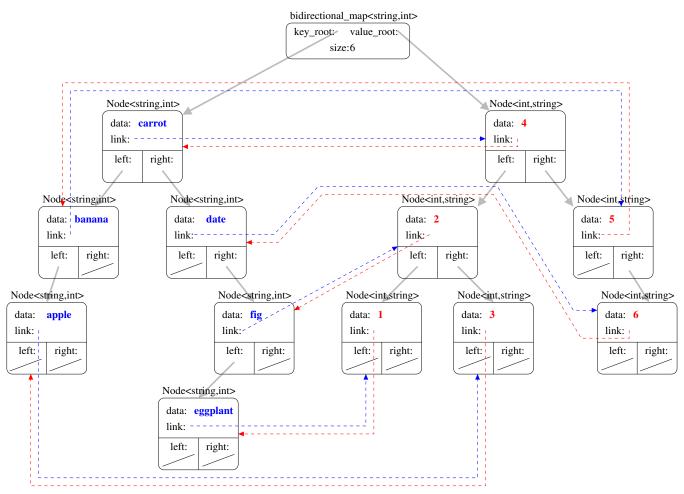
CSCI-1200 Data Structures — Fall 2025 Homework 8 — Bidirectional Map

In this assignment you will build a custom data structure named bidirectional_map. A bidirectional_map is similar to an STL map, in that it stores the association between key and value data. Like a map, inserting and erasing an association between a key and a value is completed in $O(\log n)$, where n is the number of association pairs in the map. Also, like a map, lookup by key is $O(\log n)$, but additionally, with a bidirectional map, lookup by value is also $O(\log n)$!

The typical implementation of an STL map stores STL pairs of the key and value in a single binary search tree, ordered by the keys. Our bidirectional_map will instead be stored in two distinct binary search trees, one storing the keys and one storing the values. The associations are stored as bidirectional *links* between the nodes of the two trees.

The diagram below illustrates the core structure of the bidirectional_map data structure:



Note that the bidirectional_map is templated over two types, the *key type* and the *value type*. In this example, the key type is STL string and the value type is int. We are currently storing 6 associations in this structure. Note that in this initial example, the associations are "one-to-one". This means that there are no repeated or duplicate keys or values.

Like an STL map it is not possible to edit the key of an association, because that edit may disrupt the overall binary search ordering property of the tree. Because the values of our bidirectional_map are also stored in their own binary search tree, we must also prohibit editing of the values in a bidirectional_map. If the key or the value of an association needs to be changed, that data must be removed from the tree and re-inserted.

Implementation

Your task for this homework is to implement the structure diagrammed on the previous page. We recommend that you begin your implementation by following the structure of the ds_set class we studied and worked with in lecture and lab. You will need to make a number of significant changes to the code, but the overall design composed of 3 classes — a node class, an iterator class, and "manager" class (bidirectional_map) — remains the same. Note that each class is now templated over two types rather than just one. You may choose to either nest the node & iterator class inside the manager class or to keep them separate and use the friend keyword as necessary.

The provided code in main.cpp illustrates the basic functionality of the bidirectional_map class including the bidirectional_map functions: size, insert, erase, find, operator[], key_begin, key_end, value_begin, and value_end. Study these examples carefully to deduce the expected argument and return types of the functions. The bidirectional_map has iterators over both the keys and values, which can be incremented and decremented like regular STL iterators. Also, each iterator's follow_link function can be used to obtain an iterator pointing to the associated data in the other half of the structure. You will also write a print function to help your implementation and debugging.

As this is a class with dynamically allocated memory, you will also need to implement the default constructor, copy constructor, assignment operator, and destructor. The provided code in main.cpp does not thoroughly test these functions, so you must write your own test cases. The homework server will compile and run your bidirectional_map.h file with the instructor's solution to test your implementation of these functions.

Additions/Modifications to the Core Data Structure Diagram

The Node objects illustrated in the diagram do not include parent pointers. In order to implement the forward and backward iterators you will need to add these pointers. Alternatively, you can implement your bidirectional_map iterators using a vector of Node pointers, as discussed in lecture.

Also, for extra credit, you can extend the structure to allow duplicate keys and/or duplicate values. To do this, you will have *many-to-one*, *one-to-many*, and *many-to-many* key/value associations. To add this feature, each node in the structure will store an STL vector of *links* to Node pointers in the other tree rather than just a single Node pointer. Examples of the non-*one-to-one* interface are included in the provided code.

Performance & Algorithm Analysis

For this assignment we will assume that the data stored in the structure is added and removed in a mostly random fashion and that the binary tree remains sufficiently balanced so that we may claim that the maximum height of the tree structures is not significantly greater than $\log n$, where n is the number of associations stored in the structure. In lecture, we will talk about algorithms for automatically rebalancing trees (but you do not need to implement this for the homework). In your README.txt file include the Big O Notation for each of the functions described above. If you complete the implementation of non-one-to-one associations for extra credit, you will also use k = 1 the maximum number of links in a single Node in your answers.

Additional Testing & Homework Submission

We encourage you to work through the test cases in the provided main.cpp step-by-step, uncommenting and debugging one test at a time. It is your responsibility to add additional test cases, including examples where the template class types are something other than string and int. Note: Your print function is only required to work for simple types (e.g., int, double, char, and short strings). Also, your print function is to help you debug, and does not need to exactly match the sample output. The homework submission server is configured to run your code with Dr. Memory to search for memory problems. Your program must be memory error free and memory leak free to receive full credit. You must do this assignment on your own, as described in the "Collaboration Policy & Academic Integrity" document. Be sure to list the names of anyone you talked to about the problem or debugging and all references you consulted in preparing your solution.