

Declarative Programming Techniques

Declarativeness, iterative computation (VRH 3.1-3.2)
Higher-order programming (VRH 3.6)
Abstract data types (VRH 3.7)

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Overview

- What is declarativeness?
 - Classification,
 - Advantages for large and small programs
- Control Abstractions
 - Iterative programs
- Higher-Order Programming
 - Procedural abstraction
 - Genericity
 - Instantiation
 - Embedding
- Abstract data types
 - Encapsulation
 - Security

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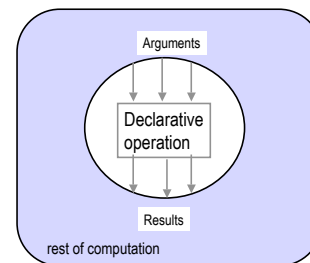
Declarative operations (1)

- An operation is *declarative* if whenever it is called with the same arguments, it returns the same results independent of any other computation state
- A declarative operation is:
 - *Independent* (depends only on its arguments, nothing else)
 - *Stateless* (no internal state is remembered between calls)
 - *Deterministic* (call with same operations always give same results)
- Declarative operations can be composed together to yield other declarative components
 - All basic operations of the declarative model are declarative and combining them always gives declarative components

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Declarative operations (2)



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Why declarative components (1)

- There are two reasons why they are important:
- (*Programming in the large*) A declarative component can be written, tested, and proved correct independent of other components and of its own past history.
 - The complexity (reasoning complexity) of a program composed of declarative components is the *sum* of the complexity of the components
 - In general the reasoning complexity of programs that are composed of nondeclarative components explodes because of the intimate interaction between components
- (*Programming in the small*) Programs written in the declarative model are much easier to reason about than programs written in more expressive models (e.g., an object-oriented model).
 - Simple algebraic and logical reasoning techniques can be used

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Why declarative components (2)

- Since declarative components are mathematical functions, algebraic reasoning is possible i.e. substituting equals for equals
- The declarative model of chapter 2 guarantees that all programs written are declarative
- Declarative components can be written in models that allow stateful data types, but there is no guarantee

Given
 $f(a) = a^2$
We can replace $f(a)$ in any other equation
 $b = 7f(a)^2$ becomes $b = 7a^4$

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Classification of declarative programming

```

graph LR
    DP[Declarative programming] --> D[Descriptive]
    DP --> P[Programmable]
    P --> O[Observational]
    P --> DEF[Definitional]
    DEF --> DM[Declarative model]
    DM --> FP[Functional programming]
    DM --> DLP[Deterministic logic programming]
    DM --> NLP[Nondeterministic logic programming]
  
```

- The word *declarative* means many things to many people. Let's try to eliminate the confusion.
- The basic intuition is to program by defining the *what* without explaining the *how*

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Descriptive language

```

(s) ::= skip
      | (x) = (y)
      | (x) = (record)
      | (s1) (s2)
      | local (x) in (s1) end
  
```

empty statement
variable-variable binding
variable-value binding
sequential composition
declaration

Other descriptive languages include HTML and XML

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Descriptive language

```

<person id = "530101-xxx">
  <name> Seif </name>
  <age> 48 </age>
</person>
  
```

Other descriptive languages include HTML and XML

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Kernel language

The following defines the syntax of a statement, (s) denotes a statement

```

(s) ::= skip
      | (x) = (y)
      | (x) = (v)
      | (s1) (s2)
      | local (x) in (s1) end
      | proc '{(x) (y1 ... (yn) }' (s1) end
      | if (x) then (s1) else (s2) end
      | '{(x) (y1 ... (yn) }'
      | case (x) of (pattern) then (s1) else (s2) end
  
```

empty statement
variable-variable binding
variable-value binding
sequential composition
declaration
procedure introduction
conditional
procedure application
pattern matching

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Why the KL is declarative

- All basic operations are declarative
- Given the components (sub-statements) are declarative,
 - sequential composition
 - local statement
 - procedure definition
 - procedure call
 - if statement
 - case statement

are all declarative (independent, stateless, deterministic).

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Iterative computation

- An iterative computation is a one whose execution stack is bounded by a constant, independent of the length of the computation
- Iterative computation starts with an initial state S_0 , and transforms the state in a number of steps until a final state S_{final} is reached:

$$S_0 \rightarrow S_1 \rightarrow \dots \rightarrow S_{final}$$

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The general scheme

```

fun {Iterate Si}
  if {IsDone Si} then Si
  else Si+1 in
    Si+1 = {Transform Si}
    {Iterate Si+1}
  end
end

```

- *IsDone* and *Transform* are problem dependent

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The computation model

- STACK : [R={Iterate S₀}]
- STACK : [S₁ = {Transform S₀}, R={Iterate S₁}]
- STACK : [R={Iterate S_i}]
- STACK : [S_{i+1} = {Transform S_i}, R={Iterate S_{i+1}}]
- STACK : [R={Iterate S_{i+1}}]

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Newton's method for the square root of a positive real number

- Given a real number x , start with a guess g , and improve this guess iteratively until it is accurate enough
- The improved guess g' is the average of g and x/g :

$$g' = (g + x/g) / 2$$

$$\epsilon = g - \sqrt{x}$$

$$\epsilon' = g' - \sqrt{x}$$

For g' to be a better guess than g : $\epsilon' < \epsilon$

$$\epsilon' = g' - \sqrt{x} = (g + x/g) / 2 - \sqrt{x} = \epsilon^2 / 2g$$

$$\text{i.e. } \epsilon^2 / 2g < \epsilon, \quad \epsilon / 2g < 1$$

$$\text{i.e. } \epsilon < 2g, \quad g - \sqrt{x} < 2g, \quad 0 < g + \sqrt{x}$$

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Newton's method for the square root of a positive real number

- Given a real number x , start with a guess g , and improve this guess iteratively until it is accurate enough
- The improved guess g' is the average of g and x/g :
- Accurate enough is defined as:

$$|x - g^2| / x < 0.00001$$

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SqrtIter

```

fun {SqrtIter Guess X}
  if {GoodEnough Guess X} then Guess
  else
    Guess1 = {Improve Guess X} in
      {SqrtIter Guess1 X}
    end
  end
end

```

- Compare to the general scheme:
 - The state is the pair *Guess* and *X*
 - *IsDone* is implemented by the procedure *GoodEnough*
 - *Transform* is implemented by the procedure *Improve*

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The program version 1

```

fun {Sqrt X}
  Guess = 1.0
  in {SqrtIter Guess X}
end
fun {SqrtIter Guess X}
  if {GoodEnough Guess X} then
    Guess
  else
    {SqrtIter {Improve Guess X} X}
  end
end
fun {Improve Guess X}
  (Guess + X/Guess)/2.0
end
fun {GoodEnough Guess X}
  (Abs X - Guess*Guess)/X < 0.00001
end

```

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Using local procedures

- The main procedure Sqrt uses the helper procedures SqrtIter, GoodEnough, Improve, and Abs
- SqrtIter is only needed inside Sqrt
- GoodEnough and Improve are only needed inside SqrtIter
- Abs (absolute value) is a general utility
- The general idea is that helper procedures should not be visible globally, but only locally

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Sqrt version 2

```

local
fun {SqrtIter Guess X}
  if {GoodEnough Guess X} then Guess
  else {SqrtIter {Improve Guess X} X} end
end
fun {Improve Guess X}
  (Guess + X/Guess)/2.0
end
fun {GoodEnough Guess X}
  {Abs X - Guess*Guess}/X < 0.000001
end
in
fun {Sqrt X}
  Guess = 1.0
  in {SqrtIter Guess X} end
end

```

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Sqrt version 3

- Define GoodEnough and Improve inside SqrtIter

```

local
fun {SqrtIter Guess X}
  fun {Improve}
    (Guess + X/Guess)/2.0
  end
  fun {GoodEnough}
    {Abs X - Guess*Guess}/X < 0.000001
  end
  in
  if {GoodEnough} then Guess
  else {SqrtIter {Improve} X} end
  end
in fun {Sqrt X}
  Guess = 1.0 in
  {SqrtIter Guess X}
end
end

```

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Sqrt version 3

- Define GoodEnough and Improve inside SqrtIter

```

local
fun {SqrtIter Guess X}
  fun {Improve}
    (Guess + X/Guess)/2.0
  end
  fun {GoodEnough}
    {Abs X - Guess*Guess}/X < 0.000001
  end
  in
  if {GoodEnough} then Guess
  else {SqrtIter {Improve} X} end
  end
in fun {Sqrt X}
  Guess = 1.0 in
  {SqrtIter Guess X}
end
end

```

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The program has a single drawback: on each iteration two procedure values are created, one for Improve and one for GoodEnough

Sqrt final version

```

fun {Sqrt X}
  fun {Improve Guess}
    (Guess + X/Guess)/2.0
  end
  fun {GoodEnough Guess}
    {Abs X - Guess*Guess}/X < 0.000001
  end
  fun {SqrtIter Guess}
    if {GoodEnough Guess} then Guess
    else {SqrtIter {Improve Guess}} end
  end
  Guess = 1.0
  in {SqrtIter Guess}
end

```

The final version is a compromise between abstraction and efficiency

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From a general scheme to a control abstraction (1)

```

fun {Iterate Si}
  if {IsDone Si} then Si
  else Si+1 in
    Si+1 = {Transform Si}
    {Iterate Si+1}
  end
end

```

- *IsDone* and *Transform* are problem dependent

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From a general scheme to a control abstraction (2)

```

fun {Iterate S IsDone Transform}
  if {IsDone S} then S
  else S1 in
    S1 = {Transform S}
    {Iterate S1 IsDone Transform}
  end
end
end

fun {Iterate Si}
  if {IsDone Si} then Si
  else Si+1 in
    Si+1 = {Transform Si}
    {Iterate Si+1}
  end
end
end
  
```

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Sqrt using the Iterate abstraction

```

fun {Sqrt X}
  fun {Improve Guess}
    (Guess + X/Guess)/2.0
  end
  fun {GoodEnough Guess}
    {Abs X - Guess*Guess}/X < 0.000001
  end
  Guess = 1.0
in
  {Iterate Guess GoodEnough Improve}
end
end
  
```

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Sqrt using the control abstraction

```

fun {Sqrt X}
  {Iterate
    1.0
    fun {$ G} {Abs X - G*G}/X < 0.000001 end
    fun {$ G} (G + X/G)/2.0 end
  }
end
  
```

Iterate could become a linguistic abstraction

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Higher-order programming

- Higher-order programming = the set of programming techniques that are possible with procedure values (lexically-scoped closures)
- Basic operations
 - Procedural abstraction: creating procedure values with lexical scoping
 - Genericity: procedure values as arguments
 - Instantiation: procedure values as return values
 - Embedding: procedure values in data structures
- Control abstractions
 - Integer and list loops, accumulator loops, folding a list (left and right)
- Data-driven techniques
 - List filtering, tree folding
- Explicit lazy evaluation, currying
- Higher-order programming is the foundation of component-based programming and object-oriented programming

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Procedural abstraction

- Procedural abstraction is the ability to convert any statement into a procedure value
 - A procedure value is usually called a **closure**, or more precisely, a **lexically-scoped closure**
 - A procedure value is a pair: it combines the procedure code with the environment where the procedure was created (the contextual environment)
- Basic scheme:
 - Consider any statement <S>
 - Convert it into a procedure value: P = proc {\$} <S> end
 - Executing {P} has **exactly the same effect** as executing <S>

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Procedural abstraction

```

fun {AndThen B1 B2}
  if B1 then B2 else false
  end
end
end
  
```

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Procedural abstraction

```
fun {AndThen B1 B2}
  if {B1} then {B2} else false
end
end
```

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A common limitation

- Most popular imperative languages (C, C++, Java) do **not** have procedure values
- They have only **half** of the pair: variables can reference procedure code, but there is no contextual environment
- This means that **control abstractions cannot be programmed** in these languages
 - They provide a predefined set of control abstractions (for, while loops, if statement)
- Generic operations are still possible
 - They can often get by with just the procedure code. The contextual environment is often empty.
- The limitation is due to **the way memory is managed** in these languages
 - Part of the store is put on the stack and deallocated when the stack is deallocated
 - This is supposed to make memory management simpler for the programmer on systems that have no garbage collection
 - It means that contextual environments cannot be created, since they would be full of dangling pointers

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Genericity

- Replace specific entities (zero 0 and addition +) by function arguments
- The same routine can do the sum, the product, the logical or, etc.

```
fun {SumList L}
  case L
  of nil then 0
  [] X|L2 then X+{SumList L2}
  end
end
```



```
fun {FoldR L F U}
  case L
  of nil then U
  [] X|L2 then {F X {FoldR L2 F U}}
  end
end
```

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Instantiation

```
fun {FoldFactory F U}
  fun {FoldR L F U}
    case L
    of nil then U
    [] X|L2 then {F X {FoldR L2 F U}}
    end
  end
in
  fun {$ L} {FoldR L F U} end
end
```

- Instantiation is when a procedure returns a procedure value as its result
- Calling {FoldFactory fun {\$ A B} A+B end U} returns a function that behaves identically to SumList, which is an «instance» of a folding function

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Embedding

- Embedding is when procedure values are put in data structures
- Embedding has many uses:
 - **Modules**: a module is a record that groups together a set of related operations
 - **Software components**: a software component is a generic function that takes a set of modules as its arguments and returns a new module. It can be seen as **specifying** a module in terms of the modules it needs.
 - **Delayed evaluation** (also called **explicit lazy evaluation**): build just a small part of a data structure, with functions at the extremities that can be called to build more. The consumer can control explicitly how much of the data structure is built.

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Control Abstractions

```
declare
proc {For I J P}
  if I >= J then skip
  else {P I} {For I+1 J P}
  end
end

{For 1 10 Browse}

for I in 1..10 do {Browse I} end
```

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Control Abstractions

```

proc {ForAll Xs P}
  case Xs
  of nil then skip
  [] X|Xr then
    {P X} {ForAll Xr P}
  end
end

{ForAll [a b c d]
  proc {$ I} {System.showInfo "the item is: " # I} end}

for I in [a b c d] do
  {System.showInfo "the item is: " # I}
end

```

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Control abstractions

```

fun {FoldL Xs F U}
  case Xs
  of nil then U
  [] X|Xr then {FoldL Xr F {F X U}}
  end
end

Assume a list [x1 x2 x3 ...]
S0 → S1 → S2
U → {F x1 U} → {F x2 {F x1 U}} → ... →

```

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Control abstractions

```

fun {FoldL Xs F U}
  case Xs
  of nil then U
  [] X|Xr then {FoldL Xr F {F X U}}
  end
end

```

What does this program do ?

```

{Browse {FoldL [1 2 3]
  fun {$ X Y} X|Y end nil}}

```

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List-based techniques

```

fun {Map Xs F}
  case Xs
  of nil then nil
  [] X|Xr then
    {F X}|{Map Xr F}
  end
end

```

```

fun {Filter Xs P}
  case Xs
  of nil then nil
  [] X|Xr andthen {P X} then
    X|{Filter Xr P}
  end
end

```

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Tree-based techniques

```

proc {DFS Tree}
  case Tree of tree(node:N sons:Sons ...) then
    {Browse N}
    for T in Sons do {DFS T} end
  end
end

Call {P T} at each node T

proc {VisitNodes Tree P}
  case Tree of tree(node:N sons:Sons ...) then
    {P tree}
    for T in Sons do {VisitNodes T P} end
  end
end

```

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Explicit lazy evaluation

- Supply-driven evaluation. (e.g. The list is completely calculated independent of whether the elements are needed or not.)
- Demand-driven execution. (e.g. The consumer of the list structure asks for new list elements when they are needed.)
- Technique: a programmed trigger.
- How to do it with higher-order programming? The consumer has a function that it calls when it needs a new list element. The function call returns a pair: the list element and a new function. The new function is the new trigger: calling it returns the next data item and another new function. And so forth.


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Currying

- Currying is a technique that can simplify programs that heavily use higher-order programming.
- The idea: function of n arguments \Rightarrow n nested functions of one argument.
- Advantage: The intermediate functions can be useful in themselves.

```
fun {Max X Y}
  if X>=Y then X else Y end
end
```



```
fun {Max X}
  fun {$ Y}
    if X>=Y then X else Y end
  end
end
```

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Abstract data types

- A datatype is a set of values and an associated set of operations
- A datatype is abstract only if it is completely described by its set of operations regardless of its implementation
- This means that it is possible to change the implementation of the datatype without changing its use
- The datatype is thus described by a set of procedures
- These operations are the only thing that a user of the abstraction can assume

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Example: A Stack

- Assume we want to define a new datatype \langle stack $T \rangle$ whose elements are of any type T
fun {NewStack}: \langle Stack $T \rangle$
fun {Push \langle Stack $T \rangle$ $T \rangle$: \langle Stack $T \rangle$
fun {Pop \langle Stack $T \rangle$ $T \rangle$: \langle Stack $T \rangle$
fun {IsEmpty \langle Stack $T \rangle$ }: \langle Bool \rangle
- These operations normally satisfy certain conditions:
{IsEmpty {NewStack}} = true
for any E and $S0, S1 = \{ \text{Push } S0 E \}$ and $S0 = \{ \text{Pop } S1 E \}$ hold
{Pop {NewStack} E } raises error

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Stack (implementation)

```
fun {NewStack} nil end
fun {Push S E} E|S end
fun {Pop S E} case S of X|S1 then E = X S1 end end
fun {IsEmpty S} S==nil end
```

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Stack (another implementation)

```
fun {NewStack} nil end
fun {Push S E} E|S end
fun {Pop S E} case S of X|S1 then E = X S1 end end
fun {IsEmpty S} S==nil end
```

```
fun {NewStack} emptyStack end
fun {Push S E} stack(E S) end
fun {Pop S E} case S of stack(X S1) then E = X S1 end end
fun {IsEmpty S} S==emptyStack end
```

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Dictionaries

- The datatype dictionary is a finite mapping from a set T to \langle value \rangle , where T is either \langle atom \rangle or \langle integer \rangle
- fun {NewDictionary}
– returns an empty mapping
- fun {Put D Key Value}
– returns a dictionary identical to D except Key is mapped to $Value$
- fun {CondGet D Key Default}
– returns the value corresponding to Key in D , otherwise returns $Default$
- fun {Domain D}
– returns a list of the keys in D

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Implementation

```
fun {Put Ds Key Value}
  case Ds
  of nil then [Key#Value]
  [] (K#V)|Dr andthen Key==K then
    (Key#Value) | Dr
  [] (K#V)|Dr andthen K>Key then
    (Key#Value)|(K#V)|Dr
  [] (K#V)|Dr andthen K<Key then
    (K#V){Put Dr Key Value}
  end
end
```

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Implementation

```
fun {CondGet Ds Key Default}
  case Ds
  of nil then Default
  [] (K#V)|Dr andthen Key==K then
    V
  [] (K#V)|Dr andthen K>Key then
    Default
  [] (K#V)|Dr andthen K<Key then
    {CondGet Dr Key Default}
  end
end
fun {Domain Ds}
  {Map Ds fun {$ K#_} K end}
end
```

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Further implementations

- Because of abstraction, we can replace the dictionary ADT implementation using a list, whose complexity is linear (i.e., $O(n)$), for a binary tree implementation with logarithmic operations (i.e., $O(\log(n))$).
- Data abstraction makes clients of the ADT unaware (other than through perceived efficiency) of the internal implementation of the data type.
- It is important that clients do not use anything about the internal representation of the data type (e.g., using `{Length Dictionary}` to get the size of the dictionary). Using only the interface (defined ADT operations) ensures that different implementations can be used in the future.

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Secure abstract data types: Stack is not secure

```
fun {NewStack} nil end
fun {Push S E} E|S end
fun {Pop S E}
  case S of X|S1 then E=X S1 end
end
fun {IsEmpty S} S==nil end
```

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Secure abstract data types II

- The representation of the stack is visible:

[a b c d]

- Anyone can use an incorrect representation, i.e., by passing other language entities to the stack operation, causing it to malfunction (like `a|b|X` or `Y=a|b|Y`)
- Anyone can write new operations on stacks, thus breaking the abstraction-representation barrier
- How can we guarantee that the representation is invisible?

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Secure abstract data types III

- The model can be extended. Here are two ways:
 - By adding a new basic type, an **unforgeable constant** called a **name**
 - By adding **encapsulated state**.
- A **name** is like an atom except that it **cannot be typed in on a keyboard or printed!**
 - The only way to have a name is if one is given it explicitly
- There are just two operations on names:
 - `N={NewName}` : returns a fresh name
 - `N1==N2` : returns true or false

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Secure abstract datatypes IV

- We want to « wrap » and « unwrap » values
- Let us use names to define a wrapper & unwrapper

```
proc {NewWrapper ?Wrap ?Unwrap}
  Key={NewName}
in
  fun {Wrap X}
    fun {$ K} if K==Key then X end end
  end
  fun {Unwrap C}
    {C Key}
  end
end
```

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Secure abstract data types: A secure stack

With the wrapper & unwrapper we can build a secure stack

```
local Wrap Unwrap in
  {NewWrapper Wrap Unwrap}
  fun {NewStack} {Wrap nil} end
  fun {Push S E} {Wrap E}{Unwrap S} end
  fun {Pop S E}
    case {Unwrap S} of X|S1 then E=X {Wrap S1} end
  end
  fun {IsEmpty S} {Unwrap S}==nil end
end
```

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Capabilities and security

- We say a computation is **secure** if it has well-defined and controllable properties, independent of the existence of other (possibly malicious) entities (either computations or humans) in the system
- What properties must a language have to be secure?
- One way to make a language secure is to base it on **capabilities**
 - A **capability** is an unforgeable language entity (« ticket ») that gives its owner the right to perform a particular action and only that action
 - In our model, all values are capabilities (records, numbers, procedures, names) since they give the right to perform operations on the values
 - Having a procedure gives the right to call that procedure. Procedures are very general capabilities, since what they do depends on their argument
 - Using names as procedure arguments allows very precise control of rights; for example, it allows us to build secure abstract data types
- Capabilities originated in operating systems research
 - A capability can give a process the right to create a file in some directory

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Secure abstract datatypes V

- We add two new concepts to the computation model
- {NewChunk Record}
 - returns a value similar to record but its arity cannot be inspected
 - recall {Arity foo(a:1 b:2)} is [a b]
- {NewName}
 - a function that returns a new symbolic (unforgeable, i.e. cannot be guessed) name
 - foo(a:1 b:2 {NewName}:3) makes impossible to access the third component, if you do not know the arity
- {NewChunk foo(a:1 b:2 {NewName}:3) }
 - Returns what ?

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Secure abstract datatypes VI

```
proc {NewWrapper ?Wrap ?Unwrap}
  Key={NewName}
in
  fun {Wrap X}
    {NewChunk foo(Key:X)}
  end
  fun {Unwrap C}
    C.Key
  end
end
```

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Secure abstract data types: Another secure stack

With the new wrapper & unwrapper we can build another secure stack (since we only use the interface to wrap and unwrap, the code is identical to the one using higher-order programming)

```
local Wrap Unwrap in
  {NewWrapper Wrap Unwrap}
  fun {NewStack} {Wrap nil} end
  fun {Push S E} {Wrap E}{Unwrap S} end
  fun {Pop S E}
    case {Unwrap S} of X|S1 then E=X {Wrap S1} end
  end
  fun {IsEmpty S} {Unwrap S}==nil end
end
```

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Exercises

76. Modify the Pascal function to use local functions for AddList, ShiftLeft, ShiftRight. Think about the abstraction and efficiency tradeoffs.
77. VRH Exercise 3.10.2 (page 230)
78. *VRH Exercise 3.10.3 (page 230)
79. *Develop a control abstraction for iterating over a list of elements.

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Exercises

80. Implement the function $\{\text{FilterAnd } Xs\ P\ Q\}$ that returns all elements of Xs in order for which P and Q return true. Hint: Use $\{\text{Filter } Xs\ P\}$.
81. Compute the maximum element from a nonempty list of numbers by folding.
82. *Suppose you have two sorted lists. Merging is a simple method to obtain an again sorted list containing the elements from both lists. Write a Merge function that is generic with respect to the order relation.
83. *VRH Exercise 3.10.17 (pg. 232). You do not need to implement it using gump, simply specify how you would add currying to Oz (syntax and semantics).

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