1. Upside-Down Binary Search Tree [ / 36 ]

1.1 Binary Search Tree Diagram Warmup [ / 7 ]

Draw the tree that results when this sequence of 12 numbers is inserted (in this order) into a binary search tree using the algorithm covered in lecture and lab.

```
13 8 20 4 18 25 2 10 16 21 6 23
```

Which numbers are the leaves of this tree? *Hint: There are five.*

Upside-Down Binary Search Tree

Ben Bitdiddle has come up with another wacky tree scheme (with questionable usefulness). He proposes to represent a binary search tree not with a single pointer to the tree root, but instead with an STL list of the leaf nodes. And then it follows that each `Node` will store only a pointer to its parent.

```cpp
class Node {
    public:
        Node(int v) : value(v), parent(NULL) {} 
        int value;
        Node* parent;
    }
```

Ben is sure that because his new representation only has one pointer per `Node` this structure will be much more memory efficient than the typical binary tree. Here’s how he proposes to construct the tree you drew above:

```
std::list<Node*> leaves;
Insert(leaves,13); Insert(leaves,8); Insert(leaves,20); Insert(leaves,4);
Insert(leaves,18); Insert(leaves,25); Insert(leaves,2); Insert(leaves,10);
Insert(leaves,16); Insert(leaves,21); Insert(leaves,6); Insert(leaves,23);
assert (leaves.size() == 5);
```
Rather than jumping straight into the implementation of the `Insert` function, Alyssa P. Hacker suggests that Ben start by implementing the `BelongsInSubtree` function. This recursive function takes in two arguments: `node`, a pointer to a `Node` already in the upside down tree, and `value`, an element we would like to add. The function returns false if placing `value` within a subtree of `node` violates the binary search tree property of the whole tree and true otherwise. Note: Ben’s tree does not allow duplicate elements.

```cpp
bool BelongsInSubtree(Node* node, int value) {
    // sample solution: 8 line(s) of code
}
```

The implementation of `Insert` will call the `BelongsInSubtree` function on each `Node` in the tree. Note: This function will return true for at least one, but possibly many nodes in the tree! Of these possible choices, `Insert` will select the node that is furthest (in number of parent pointer links) from the root of the tree. For example, if we’d like to insert the value 15 into our example tree, there are four nodes that will return true for the `BelongsInSubtree` function above. What values are stored in those nodes? Which of these nodes will be selected by `Insert` as the immediate parent for ’15’?
Now, let’s write the DestroyTree function, which cleans up all of the dynamically allocated memory associated with Ben’s upside-down tree leaving a valid empty tree.

```cpp
void DestroyTree(std::list<Node*> &leaves) {

}  // sample solution: 14 line(s) of code
```

If the tree contains \( n \) elements, and is approximately balanced, what is the order notation of your implementation of destroy tree? Write 2-3 sentences justifying your answer.
2 Halloween History Maps [ / 34 ]

r Bob Williams pirate
r Chris Smith doctor
r Chris Smith doctor
r Bob Williams zombie
r Alice Jones zombie
r Chris Smith pirate
r Bob Williams pirate
r Chris Smith zombie
r Chris Smith elf
r Bob Williams doctor

The costume shop owner from Homework 7 has asked for help predicting what costumes their indecisive customers might choose in the future. Looking at the history of costume rentals they suspect there might be a pattern when a customer changes their mind about their Halloween costume.

For the example data on the left, we can see two instances where a customer switched from a pirate costume to a doctor costume, and only once did a customer switch from a pirate costume to a zombie costume. Here is the output we expect from the sample 'r' = rental and 'h' = print costume history commands:

<table>
<thead>
<tr>
<th>history for pirate</th>
</tr>
</thead>
<tbody>
<tr>
<td>next rental was doctor 1 time(s)</td>
</tr>
<tr>
<td>next rental was zombie 2 time(s)</td>
</tr>
<tr>
<td>no next rental history for elf</td>
</tr>
<tr>
<td>history for doctor</td>
</tr>
<tr>
<td>next rental was pirate 1 time(s)</td>
</tr>
</tbody>
</table>

The shop owner emphasizes the need for fast performance in this implementation, since the system will be handling the records for thousands of customers and costumes in many different cities.

2.1 Data Structure Sketch [ / 6 ]

Let’s store this data in two variables, one with the current customer information, and the second with the costume history. (You’ll specify the typedefs in the next part). Sketch the contents of these variables after the rental commands above. Follow the conventions from lecture for your diagrams.

PEOPLE_TYPE people;
HISTORY_TYPE history;
2.2 The typedefs

Next, fill in these `typedef` declarations.

```cpp
typedef PEOPLE_TYPE;

typedef HISTORY_TYPE;
```

2.3 Implementation of the Rental Command

Now, complete the implementation:

```cpp
int main() {
    PEOPLE_TYPE people;
    HISTORY_TYPE history;
    std::string first, last, costume;
    char c;
    while (std::cin >> c) {
        if (c == 'r') {
            std::cin >> first >> last >> costume;
        }
    }
}
```

*sample solution: 6 line(s) of code*

*NOTE: main function code continued on next page...*
2.4 Implementation of the History Command [ / 10 ]

```cpp
else {
    assert (c == 'h');
    std::cin >> costume;
}
```

Sample solution: 10 line(s) of code

2.5 Order Notation [ / 5 ]

If the shop has $p$ customers, $c$ costumes, and $r$ total rental events, what is the order notation for performing a single rental (the '$r$' command)? Write 1-2 sentences justification.

What is the order notation for performing a history query (the '$h$' command)? (justify your answer)
Complete the functions below without using any additional for or while expressions. Given an STL vector of words, find all pairs of those words that share at least one common letter. For example, if `words` contains: apple boat cat dog egg fig then `common(words)` should return:
(apple,boat) (apple,cat) (apple,egg) (boat,cat) (boat,dog) (dog,egg) (dog,fig) (egg,fig)

```cpp
typedef std::set<std::pair<std::string, std::string>> set_of_word_pairs;

bool common(const std::string &a, const std::string &b) {
    for (int i = 0; i < a.size(); i++)
        for (int j = 0; j < b.size(); j++)
            if (a[i] == b[j]) return true;
    return false;
}

void common(set_of_word_pairs &answer, const std::vector<std::string>& words, int a, int b) {
    // sample solution: 6 line(s) of code
}

void common(set_of_word_pairs &answer, const std::vector<std::string>& words, int a) {
    // sample solution: 4 line(s) of code
}

set_of_word_pairs common(const std::vector<std::string>& words) {
    // sample solution: 5 line(s) of code
}
4  Bitdiddle Post-Breadth Tree Traversal [ / 31 ]

4.1 Balanced Tree Example [ / 3 ]

Ben Bitdiddle really wants to get his name on a traversal ordering. Even without a real world application for its use, he has invented what he calls the post-breadth ordering. His primary demonstration example is an exactly balanced, binary search tree with the numbers 1-15.

Your first task is to make a neat diagram of this tree in the box on the right.

For this example, Ben decrees that the PrintPostBreadth function should output:

<table>
<thead>
<tr>
<th>LEVEL</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1</td>
<td>3</td>
<td>5</td>
<td>7</td>
</tr>
<tr>
<td></td>
<td>9</td>
<td>11</td>
<td>13</td>
<td>15</td>
</tr>
<tr>
<td>LEVEL</td>
<td>1</td>
<td>2</td>
<td>6</td>
<td>10</td>
</tr>
<tr>
<td></td>
<td>14</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>LEVEL</td>
<td>2</td>
<td>4</td>
<td>12</td>
<td></td>
</tr>
<tr>
<td>LEVEL</td>
<td>3</td>
<td>8</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

4.2 Un-Balanced Tree Example [ / 3 ]

Alyssa P. Hacker rolls her eyes at Ben but agrees to help him with the implementation. However, before tackling the implementation she wants to make sure that Ben’s idea is sound. She sketches the unbalanced tree shape on the left.

Your second task is to place the numbers 1-10 in this diagram so it is a proper binary search tree.

This unbalanced tree initially confuses Ben. But he thinks for a while and decides that for his new traversal ordering, level 0 is defined to be all of the leaves of the tree, level 1 is the parents of the leaves, level 2 is the grandparents, etc. So he decrees that for this second example, the output of the PrintPostBreadth function is:

<table>
<thead>
<tr>
<th>LEVEL</th>
<th>0</th>
<th>1</th>
<th>2</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>2</td>
<td>5</td>
<td>7</td>
</tr>
<tr>
<td></td>
<td>9</td>
<td></td>
<td></td>
</tr>
<tr>
<td>LEVEL</td>
<td>1</td>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td></td>
<td>8</td>
<td>10</td>
<td></td>
</tr>
<tr>
<td>LEVEL</td>
<td>2</td>
<td>1</td>
<td>6</td>
</tr>
</tbody>
</table>

Alyssa studies Ben’s sample output carefully and then asks Ben if the traversal ordering will ever contain repeated elements. Ben says no, each element in the structure should be output exactly once. Alyssa suggests that they add a boolean mark member variable to the Node class since it will be helpful for an efficient implementation. This flag will help ensure the traversal ordering does not contain duplicates.
Alyssa's Node class is on the right.

She further suggests starting with the implementation of a helper function named CollectLeaves. This is a void recursive function that takes in two arguments: ptr is a pointer to a Node (initially the root of the tree), and leaves is an STL list of pointers to Nodes (the list is initially empty) that will collect all of the leaves of the tree.

She also indicates that this function should initialize all of the mark variables. Only the leaf nodes should be marked true.

Complete the implementation below.

```cpp
class Node {
public:
    // CONSTRUCTOR
    Node(int v) : value(v), mark(false),
        left(NULL), right(NULL), parent(NULL) {}
    // REPRESENTATION
    int value;
    bool mark;
    Node* left;
    Node* right;
    Node* parent;
};

void CollectLeaves(Node* ptr, std::list<Node*> leaves) {
    // Implementation goes here...
}
```

Sample solution: 9 line(s) of code
Now finish the implementation of the `PrintPostBreadth` function:

```cpp
void PrintPostBreadth(Node* root) {
    std::list<Node*> current;
    CollectLeaves(root, current);
    int count = 0;
    while (current.size() > 0) {
        std::cout << "LEVEL " << count << " : ";
        ...
Louis B. Reasoner has taken a job at a genome sequencing startup working on algorithms to detect differences between the genomes of different species. He came up with the sketch of the data structure on the right and showed it to his manager and got approval to start implementation.

He’s defined two typedefs named `count_t` and `kmer_t` to improve the readability of his code. Here’s an example of how this data structure is constructed using the `Add` function:

```cpp
kmer_t kmers;
count_t totals;
Add(totals,kmers,"human","ACT"); Add(totals,kmers,"human","ACT");
Add(totals,kmers,"human","ACT"); Add(totals,kmers,"human","GAG");
Add(totals,kmers,"human","TAG"); Add(totals,kmers,"human","TAG");
Add(totals,kmers,"dog","ACT"); Add(totals,kmers,"dog","ACT");
Add(totals,kmers,"dog","GAG"); Add(totals,kmers,"dog","TAG");
Add(totals,kmers,"fruit fly","ACT"); Add(totals,kmers,"fruit fly","ACT");
Add(totals,kmers,"fruit fly","CAT"); Add(totals,kmers,"fruit fly","GAG");
```

Two of the key operations for this data structure are to query the number of matches of a given k-mer for a particular species and to find the most frequently occurring k-mer for a species. Here are several example usages of the `Query` and `MostCommon` functions:

```cpp
assert (Query(kmers,"human","ACT") == 3); assert (MostCommon(kmers,"human") == "TAG");
assert (Query(kmers,"human","CAT") == 0); assert (MostCommon(kmers,"fruit fly") == "ACT");
assert (Query(kmers,"human","TAG") == 4); assert (MostCommon(kmers,"cat") == "");
assert (Query(kmers,"cat","ACT") == 0);
assert (Query(kmers,"dog","GAG") == 1);
```

Finally, we can compute the difference between two species. The `k-mer fraction` is the percent of a species total k-mers that match the particular k-mer. The `k-mer difference` is the absolute value of the difference between the k-mer fractions for each of the species. And the overall difference between two species is the sum over all k-mers of the k-mer difference. Here is the math to calculate the difference between a human and a dog:

- **ACT**: \( \text{abs}(2/5 - 3/9) = 0.067 \)
- **CAT**: \( \text{abs}(1/5 - 2/9) = 0.022 \)
- **GAG**: \( \text{abs}(1/5 - 2/9) = 0.044 \)
- **TAG**: \( \text{abs}(2/5 - 3/9) = 0.067 \)

Here is code to call the `Difference` helper function:

```cpp
std::cout << "Difference between human & dog "
  << Difference(totals,kmers,"human","dog") << std::endl;
std::cout << "Difference between human & fruit fly "
  << Difference(totals,kmers,"human","fruit fly") << std::endl;
std::cout << "Difference between dog & fruit fly "
  << Difference(totals,kmers,"dog","fruit fly") << std::endl;
```

And the resulting output:

- Difference between human & dog 0.133
- Difference between human & fruit fly 0.889
- Difference between dog & fruit fly 0.800
5.1 The typedefs

First, fill in the `typedef` declarations for the two shorthand types used on the previous page.

```c
typedef count_t;
typedef kmer_t;
```

5.2 Add Implementation

Next, finish the implementation of the `Add` function.

```c
void Add( totals, kmers,
          species, kmer) {

  sample solution: \( \leq 4 \) line(s) of code
}
```

If the data structure contains \( s \) different species, and \( k \) unique k-mers, and each animal contains \( p \) total k-mers, what is the order notation for the running time of a single call to `Add`? Write 2-3 concise and well-written sentences justifying your answer.
5.3 Query Implementation [ / 6 ]

```cpp
int Query(kmers, species, kmer) {
    // sample solution: 7 line(s) of code
}
```

5.4 MostCommon Implementation [ / 7 ]

```cpp
MostCommon(kmers, species) {
    std::string answer = "";
    int count = -1;
    // sample solution: 8 line(s) of code
    return answer;
}
```
5.5 Difference Implementation

float Difference(totals, kmers, speciesA, speciesB) {
    // sample solution: 3 line(s) of code
    if ( ) {
        std::cerr << "ERROR! One or both species are unknown" << std::endl;
        return -1;
    }
    // sample solution: 8 line(s) of code
}

If the data structure contains \( s \) different species, and \( k \) unique k-mers, and each animal contains \( p \) total k-mers, what is the order notation for the running time of a single call to `Difference`? Write 2-3 concise and well-written sentences justifying your answer.
6 Prescribed Pre-Ordering

In this problem we will create an algorithm to construct a binary search tree from the desired pre-order traversal order. The driver function (below) takes in this sequence as a STL vector. If the contents of the vector is not a valid pre-order traversal order of a binary search tree, the function should return NULL.

```cpp
template <class T> class Node {
public:
    Node(T v) : value(v), left(NULL), right(NULL) {}  
    T value;
    Node* left;
    Node* right;
};

template <class T> void destroy(Node<T>* root) {
    if (root == NULL) return;
    destroy(root->left);
    destroy(root->right);
    delete root;
}

// "driver" function (starts the recursive function that does the actual work)
template <class T> Node<T>* MakePreOrderTree(const std::vector<T>& values) {
    if (values.size() == 0) return NULL;
    return MakePreOrderTree(values, 0, values.size()-1);
}

6.1 Test Cases

First, create 4 different test cases of input for this problem. Each input vector should contain the numbers 1-7. The first two should be valid pre-orderings for a binary search tree containing these 7 numbers. Draw the corresponding tree for these cases. The other two test case inputs should be invalid pre-orderings.

<table>
<thead>
<tr>
<th>valid</th>
<th>valid</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>invalid</th>
<th>invalid</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>
6.2 Finish the MakePreOrderTree Implementation

Note: If you discover the input sequence is an invalid pre-ordering for a binary search tree, make sure you do not leak any memory!

```cpp
template <class T>
Node<T>* MakePreOrderTree(const std::vector<T>& values, int start, int end) {
    assert (start <= end);
    // find the split between the left & right branches

    // make the new node
    Node<T>* answer = new Node<T>(values[start]);
    // recurse left and/or right as needed

    return answer;
}
```

sample solution: 9 line(s) of code

sample solution: 14 line(s) of code
Ben Bitdiddle was overwhelmed during the Data Structures lecture that covered the implementation details of erase for binary search trees. Separately handling the cases where the node to be erased had zero, one, or two non-NULL child pointers and then moving data around within the tree and/or disconnecting and reconnecting pointers seemed pointlessly complex (pun intended). Ben’s plan is to instead leave the overall tree structure unchanged, but mark a node as unoccupied when the node containing the value to be erased has one or more children.

Ben’s modified Node class is provided on the right.

7.1 Diagramming the Expected Output of erase

First, help Ben work through different test cases for the erase function. For each of the sample trees below, draw the tree after the call erase(root,10). The first one has been done for you.

If a node is unoccupied, we draw it as an empty box. Below each result diagram we note the counts of occupied nodes and the number of unoccupied nodes within the tree. (We’ll write the count function on the next page!) Note that an unoccupied node should always have at least one non-NULL child.

```
template <class T>
class Node {
public:
    Node(const T& v) :
        occupied(true), value(v),
        left(NULL), right(NULL) {} 
    bool occupied;
    T value;
    Node* left;
    Node* right;
};
```
7.2 Counting Occupied & Unoccupied Nodes

Now let’s write a recursive \texttt{count} function that takes a single argument, a pointer to the root of the tree, and returns an STL pair of integers. The first integer is the total number of \textit{occupied} nodes in the tree and the second integer is the total number of \textit{unoccupied} nodes in the tree. Refer to the diagrams on the previous page as examples.

\begin{verbatim}
// sample solution: 10 line(s) of code

Alyssa P. Hacker stops by to see if Ben needs any help with his programming. She notes that when we insert a value into a tree, sometimes we will be able to re-use an unoccupied node, and other times we will have to create a new node and add it to the structure. She suggests a few helper functions that will be helpful in implementing the \texttt{insert} function for his binary search tree with unoccupied nodes:

\begin{verbatim}
template <class T>
const T& largest_value(Node<T>* p) {
    assert (p != NULL);
    if (p->right == NULL) {
        if (p->occupied)
            return p->value;
        else
            return largest_value(p->left);
    }
    return largest_value(p->right);
}

const T& smallest_value(Node<T>* p) {
    assert (p != NULL);
    if (p->left == NULL) {
        if (p->occupied)
            return p->value;
        else
            return smallest_value(p->right);
    }
    return smallest_value(p->left);
}
\end{verbatim}

\end{verbatim}

\end{verbatim}

\begin{verbatim}
// sample solution: 10 line(s) of code

Alyssa P. Hacker stops by to see if Ben needs any help with his programming. She notes that when we insert a value into a tree, sometimes we will be able to re-use an unoccupied node, and other times we will have to create a new node and add it to the structure. She suggests a few helper functions that will be helpful in implementing the \texttt{insert} function for his binary search tree with unoccupied nodes:

\begin{verbatim}
template <class T>
const T& largest_value(Node<T>* p) {
    assert (p != NULL);
    if (p->right == NULL) {
        if (p->occupied)
            return p->value;
        else
            return largest_value(p->left);
    }
    return largest_value(p->right);
}

const T& smallest_value(Node<T>* p) {
    assert (p != NULL);
    if (p->left == NULL) {
        if (p->occupied)
            return p->value;
        else
            return smallest_value(p->right);
    }
    return smallest_value(p->left);
}
\end{verbatim}

\end{verbatim}
7.3 Implement erase for Trees with Unoccupied Nodes

Now implement the `erase` function for Ben’s binary search tree with unoccupied nodes. This function takes in two arguments, a pointer to the root node and the value to erase, and returns true if the value was successfully erased or false if the value was not found in the tree.

*sample solution: 28 line(s) of code*
Now implement the `insert` function for Ben’s binary search tree with unoccupied nodes. This function takes in two arguments, a pointer to the root node and the value to insert, and returns true if the value was successfully inserted or false if the value was not inserted because it was a duplicate of a value already in the tree. Use the provided `smallest_value` and `largest_value` functions in your implementation.

*sample solution: 25 line(s) of code*
Louis B. Reasoner has been hired to automate RPI's weekly classroom scheduling system. A big fan of the C++ STL map data structure, he decided that maps would be a great fit for this application. Here's a portion of the main function with an example of how his program works:

```cpp
room_reservations rr;
add_room(rr, "DCC", 308);
add_room(rr, "DCC", 318);
add_room(rr, "Lally", 102);
add_room(rr, "Lally", 104);

bool success = make_reservation(rr, "DCC", 308, "Monday", 18, 2, "DS Exam") &&
make_reservation(rr, "DCC", 318, "Monday", 18, 2, "DS Exam") &&
make_reservation(rr, "DCC", 308, "Tuesday", 10, 2, "DS Lecture") &&
make_reservation(rr, "Lally", 102, "Wednesday", 10, 10, "DS Lab") &&
make_reservation(rr, "Lally", 104, "Wednesday", 10, 10, "DS Lab") &&
make_reservation(rr, "DCC", 308, "Friday", 10, 2, "DS Lecture");
assert (success == true);
```

In the small example above, only 4 classrooms are schedulable. To make a reservation we specify the building and room number, the day of the week (the initial design only handles Monday-Friday), the start time (using military 24-hour time, where 18 = 6pm), the duration (in # of hours), and an STL string description of the event.

Here are a few key functions Louis wrote:

```cpp
bool operator< (const std::pair<std::string,int> &a, const std::pair<std::string,int> &b) {
    return (a.first < b.first || (a.first == b.first && a.second < b.second));
}

void add_room(room_reservations &rr, const std::string &building, int room) {
    week_schedule ws;
    std::vector<std::string> empty_day(24,""/");
    ws[std::string("Monday")]] = empty_day;
    ws[std::string("Tuesday")]] = empty_day;
    ws[std::string("Wednesday")]] = empty_day;
    ws[std::string("Thursday")]) = empty_day;
    ws[std::string("Friday")]] = empty_day;
    rr[std::make_pair(building,room)] = ws;
}
```

Unfortunately, due to hard disk crash, Louis has lost the details of the two typedefs and his implementation of the `make_reservation` function. Your task is to help him recreate the implementation.

He does have a few more test cases for you to examine. Given the current state of the reservation system, these attempted reservations will all fail:

```cpp
success = make_reservation(rr, "DCC", 308, "Monday", 19, 3, "American Sniper") ||
make_reservation(rr, "DCC", 308, "Monday", 22, 3, "American Sniper") ||
make_reservation(rr, "DCC", 308, "Saturday", 19, 3, "American Sniper");
assert (success == false);
```

With these explanatory messages printed to std::cerr:

```
ERROR! conflicts with prior event: DS Exam
ERROR! room DCC 307 does not exist
ERROR! invalid time range: 22-25
ERROR! invalid day: Saturday
```
8.1 The typedefs

First, fill in the typedef declarations for the two shorthand types used on the previous page.

```cpp
typedef week_schedule;

typedef room_reservations;
```

8.2 Diagram of the data stored in room_reservations rr

Now, following the conventions from lecture for diagramming map data structures, draw the specific data stored in the rr variable after executing the instructions on the previous page. Yes, this is actually quite a big diagram, so don’t attempt to draw everything, but be neat and draw enough detail to demonstrate that you understand how each component of the data structure is organized and fits together.
Next, implement the `make_reservation` function. Closely follow the samples shown on the first page of this problem to match the arguments, return type, and error checking.
Now let’s analyze the running time of the `make_reservation` function you just wrote. If RPI has \( b \) buildings, and each building has on average \( c \) classrooms, and we are storing schedule information for \( d \) days (in the sample code \( d = 5 \) days of the week), and the resolution of the schedule contains \( t \) time slots (in the sample code \( t = 24 \) 1-hour time blocks), with a total of \( e \) different events, each lasting an average of \( s \) timeslots (data structures lecture lasts 2 1-hour time blocks), what is the order notation for the running time of this function? Write 2-3 concise and complete sentences explaining your answer.

Using the same variables, write a simple formula for the approximate upper bound on the memory required to store this data structure. Assume each int is 4 bytes and each string has at most 32 characters = 32 bytes per string. Omit the overhead for storing the underlying tree structure of nodes & pointers. Do not simplify the answer as we normally would for order notation analysis. Write 1-2 concise and complete sentences explaining your answer.

Finally, using the same variables, what would be the order notation for the running time of a function (we didn’t ask you to write this function!) to find all currently available rooms for a specific day and time range? Write 1-2 concise and complete sentences explaining your answer.
In this problem you will write a recursive function named `outfits` that takes as input two arguments: `items` and `colors`. `items` is an STL list of STL strings representing different types of clothing. `colors` is an STL list of STL sets of STL strings representing the different colors of each item of clothing. Your function should return an STL vector of STL strings describing each unique outfit (in any order) that can be created from these items of clothing.

Here is a small example:

```cpp
items = { "hat", "shirt", "pants" }
colors = { { "red" },
           { "red", "green", "white" },
           { "blue", "black" } }
```

```
red hat & red shirt & blue pants
red hat & green shirt & blue pants
red hat & white shirt & blue pants
red hat & red shirt & black pants
red hat & green shirt & black pants
red hat & white shirt & black pants
red hat & white shirt & black pants
```

sample solution: 22 line(s) of code