#### **Declarative Computation Model**

Single assignment store (CTM 2.2) Kernel language syntax (CTM 2.3)

> Carlos Varela RPI March 5, 2015

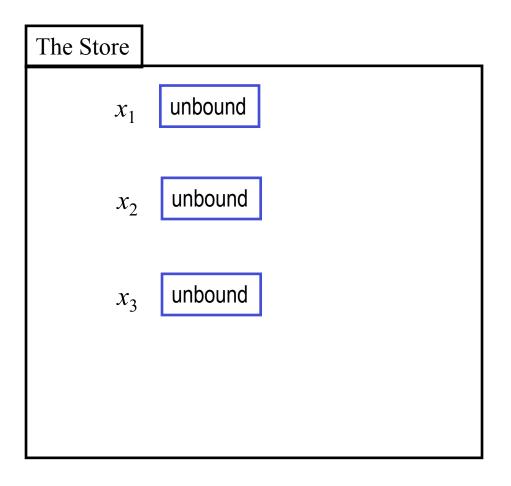
Adapted with permission from: Seif Haridi KTH Peter Van Roy UCL

# Sequential declarative computation model

- The single assignment store
  - declarative (dataflow) variables
  - partial values (variables and values are also called *entities*)
- The kernel language syntax
- The kernel language semantics
  - The environment: maps textual variable names (variable identifiers) into entities in the store
  - Interpretation (execution) of the kernel language elements (statements) by the use of an abstract machine
  - Abstract machine consists of an execution stack of statements transforming the store

# Single assignment store

- A single assignment store is a store (set) of variables
- Initially the variables are unbound, i.e. do not have a defined value
- Example: a store with three variables,  $x_1$ ,  $x_2$ , and  $x_3$



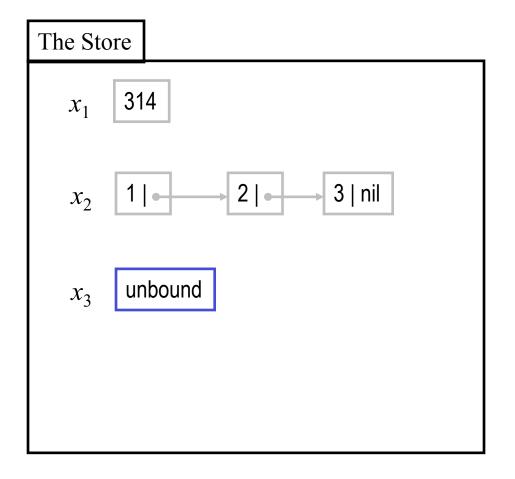
# Single assignment store (2)

- Variables in the store may be bound to values
- Example: assume we allow as values, integers and lists of integers

| The Store             |         |
|-----------------------|---------|
| <i>x</i> <sub>1</sub> | unbound |
| <i>x</i> <sub>2</sub> | unbound |
| <i>x</i> <sub>3</sub> | unbound |
|                       |         |

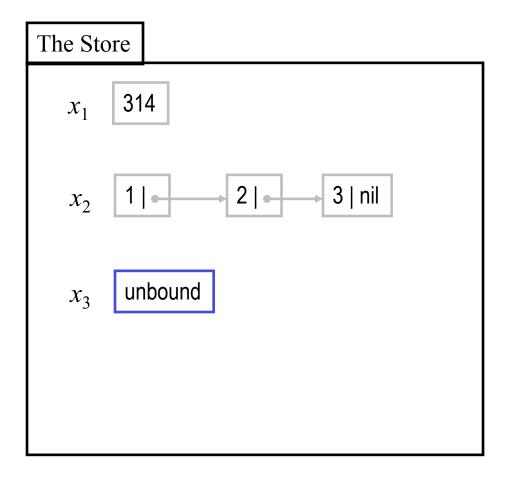
# Single assignment store (3)

- Variables in the store may be bound to values
- Assume we allow as values, integers and lists of integers
- Example:  $x_1$  is bound to the integer 314,  $x_2$  is bound to the list [1 2 3], and  $x_3$  is still unbound



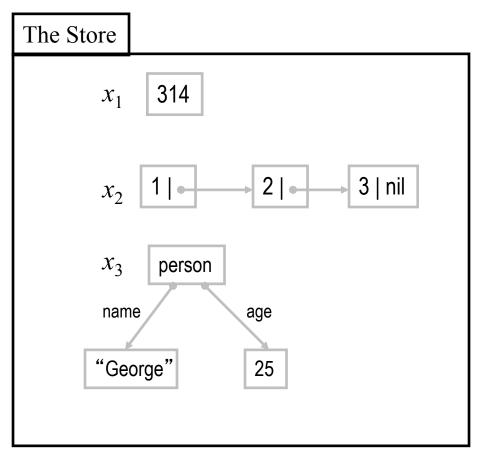
### Declarative (single-assignment) variables

- A declarative variable starts out as being unbound when created
- It can be bound to exactly one value
- Once bound it stays bound through the computation, and is indistinguishable from its value

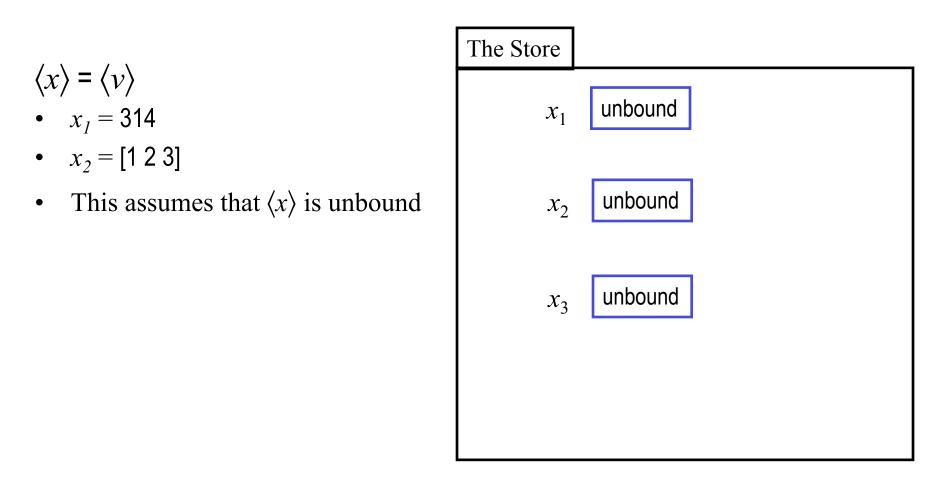


### Value store

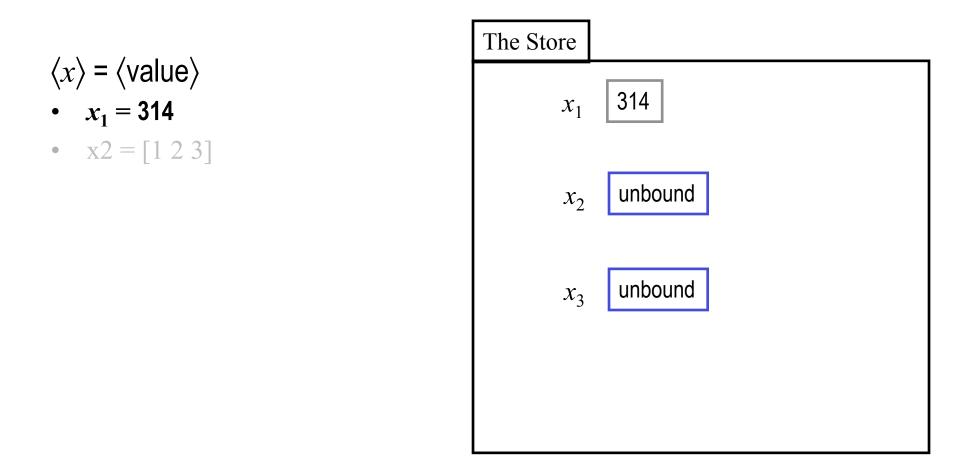
- A store where all variables are bound to values is called a value store
- Example: a value store where x<sub>1</sub> is bound to integer 314, x<sub>2</sub> to the list [1 2 3], and x<sub>3</sub> to the record (labeled tree) person(name: "George" age: 25)
- Functional programming computes functions on values, needs only a value store
- This notion of value store is enough for functional programming (ML, Haskell, Scheme)



#### Operations on the store (1) Single assignment



# Single-assignment

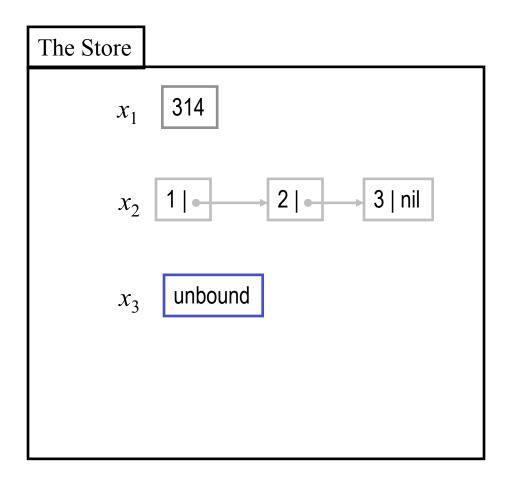


# Single-assignment (2)

#### $\langle x \rangle = \langle v \rangle$

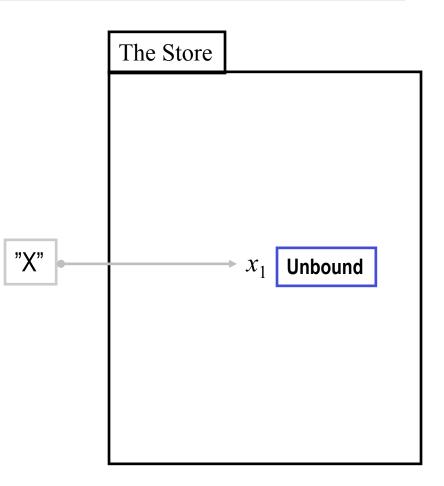
- $x_1 = 314$
- $x_2 = [1 2 3]$
- The single assignment operation

   ('=') constructs the \langle v \rangle in the store and binds the variable \langle x \rangle to this value
- If the variable is already bound, the operation will test the compatibility of the two values
- If the test fails an error is raised



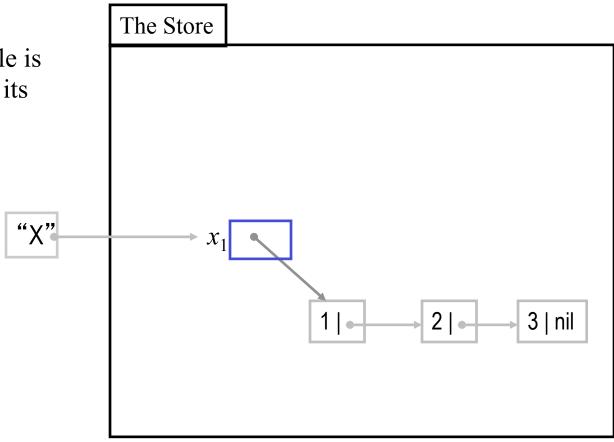
#### Variable identifiers

- Variable identifiers refers to store entities (variables or values)
- The environment maps variable identifiers to variables
- declare X
- local X in ...
- "X" is a (variable) identifier
- This corresponds to 'environment'  $\{"X" \rightarrow x_1\}$



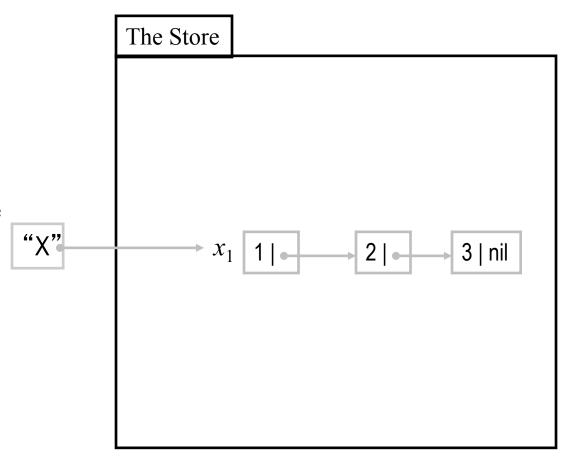
# Variable-value binding revisited (1)

- X = [1 2 3]
- Once bound the variable is indistinguishable from its value



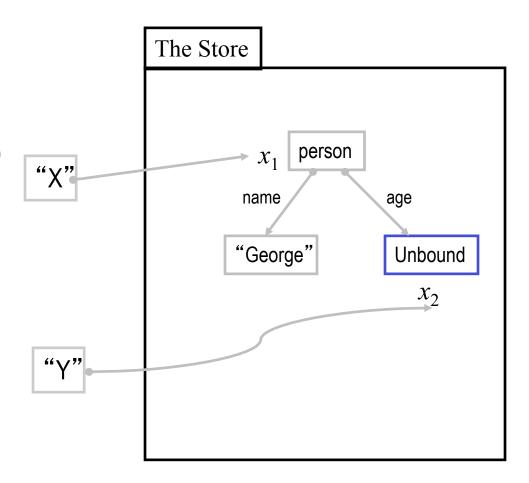
# Variable-value binding revisited (2)

- X = [1 2 3]
- Once bound the variable is indistinguishable from its value
- The operation of traversing variable cells to get the value is known as *dereferencing* and is invisible to the programmer



#### Partial Values

- A partial value is a data structure that may contain unbound variables
- The store contains the partial value: person(name: "George" age: x<sub>2</sub>)
- declare Y X
   X = person(name: "George" age: Y)
- The identifier 'Y' refers to  $x_2$

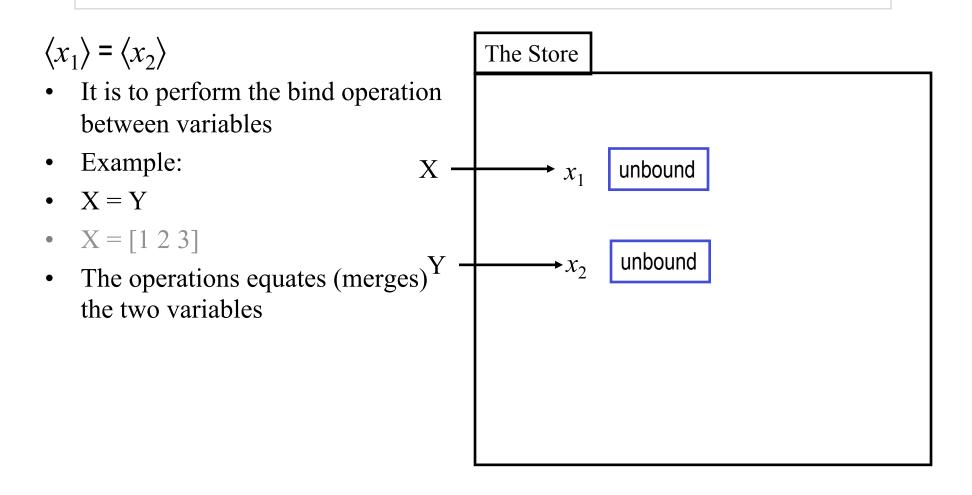


C. Varela; Adapted w/permission from S. Haridi and P. Van Roy

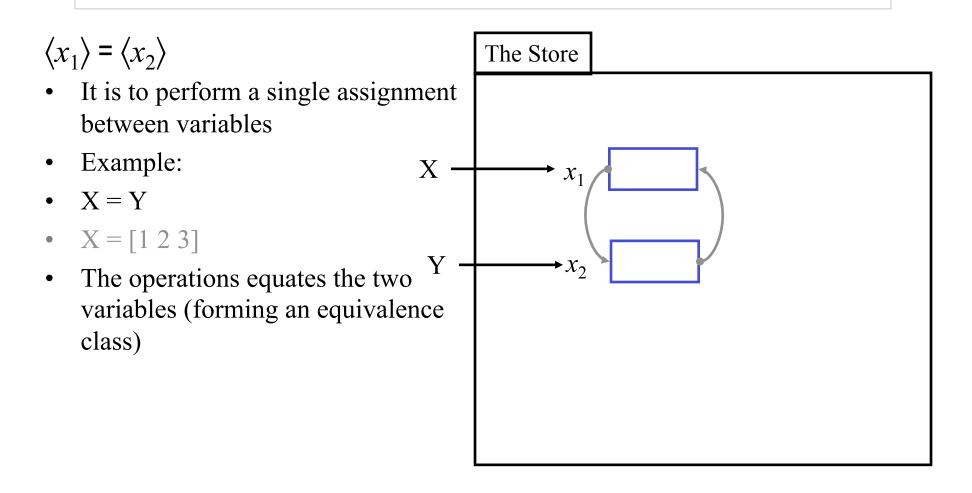
#### Partial Values (2)

#### Partial Values may be complete The Store declare Y X • X = person(name: "George" age: Y) Y = 25 • person $X_1$ "Х" name age "George" 25 $x_2$ "V"

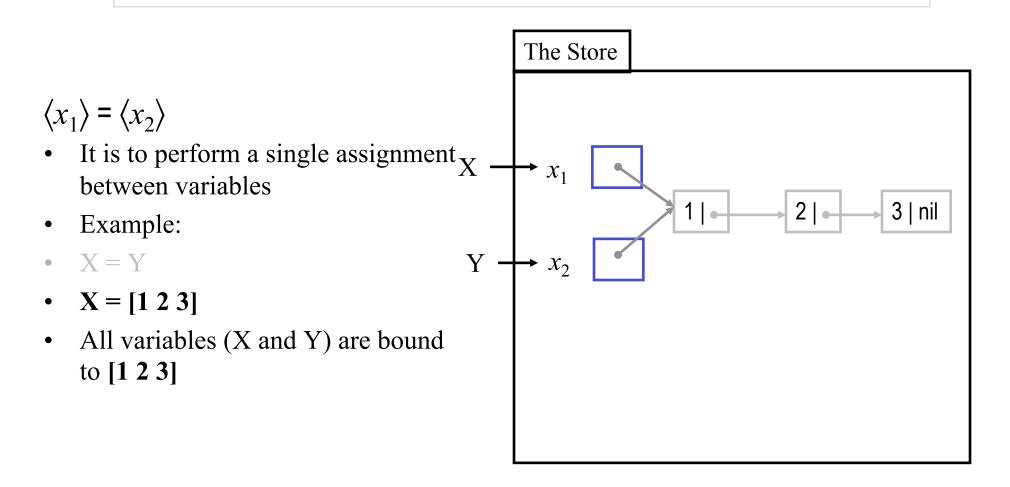
#### Variable to variable binding



# Variable to variable binding (2)



# Variable to variable binding (3)



#### Summary

#### Variables and partial values

- Declarative variable:
  - is an entity that resides in a single-assignment store, that is initially unbound, and can be bound to exactly one (partial) value
  - it can be bound to several (partial) values as long as they are compatible with each other
- Partial value:
  - is a data-structure that may contain unbound variables
  - when one of the variables is bound, it is replaced by the (partial) value it is bound to
  - a complete value, or *value* for short is a data structure that does not contain any unbound variables

# Declaration and use of variables

- Assume that variables can be declared (introduced) and used separately
- What happens if we try to use a variable before it is bound?
- 1. Use whatever value happens to be in the memory cell occupied by the variable (C, C++)
- 2. The variable is initialized to a default value (Java, SALSA), use the default
- 3. An error is signaled (Prolog). Makes sense if there is a single activity running (pure sequential programs)
- 4. An attempt to use the variable will wait (suspends) until another activity binds the variable (Oz/Mozart)

# Declaration and use of variables (2)

- An attempt to use the variable will wait (suspends) until another activity binds the variable (Oz/Mozart)
- Declarative (single assignment) variables that have this property are called *dataflow* variables
- It allows multiple operations to proceed concurrently giving the correct result
- Example: A = 23 running concurrently with B = A+1
- Functional (concurrent) languages do not allow the separation between declaration and binding (ML, Haskell, and Erlang)

# Kernel language syntax

The following defines the syntax of a statement,  $\langle s \rangle$  denotes a statement

 $\begin{array}{ll} \langle s \rangle & ::= skip \\ & | & \langle x \rangle = \langle y \rangle \\ & | & \langle x \rangle = \langle v \rangle \\ & | & \langle s_1 \rangle \langle s_2 \rangle \\ & | & local \langle x \rangle in \langle s_1 \rangle end \\ & | & if \langle x \rangle then \langle s_1 \rangle else \langle s_2 \rangle end \\ & | & if \langle x \rangle \langle y_1 \rangle \dots \langle y_n \rangle \ ' \}' \\ & | & case \langle x \rangle of \langle pattern \rangle then \langle s_1 \rangle else \langle s_2 \rangle end \end{array}$ 

empty statement variable-variable binding variable-value binding sequential composition declaration conditional procedural application pattern matching

value expression

{pattern> ::= ...

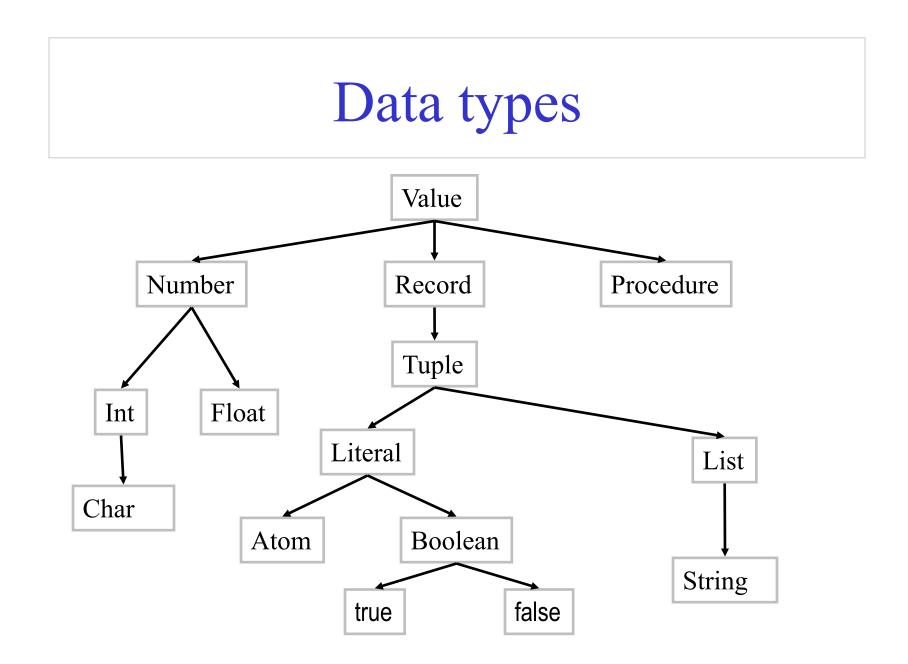
⟨v⟩ ::= ...

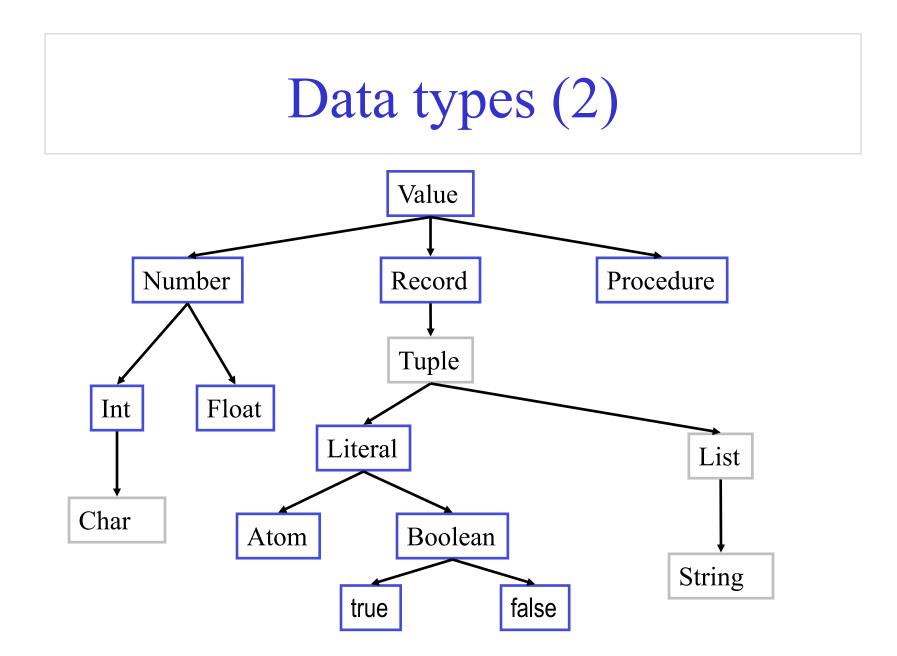
# Variable identifiers

- $\langle x \rangle$ ,  $\langle y \rangle$ ,  $\langle z \rangle$  stand for variables
- In the concrete kernel language variables begin with uppercase letter followed by a (possibly empty) sequence of alphanumeric characters or underscore
- Any sequence of printable characters within back-quote
- Examples:
  - X
  - Y1
  - Hello\_World
  - `hello this is a \$5 bill` (back-quote)

# Values and types

- A *data type* is a set of values and a set of associated operations
- Example: Int is the the data type "Integer", i.e set of all integer values
- 1 is *of type* lnt
- Int has a set of operations including +,-,\*,div, etc
- The model comes with a set of basic types
- Programs can define other types, e.g., *abstract data types* ADT





## Value expressions

 $\langle v \rangle$  ::=  $\langle procedure \rangle | \langle record \rangle | \langle number \rangle$ 

 $\langle \text{procedure} \rangle$  ::= proc '{ '\$  $\langle y_1 \rangle \dots \langle y_n \rangle$ '}'  $\langle s \rangle$  end

 $\begin{array}{ll} \langle \text{record} \rangle, \langle \text{pattern} \rangle & ::= & \langle \text{literal} \rangle \\ & | & \langle \text{literal} \rangle \left( \left[ \langle \text{feature}_1 \rangle : \langle X_1 \rangle \dots \langle \text{feature}_n \rangle : \langle X_n \rangle \right] \right) \end{array}$ 

 $\langle bool \rangle$  ::= true | false

 $\langle number \rangle$  ::=  $\langle int \rangle | \langle float \rangle$ 

#### Numbers

- Integers
  - 314, 0
  - ~10 (minus 10)
- Floats
  - 1.0, 3.4, 2.0e2, 2.0E2 (2×10<sup>2</sup>)

# Atoms and booleans

- A sequence starting with a lower-case character followed by characters or digits, ...
  - person, peter
  - 'Seif Haridi'
- Booleans:
  - true
  - false

# Records

- Compound representation (data-structures)
  - $\langle l \rangle (\langle f_1 \rangle : \langle x_1 \rangle \dots \langle f_n \rangle : \langle x_n \rangle)$
  - $-\langle l \rangle$  is a literal
- Examples
  - person(age:X1 name:X2)
  - person(1:X1 2:X2)
  - '|' (1:H 2:T)
  - nil
  - person

# Syntactic sugar (tuples)

• Tuples

 $\langle l \rangle (\langle x_1 \rangle \dots \langle x_n \rangle)$  (tuple)

- This is equivalent to the record  $\langle l \rangle (1: \langle x_1 \rangle \dots n: \langle x_n \rangle)$
- Example:

person('George' 25)

• This is the record

person(1: 'George' 2:25)

# Syntactic sugar (lists)

• Lists

 $\langle x_1 \rangle | \langle x_2 \rangle$  (a cons with the infix operator '|')

- This is equivalent to the tuple  $(\langle x_1 \rangle \langle x_2 \rangle)$
- Example:

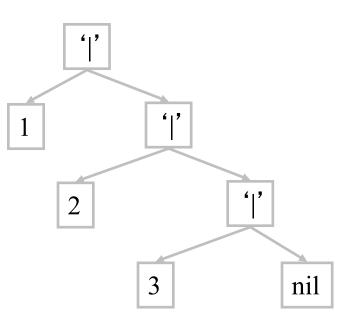
H|T

• This is the tuple '|' (H T)

# Syntactic sugar (lists)

- Lists
  - $\langle x_1 \rangle \mid \langle x_2 \rangle \mid \langle x_3 \rangle$
- '|' associates to the right  $\langle x_1 \rangle | (\langle x_2 \rangle | \langle x_3 \rangle)$
- Example:
   1 | 2 | 3 | nil
- Is

1 | (2 | (3 | nil ))



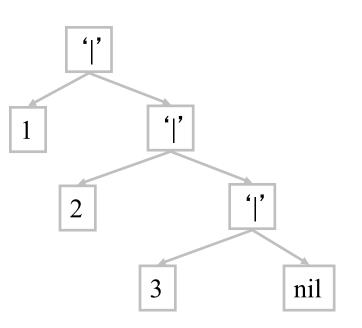
# Syntactic sugar (complete lists)

- Complete lists
- Example:

[1 2 3]

• Is

1 | (2 | (3 | nil ))



# Strings

- A string is a list of character codes enclosed with double quotes
- Ex: "E=mc^2"
- Means the same as [69 61 109 99 94 50]

#### Procedure declarations

- According to the kernel language  $\langle x \rangle = \text{proc} \{ \{ \langle y_1 \rangle \dots \langle y_n \rangle \} \langle s \rangle \text{ end} \}$ is a legal statement
- It binds  $\langle x \rangle$  to a procedure value
- This statement actually declares (introduces) a procedure
- Another syntactic variant which is more familiar is proc  $\{\langle x \rangle \langle y_1 \rangle \dots \langle y_n \rangle\} \langle s \rangle$  end
- This introduces (declares) the procedure  $\langle x \rangle$

# Operations of basic types

- Arithmetics
  - Floating point numbers: +,-,\*, and /
  - Integers: +,-,\*,div (integer division, i.e. truncate fractional part), mod (the remainder after a division, e.g.10 mod 3 = 1)
- Record operations
  - Arity, Label, and "."
  - X = person(name:"George" age:25)
  - ${Arity X} = [age name]$
  - {Label X} = person, X.age = 25
- Comparisons
  - Boolean comparisons, including ==,  $\geq$  (equality)
  - Numeric comparisons, =<, <, >, >=, compares integers, floats, and atoms

# Value expressions

 $\langle v \rangle$  ::=  $\langle procedure \rangle | \langle record \rangle | \langle number \rangle | \langle basicExpr \rangle$ 

```
\langle basicExpr \rangle ::= ... | \langle numberExpr \rangle | ...
```

```
\langle numberExpr \rangle ::= \langle x \rangle_1 + \langle x \rangle_2 | \dots
```

....

#### Syntactic sugar (multiple variables)

• Multiple variable introduction

local X Y in (statement) end

 is transformed to local X in local Y in (statement) end end

# Syntactic sugar (basic expressions)

• Basic expression nesting

if  $\langle basicExpr \rangle$  then  $\langle statement \rangle_1$  else  $\langle statement \rangle_2$  end

- is transformed to local T in T = (basicExpr) if T then (statement)<sub>1</sub> else (statement)<sub>2</sub> end end
- where T is a fresh ('new') variable identifier

# Syntactic sugar (variables)

• Variable initialization

local X =  $\langle value \rangle$  in  $\langle statement \rangle$  end

 Is transformed to local X in X = (value) (statement) end

#### Exercises

- 38. Using Oz, perform a few basic operations on numbers, records, and booleans (see Appendix B1-B3)
- 39. Explain the behavior of the declare statement in the interactive environment. Give an example of an interactive Oz session where "declare" and "declare ... in" produce different results. Explain why.
- 40. CTM Exercise 2.9.1
- 41. Describe what an anonymous procedure is, and write one in Oz. When are anonymous procedures useful?