

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Value expressions

$\langle v \rangle ::= \langle \text{procedure} \rangle \mid \langle \text{record} \rangle \mid \langle \text{number} \rangle \mid \langle \text{basicExpr} \rangle$

$\langle \text{basicExpr} \rangle ::= \dots \mid \langle \text{numberExpr} \rangle \mid \dots$

$\langle \text{numberExpr} \rangle ::= \langle x \rangle_1 + \langle x \rangle_2 \mid \dots$

.....

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Syntactic sugar (multiple variables)

- Multiple variable introduction

```
local X Y in <statement> end
```

- is transformed to

```
local X in
  local Y in <statement> end
end
```

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Syntactic sugar (basic expressions)

- Basic expression nesting

```
if <basicExpr> then <statement>_1 else <statement>_2 end
```

- is transformed to

```
local T in
  T = <basicExpr>
  if T then <statement>_1 else <statement>_2 end
end
```

- where T is a fresh ('new') variable identifier

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Syntactic sugar (variables)

- Variable initialization

```
local X = <value> in <statement> end
```

- Is transformed to

```
local X in
  X = <value>
  <statement>
end
```

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Exercises

42. Using Oz, perform a few basic operations on numbers, records, and booleans (see Appendix B1-B3)
43. Explain the behavior of the `declare` statement in the interactive environment. Give an example of an interactive Oz session where "declare" and "declare ... in" produce different results. Explain why.
44. VRH Exercise 2.9.1
45. *Describe what an anonymous procedure is, and write one in Oz. When are anonymous procedures useful?

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