Declarative Computation Model

Kernel language semantics
Basic concepts, the abstract machine (VRH 2.4.1-2.4.2)

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Sequential declarative computation model

- · The single assignment store
 - declarative (dataflow) variables
 - partial values (variables and values are also called entities)
- The kernel language syntax
- · The kernel language semantics
 - The environment: maps textual variable names (variable identifiers) into entities in the store
 - Interpretation (execution) of the kernel language elements (statements) by the use of an abstract machine
 - Abstract machine consists of an execution stack of statements transforming the store

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Kernel language syntax

The following defines the syntax of a statement, (s) denotes a statement

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Examples

```
    local X in X = 1 end
```

```
    local X Y T Z in
        X = 5
        Y = 10
        T = (X>=Y)
        if T then Z = X else Z = Y end
        {Browse Z}
        end
```

local S T in
 S = proc {\$ X Y} Y = X*X end
 {S 5 T}
 {Browse T}

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Procedure abstraction

- Any statement can be abstracted to a procedure by selecting a number of the 'free' variable identifiers and enclosing the statement into a procedure with the identifiers as parameters
- if X >= Y then Z = X else Z = Y end
- Abstracting over all variables

 proc {Max X Y Z}

 if X >= Y then Z = X else Z = Y end
- Abstracting over X and Z
 proc {LowerBound X Z}
 if X >= Y then Z = X else Z = Y end
 end

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Computations (abstract machine)

- A computation defines how the execution state is transformed step by step from the initial state to the final state
- A single assignment store σ is a set of store variables, a variable may be unbound, bound to a partial value, or bound to a group of other variables
- An *environment E* is mapping from variable identifiers to variables or values in σ , e.g. $\{X \rightarrow x_1, Y \rightarrow x_2\}$
- · A semantic statement is a pair

 $(\langle s \rangle, E)$ where $\langle s \rangle$ is a statement

• ST is a stack of semantic statements

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Computations (abstract machine)

- A computation defines how the execution state is transformed step by step from the initial state to the final state
- The *execution state* is a pair (ST, σ)
- ST is a stack of semantic statements
- A *computation* is a sequence of execution states $(ST_0, \sigma_0) \rightarrow (ST_1, \sigma_1) \rightarrow (ST_2, \sigma_2) \rightarrow ...$

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Semantics

- To execute a program (i.e., a statement) $\langle s \rangle$ the initial execution state is
 - $(\,[\,(\langle s\rangle\,,\varnothing)\,]\,\,,\varnothing\,)$
- ST has a single semantic statement $(\langle s \rangle, \emptyset)$
- The environment E is empty, and the store σ is empty
- [...] denotes the stack
- At each step the first element of ST is popped and execution proceeds according to the form of the element
- The final execution state (if any) is a state in which ST is empty

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skip

- The semantic statement is (skip, E)
- · Continue to next execution step

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skip

- The semantic statement is (skip, E)
- · Continue to next execution step

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Sequential composition

- The semantic statement is $(\langle s_1 \rangle \langle s_2 \rangle, E)$
- Push $(\langle s_2 \rangle, E)$ and then push $(\langle s_I \rangle, E)$ on ST
- · Continue to next execution step

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Calculating with environments

- E is mapping from identifiers to entities (both store variables and values) in the store
- The notation E(⟨y⟩)
 retrieves the entity x associated with the identifier ⟨y⟩ from the
 store
- The notation $E + \{\langle \mathsf{y} \rangle_1 \to x_1, \langle \mathsf{y} \rangle_2 \to x_2, \dots, \langle \mathsf{y} \rangle_n \to x_n \}$
 - denotes a new environment E' constructed from E by adding the mappings
 - $\{\langle y \rangle_1 \to x_1, \langle y \rangle_2 \to x_2, \dots, \langle y \rangle_n \to x_n\}$
- $-E'(\langle z \rangle) \text{ is } x_k \text{ if } \langle z \rangle \text{ is equal to } \langle y \rangle_k \text{ , otherwise } E'(\langle z \rangle) \text{ is equal to } E(\langle z \rangle)$ The notation $E(\langle z \rangle)$ denotes the projection of E onto
- The notation $E|_{\{\langle y\rangle_1, \langle y\rangle_2, \dots, \langle y\rangle_n\}}$ denotes the projection of E onto the set $\{\langle y\rangle_1, \langle y\rangle_2, \dots, \langle y\rangle_n\}$, i.e., E restricted to the members of the set

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Calculating with environments (2)

- $E = \{X \rightarrow 1, Y \rightarrow [2\ 3], Z \rightarrow x_i\}$
- $E' = E + \{X \rightarrow 2\}$
- E'(X) = 2, E(X) = 1
- $E|_{\{X,Y\}}$ restricts E to the 'domain' $\{X,Y\}$, i.e., it is equal to $\{X \to 1, Y \to [2\ 3]\}$

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```
Calculating with environments (3)

• local X in X = 1 (E) local X in X = 2 (E') {Browse X} end (E) {Browse X} end
```

Lexical scoping

- · Free and bound identifier occurrences
- An identifier occurrence is bound with respect to a statement \(\s \) if it is in the scope of a declaration inside \(\s \)
- A variable identifier is declared either by a 'local' statement, as a parameter of a procedure, or implicitly declared by a case statement
- An identifier occurrence is *free* otherwise
- In a running program every identifier is bound (i.e., declared)

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Lexical scoping (2)

• proc {P X}
local Y in Y = 1 {Browse Y} end
X = Y
end

Free Occurrences

Bound Occurrences

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Lexical scoping (3) • local Arg1 Arg2 in Arg1 = 111*111 Arg2 = 999*999 Res = Arg1*Arg2 end Free Occurrences Bound Occurrences This is not a runnable program! C. Varela; Adapted w/permission from S. Haridi and P. Van Roy 17

```
Lexical scoping (4)

• local Res in
local Arg1 Arg2 in
Arg1 = 111*111
Arg2 = 999*999
Res = Arg1*Arg2
end
{Browse Res}
end

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```

Lexical scoping (5)

```
local P Q in

proc {P} {Q} end

proc {Q} {Browse hello} end

local Q in

proc {Q} {Browse hi} end

{P}

end

end
```

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Exercises

46. Translate the following function to the kernel language:

fun {AddList L1 L2}
case L1 of H1|T1 then
case L2 of H2|T2 then
H1+H2|{AddList T1 T2}
end
else nil end
end

47. Translate the following function call to the kernel language: {Browse {Max 5 7}}

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Exercises

- 48. Explain the difference between static scoping and dynamic scoping. Give an example program that produces different results with static and dynamic scoping.
- 49. Think of a reason why static scoping may be preferable to dynamic scoping. Think of a reason why dynamic scoping may be preferable to static scoping.

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