In this assignment you will manipulate a linked list of nodes that store playing cards of 4 different suits: clubs ♣, diamonds ♦, hearts ♥, and spades ♠; and 13 different face values: ace, 2-10, jack, queen, and king. In physical card games the deck of cards is commonly randomized by first cutting the deck roughly in half, and then shuffling the two piles into a single stack by interleaving or alternating a card or cards from one pile with each card or cards from the other pile. This cut & shuffle process is repeated several times. Slight imperfections in splitting the deck in half and variation in the number of cards selected as the piles are interleaved add sufficient variation into the process to achieve randomness in the resulting deck that allows games of chance to be played using the deck of cards without bias to one or more players. Once the deck is sufficiently shuffled, the cards are distributed to the other players by dealing the cards from the top of the stack to each player, one at a time, sequentially, until the required number of cards have been distributed.

Your task for this assignment is to perform idealized versions of these core card deck operations on a linked list structure representing the ordered deck of cards.

Provided Framework

We provide the testing framework of code for this assignment and a few small but important classes. The PlayingCard class represents a single card (suit & face value) and includes helper functions to print and sort these objects using a common high to low ordering grouped by suit that is helpful for many card games. The Node class holds a single card and stores pointers/links to other cards in the deck. The linked structure actually maintains two different doubly-linked traversal orders. The primary traversal is the physical ordering of the cards in the deck and the order they are received by each player when the cards are dealt. In some card games the order that the cards are received is part of game play. A secondary ordering, the sorted order, is also a doubly-linked structure stored within the same set of Nodes. This second ordering is initially disconnected (everything set to NULL), but when the SortHand function is called, the blue and red links below are constructed. This additional ordering represents how a card player might re-organize his/her cards, first by suit, alternating red/black suits, and then by face value from ace (high) down to 2. This data structure allows us to store and traverse both orderings. Here is a diagram showing the relationship between Nodes and PlayingCards:

First carefully study the provided code files. main.cpp contains the testing infrastructure. You are not to edit this file except to uncomment the test cases as you progress through the assignment and to add your own test cases in the specified function. As you read through the provided helper functions and the different test cases, and study the provided sample output, you should get a feel for the expectations of the operations on this data. You will write the 10 missing functions from these examples. (Part of your task for this homework is to deduce the exact function prototypes.)
Missing Functionality

We will not implement a class structure to manage the functionality of this homework. All of the code you will write will exist as standalone functions that pass data to and from other functions.

Several of the functions you write: DeckSize, PrintDeckSorted, SamePrimaryOrder, and ReversePrimaryOrder, are helper functions that need read-only access to the linked list structure. The latter two functions are used in inspecting the output of the perfect shuffle described below.

Two of the functions, CopyDeck and DeleteAll, ask you to allocate and deallocale node objects associated with those variables. Throughout the examples you should observe where Node objects are allocated (CreateDeck and CopyDeck) and where they are deleted (DeleteAll). To earn full credit on this homework, your code must also pass the memory error and memory leak checks of Valgrind/Dr. Memory.

The remaining functions carry out the operations necessary to model physical card shuffling, dealing, and card sorting. The first function CutDeck splits a single deck into similar sized sub-decks (the top and bottom of the list):

```
dock:  A♣ 2♣ 3♣ 4♣ 5♣ 6♣ 7♣ 8♣
top:   A♣ 2♣ 3♣ 4♣
bottom: 5♠ 6♠ 7♠ 8♠
```

The Shuffle function then takes those two smaller pieces and interleaves the cards one or a few cards at a time to form a single deck again, but with a different order than the original. For the main homework you will implement a perfect CutDeck and perfect one-by-one Shuffle function. These shuffle results are called a perfect out-shuffle and perfect in-shuffle depending on whether the top deck or the bottom deck contributes the first card to the resulting deck.

```
out shuffle:  A♠ 5♣ 2♣ 6♣ 3♣ 7♣ 4♣ 8♣
in shuffle:   5♥ A♦ 6♥ 2♥ 7♥ 3♥ 8♥ 4♥
```

If we repeatedly perform perfect shuffles, we will restore the data to the original order. The number of shuffles required depends on the number of cards in the original deck, and also whether we are performing out- or in- shuffles. See also: http://en.wikipedia.org/wiki/Faro_shuffle The SamePrimaryOrder and ReversePrimaryOrder function (which you will write) allow the testing code to verify this process.

The next step is to Deal all or some of the deck to a specified number of players. We specify the number of cards each person should receive. The cards are passed to the players one-at-a-time in sequence.

```
dock:  A♠ 2♠ 3♠ 4♠ 5♠ 6♠ 7♠ 8♠ 9♠ T♦ J♣ Q♠ K♣ A♣ 2♦ 3♦ 4♦ 5♦ 6♦ 7♦ 8♦ 9♦
T♥ J♥ Q♥ K♥ A♥ 6♥ 2♥ 7♥ 3♥ 8♥ 4♥
wesit:  A♠ 5♠ 9♥ K♥ 4♥ 8♥ Q♥ 3♥ 7♥ J♥ 2♣ 6♣ T♣
north:  2♣ 6♣ T♣ A♦ 5♥ 9♥ K♦ 4♥ 8♥ Q♥ 3♠ 7♠ J♣
east:  3♠ 7♣ J♣ 2♥ 6♥ T♥ A♥ 5♥ 9♥ K♣ 4♣ 8♣ Q♣
south:  4♣ 8♣ Q♣ 3♥ 7♥ J♥ 2♥ 6♥ T♥ A♠ 5♠ 9♠ K♠
```

Once a player has received their hand, the SortHand function can be called to initialize the secondary sorted ordering shown on the earlier diagram.

```
west (sorted):  T♠ 6♠ 2♠ Q♥ 8♥ 4♥ A♠ K♣ 9♥ 5♥ J♥ 7♥ 3♥
north (sorted): J♣ 7♥ 3♥ A♣ K♦ 9♥ 5♥ T♠ 6♠ 2♠ Q♥ 8♥ 4♥
east (sorted):  Q♣ 8♠ 4♠ T♥ 6♥ 2♥ J♠ 7♠ 3♠ A♥ K♥ 9♥ 5♥
south (sorted): A♣ K♥ 9♥ 5♥ J♥ 7♥ 3♥ Q♣ 8♠ 4♠ T♥ 6♥ 2♥
```

The provided PlayingCard class includes the logic for comparing two cards to determine which one comes first in the sorted order.
Extra Credit

For extra credit, you can explore variants on the shuffling model to mimic the randomness that naturally occurs in physical shuffling. Specifically, the final arguments to the CutDeck and Shuffle functions indicate whether we are asking for a perfect or random method. When the deck is cut randomly, the two piles should be roughly the same size, but not necessarily exactly equal. When the shuffle is random (not perfect), the cards will sometimes be interleaved in pairs, triples, or other small clusters of cards. We recommend the MersenneTwister library as a robust source of randomness for C++ programs.

How many random, not-quite-perfect cut & shuffle actions are sufficient to fully randomize a deck of 52 cards? Recent theoretical research results tell us that number is about 7! See also: http://en.wikipedia.org/wiki/Shuffling

Can you devise a scheme to measure the randomness of your result? If you shuffle fewer than 7 times, then the possible final positions for a specific card in the resulting deck or the possible neighboring cards for that element are limited. If we can devise simple statistics for these measures, then we may be able to show simulated results (over many, many trials) that support the theoretical proof. Collect your data and summarize your conclusions in your README.txt file.

A Note on the Program’s Text Output

In order to print the fancy suit characters, the provided code uses UTF, the Universal Character Set (UCS) Transformation Format. These characters do not display correctly in all web browsers, console terminals, code editors, or file viewers. When compiled, the executable for this homework does not require any command line arguments and the program will, by default, output these special characters. If the default (no command line arguments) output looks like gibberish in your usual development environment, terminal console, or file viewer you can provide the optional command line argument “no_outline_symbols” (some viewers only correctly display the solid black versions of the suit symbols) or “no_symbols” (which just uses 'C', 'D', 'H', and 'S' for the suits).

Additional Requirements, Hints and Suggestions

You will not use lists or vectors or iterators or other STL containers in this assignment. Also, you should not use the the STL sort algorithm. Instead, you will be manipulating the low-level custom Node objects, and the pointers that connect each Node to other Nodes in the structure. You do not need worry about the efficiency of your implementation or the efficiency of your sorting algorithm. A simple insertion sort or bubble sort algorithm is quite efficient for small datasets. Some of your other methods may also seem a little inefficient. That’s ok for this homework – the goal is to practice linked node pointer manipulation.

You should work on the assignment step by step, uncommenting each provided test case, and creating your own additional test cases to make sure your code is fully debugged. You should not modify the provided code except where indicated, as we will be compiling and testing your submitted files with different portions of the solution file.

Submission

Do all of your work in a new folder named hw5 inside of your Data Structures homeworks directory. Use good coding style when you design and implement your program. Be sure to make up new test cases and don’t forget to comment your code! Please use the provided template README.txt file for any notes you want the grader to read. You must do this assignment on your own, as described in the “Academic Integrity for Homework” handout. If you did discuss the problem or error messages, etc. with anyone, please list their names in your README.txt file. When you are finished please zip up your files exactly as instructed for the previous assignments and submit it through the course webpage.