Declarative Computation Model

Single assignment store (VRH 2.2) Kernel language syntax (VRH 2.3)

> Carlos Varela RPI October 6, 2009

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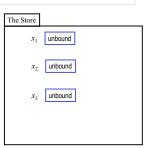
Sequential declarative computation model

- · The single assignment store
 - declarative (dataflow) variables
- partial values (variables and values are also called entities)
- The kernel language syntax
- · The kernel language semantics
 - The environment: maps textual variable names (variable identifiers) into entities in the store
 - Interpretation (execution) of the kernel language elements (statements) by the use of an abstract machine
 - Abstract machine consists of an execution stack of statements transforming the store

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Single assignment store

- A single assignment store is a store (set) of variables
- Initially the variables are unbound, i.e. do not have a defined value
- Example: a store with three variables, x_1 , x_2 , and x_3



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Single assignment store (2)

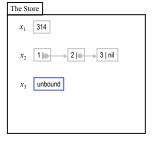
- Variables in the store may be bound to values
- Example: assume we allow as values, integers and lists of integers

The Store x_1 unbound x_2 unbound x_3 unbound

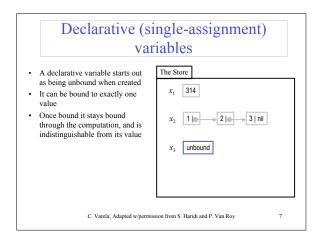
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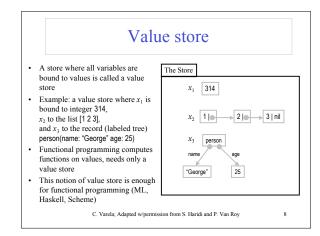
Single assignment store (3)

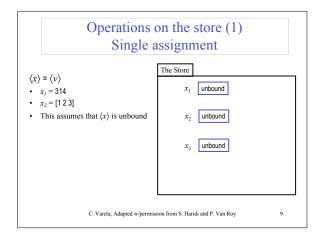
- Variables in the store may be bound to values
- Assume we allow as values, integers and lists of integers
- Example: x₁ is bound to the integer 314, x₂ is bound to the list [1 2 3], and x₃ is still unbound

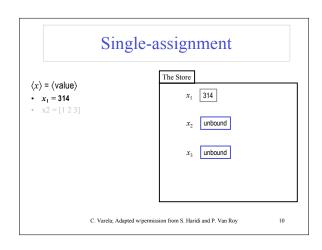


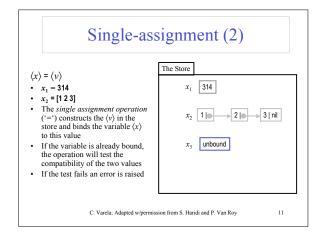
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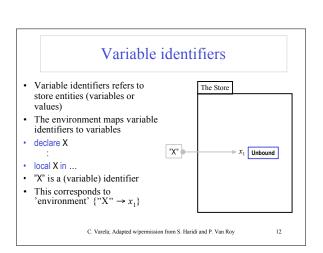


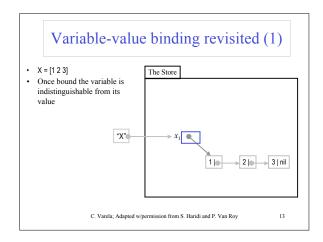


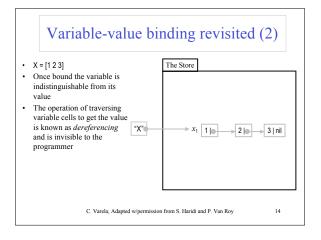


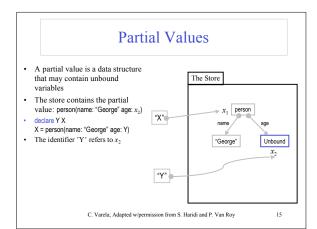


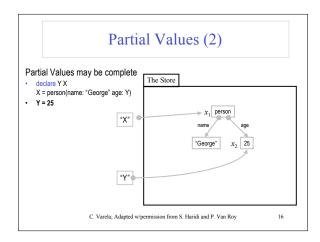


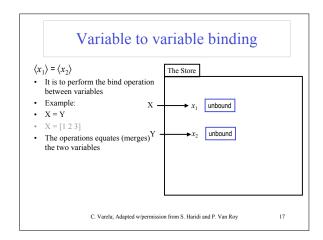


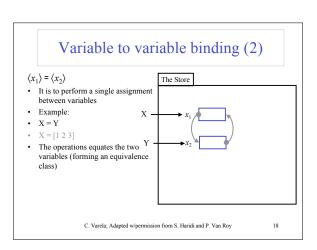


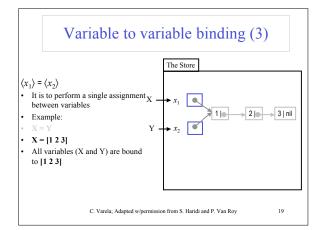












Summary Variables and partial values

- · Declarative variable:
 - is an entity that resides in a single-assignment store, that is initially unbound, and can be bound to exactly one (partial) value
 - it can be bound to several (partial) values as long as they are compatible with each other
- · Partial value:
 - is a data-structure that may contain unbound variables
 - when one of the variables is bound, it is replaced by the (partial) value it is bound to
 - a complete value, or value for short is a data structure that does not contain any unbound variables

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Declaration and use of variables

- Assume that variables can be declared (introduced) and used separately
- · What happens if we try to use a variable before it is bound?
- 1. Use whatever value happens to be in the memory cell occupied by the variable (C, C++)
- 2. The variable is initialized to a default value (Java), use the default
- 3. An error is signaled (Prolog). Makes sense if there is a single activity running (pure sequential programs)
- 4. An attempt to use the variable will wait (suspends) until another activity binds the variable (Oz/Mozart)

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Declaration and use of variables (2)

- An attempt to use the variable will wait (suspends) until another activity binds the variable (Oz/Mozart)
- Declarative (single assignment) variables that have this property are called *dataflow* variables
- It allows multiple operations to proceed concurrently giving the correct result
- Example: A = 23 running concurrently with B = A+1
- Functional (concurrent) languages do not allow the separation between declaration and binding (ML, Haskell, and Erlang)

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Kernel language syntax

The following defines the syntax of a statement, $\langle s \rangle$ denotes a statement

```
empty statement
               \langle x \rangle = \langle y \rangle
                                                                                                    variable-variable binding
                                                                                                    variable-value binding
                \langle x \rangle = \langle v \rangle
               \langle S_1 \rangle \langle S_2 \rangle
                                                                                                    sequential composition
               local \langle x \rangle in \langle s_1 \rangle end
               if \langle x \rangle then \langle s_1 \rangle else \langle s_2 \rangle end
                                                                                                      conditional
              '{' \langle x \rangle \langle y_1 \rangle \dots \langle y_n \rangle '}' case \langle x \rangle of \langle pattern \rangle then \langle s_1 \rangle else \langle s_2 \rangle end
                                                                                                     procedural application
                                                                                                    pattern matching
⟨v⟩ ::= ...
                                                                                                   value expression
(pattern)
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                                                                                                                                           23
```

Variable identifiers

- $\langle x \rangle$, $\langle y \rangle$, $\langle z \rangle$ stand for variables
- In the concrete kernel language variables begin with uppercase letter followed by a (possibly empty) sequence of alphanumeric characters or underscore
- · Any sequence of printable characters within back-quote
- · Examples:
 - X
 - Y1Hello World
 - 'hello this is a \$5 bill' (back-quote)

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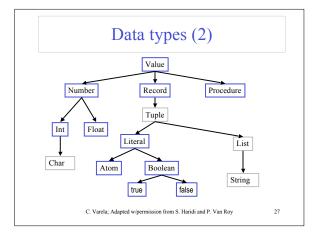
Values and types

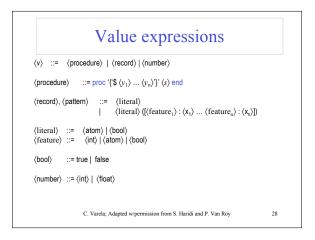
- · A data type is a set of values and a set of associated
- Example: Int is the the data type "Integer", i.e set of all integer values
- 1 is of type Int
- Int has a set of operations including +,-,*,div, etc
- The model comes with a set of basic types
- Programs can define other types, e.g., abstract data types

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Data types Value Number Record Procedure Tuple Float Literal List Char Atom Boolean String true C. Varela; Adapted w/permission from S. Haridi and P. Van Roy





Numbers

- · Integers
 - 314, 0
- ~10 (minus 10)
- · Floats
 - 1.0, 3.4, 2.0e2, 2.0E2 (2×10²)

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Atoms and booleans

- · A sequence starting with a lower-case character followed by characters or digits, ...
 - person, peter - 'Seif Haridi'
- · Booleans:

 - false

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Records

- · Compound representation (data-structures)
 - $\langle l \rangle (\langle f_1 \rangle : \langle x_1 \rangle \dots \langle f_n \rangle : \langle x_n \rangle)$ $\langle l \rangle \text{ is a literal}$
- Examples
 - person(age:X1 name:X2)
 - person(1:X1 2:X2)
 - '|'(1:H 2:T)
 - nil
 - person

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Syntactic sugar (tuples)

· Tuples

 $\langle l \rangle (\langle x_1 \rangle \dots \langle x_n \rangle)$ (tuple)

· This is equivalent to the record $\langle l \rangle (1: \langle x_1 \rangle \dots n: \langle x_n \rangle)$

• Example:

person('George' 25)

· This is the record

person(1:'George' 2:25)

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Syntactic sugar (lists)

- Lists
 - $\langle x_1 \rangle \mid \langle x_2 \rangle$

(a cons with the infix operator '|')

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- · This is equivalent to the tuple $|\langle\langle x_1\rangle\langle x_2\rangle\rangle$
- · Example:

HIT

• This is the tuple

'|'(H T)

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Syntactic sugar (lists)

- $\langle x_1 \rangle \mid \langle x_2 \rangle \mid \langle x_3 \rangle$
- '|' associates to the right $\langle x_1 \rangle \mid (\langle x_2 \rangle \mid \langle x_3 \rangle)$
- Example:

1 | 2 | 3 | nil

1 | (2 | (3 | nil))

nil

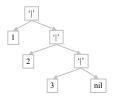
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Syntactic sugar (complete lists)

- · Complete lists
- Example:

[1 2 3]

1 | (2 | (3 | nil))



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Strings

- · A string is a list of character codes enclosed with double
- Ex: "E=mc^2"
- Means the same as [69 61 109 99 94 50]

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Procedure declarations

- According to the kernel language $\langle x \rangle = \operatorname{proc} \{\$ \langle y_1 \rangle \dots \langle y_n \rangle\} \langle s \rangle$ end is a legal statement
- It binds $\langle x \rangle$ to a procedure value
- This statement actually declares (introduces) a procedure
- Another syntactic variant which is more familiar is proc $\{\langle \mathbf{x} \rangle \langle \mathbf{y}_1 \rangle \dots \langle \mathbf{y}_n \}\} \langle \mathbf{s} \rangle$ end
- This introduces (declares) the procedure $\langle x \rangle$

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Operations of basic types

- · Arithmetics
 - Floating point numbers: +,-,*, and /
 - Integers: +,-,*,div (integer division, i.e. truncate fractional part), mod (the remainder after a division, e.g.10 mod 3 = 1)
- Record operations
 - Arity, Label, and "."
 - X = person(name:"George" age:25)
 - {Arity X} = [age name]
 - {Label X} = person, X.age = 25
- Comparisons
 - Boolean comparisons, including ==, \= (equality)
 - Numeric comparisons, =<, <, >, >=, compares integers, floats, and atoms

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Value expressions

```
\begin{tabular}{ll} $\langle v \rangle & ::= & \langle \text{procedure} \rangle & \langle \text{record} \rangle & \langle \text{number} \rangle & \langle \text{basicExpr} \rangle \\ $\langle \text{basicExpr} \rangle & := ... & \langle \text{numberExpr} \rangle & :... \\ & \langle \text{numberExpr} \rangle & ::= & \langle x \rangle_1 + \langle x \rangle_2 & .... \\ \end{tabular}
```

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Syntactic sugar (multiple variables)

· Multiple variable introduction

local X Y in (statement) end

 is transformed to local X in local Y in (statement) end end

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Syntactic sugar (basic expressions)

· Basic expression nesting

if \(basicExpr \) then \(statement \)_1 else \(statement \)_2 end

 is transformed to local T in T = (basicExpr) if T then (statement)₁ else (statement)₂ end end

• where T is a fresh ('new') variable identifier

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Syntactic sugar (variables)

· Variable initialization

local X = (value) in (statement) end

Is transformed to local X in
 X = (value)
 (statement)

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Exercises

- 42. Using Oz, perform a few basic operations on numbers, records, and booleans (see Appendix B1-B3)
- 43. Explain the behavior of the declare statement in the interactive environment. Give an example of an interactive Oz session where "declare" and "declare ... in" produce different results. Explain why.
- 44. VRH Exercise 2.9.1
- 45. Describe what an anonymous procedure is, and write one in Oz. When are anonymous procedures useful?

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