Review from Lectures 15

- Maps containing more complicated values.
  Example: index mapping words to the text line numbers on which they appear.

- Maps whose keys are class objects.
  Example: maintaining student records.

- Lists vs. Graphs vs. Trees
- Intro to Binary Trees, Binary Search Trees, & Balanced Trees

Today’s Lecture

- STL set container class (like STL map, but without the pairs!)
- Definition & basic operations
- Implementation of ds_set class using binary search trees
- Note: Lots more tree stuff in CSCI 2300 Introduction to Algorithms!

16.1 Standard Library Sets

- STL sets are ordered containers storing unique “keys”. An ordering relation on the keys, which defaults to operator<, is necessary. Because STL sets are ordered, they are technically not traditional mathematical sets.
- Sets are like maps except they have only keys, there are no associated values. Like maps, the keys are constant.
  This means you can’t change a key while it is in the set. You must remove it, change it, and then reinsert it.
- Access to items in sets is extremely fast! \(O(\log n)\), just like maps.
- Like other containers, sets have the usual constructors as well as the size member function.

16.2 Set Iterators

- Set iterators, similar to map iterators, are bidirectional: they allow you to step forward (++) and backward (--) through the set. Sets provide begin() and end() iterators to delimit the bounds of the set.
- Set iterators refer to const keys (as opposed to the pairs referred to by map iterators). For example, the following code outputs all strings in the set words:

  ```cpp
  for (set<string>::iterator p = words.begin(); p!= words.end(); ++p)
    cout << *p << endl;
  ```

16.3 Set insert, erase, and find

- There are two different versions of the insert member function. The first version inserts the entry into the set and returns a pair. The first component of the returned pair refers to the location in the set containing the entry. The second component is true if the entry wasn’t already in the set and therefore was inserted. It is false otherwise. The second version also inserts the key if it is not already there. The iterator pos is a “hint” as to where to put it. This makes the insert faster if the hint is good.

  ```cpp
  pair<iterator,bool> set<Key>::insert(const Key& entry);
  iterator set<Key>::insert(iterator pos, const Key& entry);
  ```

- There are three versions of erase. The first erase returns the number of entries removed (either 0 or 1). The second and third erase functions are just like the corresponding erase functions for maps. Note that the erase functions do not return iterators. This is different from the vector and list erase functions.

  ```cpp
  size_type set<Key>::erase(const Key& x);
  void set<Key>::erase(iterator p);
  void set<Key>::erase(iterator first, iterator last);
  ```

- The find function returns the end iterator if the key is not in the set:

  ```cpp
  const_iterator set<Key>::find(const Key& x) const;
  ```
16.4 The Tree Node Class

```cpp
template <class T> class TreeNode {
public:
    TreeNode() : left(NULL), right(NULL) {}
    TreeNode(const T& init) : value(init), left(NULL), right(NULL) {}
    T value;
    TreeNode* left;
    TreeNode* right;
};
```

Note: Sometimes a 3rd pointer — to the parent TreeNode — is added.

16.5 Exercises

1. Write a templated function to find the smallest value stored in a binary search tree whose root node is pointed to by \textit{p}.

2. Write a function to count the number of odd numbers stored in a binary tree (not necessarily a binary search tree) of integers. The function should accept a \texttt{TreeNode<int>} pointer as its sole argument and return an integer. Hint: think recursively!

16.6 \texttt{ds\_set} and Binary Search Tree Implementation

- A partial implementation of a set using a binary search tree is in the code attached. We will continue to study this implementation in the next lecture & lab.
- The increment and decrement operations for iterators have been omitted from this implementation. Next lecture we will discuss a couple strategies for adding these operations.
- We will use this as the basis both for understanding an initial selection of tree algorithms and for thinking about how standard library sets really work.

16.7 \texttt{ds\_set}: Class Overview

- There is an auxiliary \texttt{TreeNode} class, and a \texttt{tree\_iterator} class. The classes are templated.
- The only member variables of the \texttt{ds\_set} class are the root and the size (number of tree nodes).
- The iterator class is declared internally, and is effectively a wrapper on the TreeNode pointers.
  - Note that \texttt{operator*} returns a \texttt{const} reference because the keys can’t change.
  - As just discussed the increment and decrement operators are missing.
- The main public member functions just call a private (and often recursive) member function (passing the root node) that does all of the work.
- Because the class stores and manages dynamically allocated memory, a copy constructor, \texttt{operator=}, and destructor must be provided.

16.8 Exercises

1. Provide the implementation of the member function \texttt{ds\_set<T>::begin}. This is essentially the problem of finding the node in the tree that stores the smallest value.

2. Write a recursive version of the function \texttt{find}.
// Partial implementation of binary-tree based set class similar to std::set.
// The iterator increment & decrement operations have been omitted.
#ifndef ds_set_h_
#define ds_set_h_
#include <iostream>
#include <utility>

// -------------------------------------------------------------------
// TREE NODE CLASS
template <class T>
class TreeNode {
public:
    TreeNode() : left(NULL), right(NULL) {}
    TreeNode(const T& init) : value(init), left(NULL), right(NULL) {}
    T value;
    TreeNode* left;
    TreeNode* right;
};

template <class T> class ds_set;
// -------------------------------------------------------------------
// TREE NODE ITERATOR CLASS
template <class T>
class tree_iterator {
public:
    tree_iterator() : ptr_(NULL) {}
    tree_iterator(TreeNode<T>* p) : ptr_(p) {}
    tree_iterator(const tree_iterator& old) : ptr_(old.ptr_) {}
    ~tree_iterator() {}
    tree_iterator& operator=(const tree_iterator& old) { ptr_ = old.ptr_; return *this; }
    // operator* gives constant access to the value at the pointer
    const T& operator*() const { return ptr_->value; }
    // comparions operators are straightforward
    friend bool operator==(const tree_iterator& l, const tree_iterator& r) { return l.ptr_ == r.ptr_; }
    friend bool operator!=(const tree_iterator& l, const tree_iterator& r) { return l.ptr_ != r.ptr_; }
    // increment & decrement will be discussed in Lecture 17 and Lab 11
private:
    // representation
    TreeNode<T>* ptr_;
};
// -------------------------------------------------------------------
// DS SET CLASS
template <class T>
class ds_set {
public:
    ds_set() : root_(NULL), size_(0) {}
    ds_set(const ds_set<T>& old) : size_(old.size_) {
        root_ = this->copy_tree(old.root_);
    }
    ~ds_set() { this->destroy_tree(root_); root_ = NULL; }
    ds_set& operator=(const ds_set<T>& old) {
        if (&old != this) {
            this->destroy_tree(root_);
            root_ = this->copy_tree(old.root_);
            size_ = old.size_;}
        return *this;
    }
    typedef tree_iterator<T> iterator;

    int size() const { return size_; }
    bool operator==(const ds_set<T>& old) const { return (old.root_ == this->root_); }
}
// FIND, INSERT & ERASE
iterator find(const T& key_value) { return find(key_value, root_); }  
std::pair< iterator, bool > insert(T const& key_value) { return insert(key_value, root_); }  
int erase(T const& key_value) { return erase(key_value, root_); }

// OUTPUT & PRINTING
friend std::ostream& operator<< (std::ostream& ostr, const ds_set<T>& s) {
    s.print_in_order(ostr, s.root_);
    return ostr;
}

void print_as_sideways_tree(std::ostream& ostr, const ds_set<T>& s) const {
    print_as_sideways_tree(ostr, s.root_, 0);
}

// ITERATORS
iterator begin() const {
    // Implemented in Lecture 16
}

iterator end() const { return iterator(NULL); }

private:

// REPRESENTATION
TreeNode<T>* root_;  
int size_;  

// PRIVATE HELPER FUNCTIONS
TreeNode<T>* copy_tree(TreeNode<T>* old_root) { /* Implemented in Lab 10 */ }  
void destroy_tree(TreeNode<T>* p) { /* Implemented in Lecture 17 */ }

iterator find(const T& key_value, TreeNode<T>* p) {
    // Implemented in Lecture 16
}

std::pair<iterator,bool> insert(const T& key_value, TreeNode<T>*& p) { /* Discussed in Lecture 17 */ }

int erase(T const& key_value, TreeNode<T>* &p) { /* Implemented in Lecture 17 */ }

void print_in_order(std::ostream& ostr, const TreeNode<T>* p) const {
    // Discussed in Lecture 16
    if (p) {
        print_in_order(ostr, p->left);
        ostr << p->value << "\n";
        print_in_order(ostr, p->right);
    }
}

void print_as_sideways_tree(std::ostream& ostr, const TreeNode<T>* p, int depth) const {
    // Discussed in Lecture 17 */
};

#endif