

# Declarative Programming Techniques

Declarativeness, iterative computation (CTM 3.1-3.2)

Higher-order programming (CTM 3.6)

Abstract data types (CTM 3.7)

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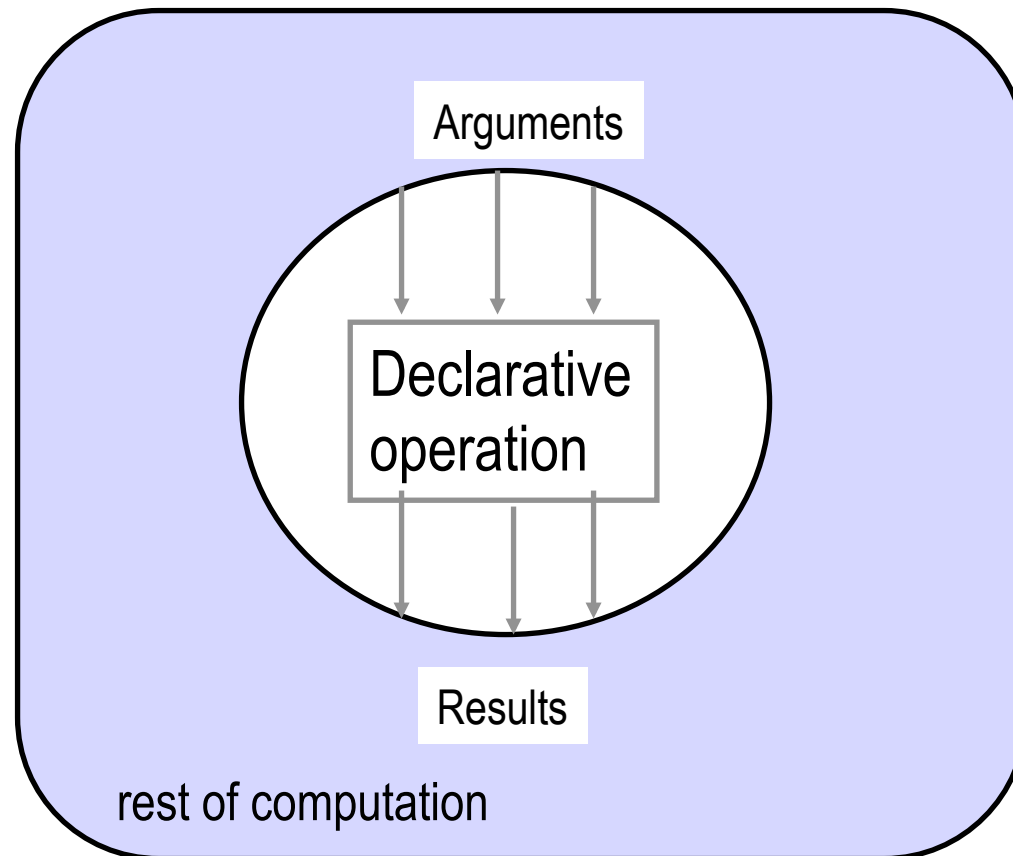
# Overview

- What is declarativeness?
  - Classification
  - Advantages for large and small programs
- Control Abstractions
  - Iterative programs
- Higher-Order Programming
  - Procedural abstraction
  - Genericity
  - Instantiation
  - Embedding
- Abstract data types
  - Encapsulation
  - Security

# Declarative operations (1)

- An operation is *declarative* if whenever it is called with the same arguments, it returns the same results independent of any other computation state
- A declarative operation is:
  - *Independent* (depends only on its arguments, nothing else)
  - *Stateless* (no internal state is remembered between calls)
  - *Deterministic* (call with same operations always give same results)
- Declarative operations can be composed together to yield other declarative components
  - All basic operations of the declarative model are declarative and combining them always gives declarative components

# Declarative operations (2)



# Why declarative components (1)

- There are two reasons why they are important:
- *(Programming in the large)* A declarative component can be written, tested, and proved correct independent of other components and of its own past history.
  - The complexity (reasoning complexity) of a program composed of declarative components is the *sum* of the complexity of the components
  - In general the reasoning complexity of programs that are composed of nondeclarative components explodes because of the intimate interaction between components
- *(Programming in the small)* Programs written in the declarative model are much easier to reason about than programs written in more expressive models (e.g., an object-oriented model).
  - Simple algebraic and logical reasoning techniques can be used

# Why declarative components (2)

- Since declarative components are mathematical functions, algebraic reasoning is possible i.e. substituting equals for equals
- The declarative model of Chapter 2 guarantees that all programs written are declarative
- Declarative components can be written in models that allow stateful data types, but there is no guarantee

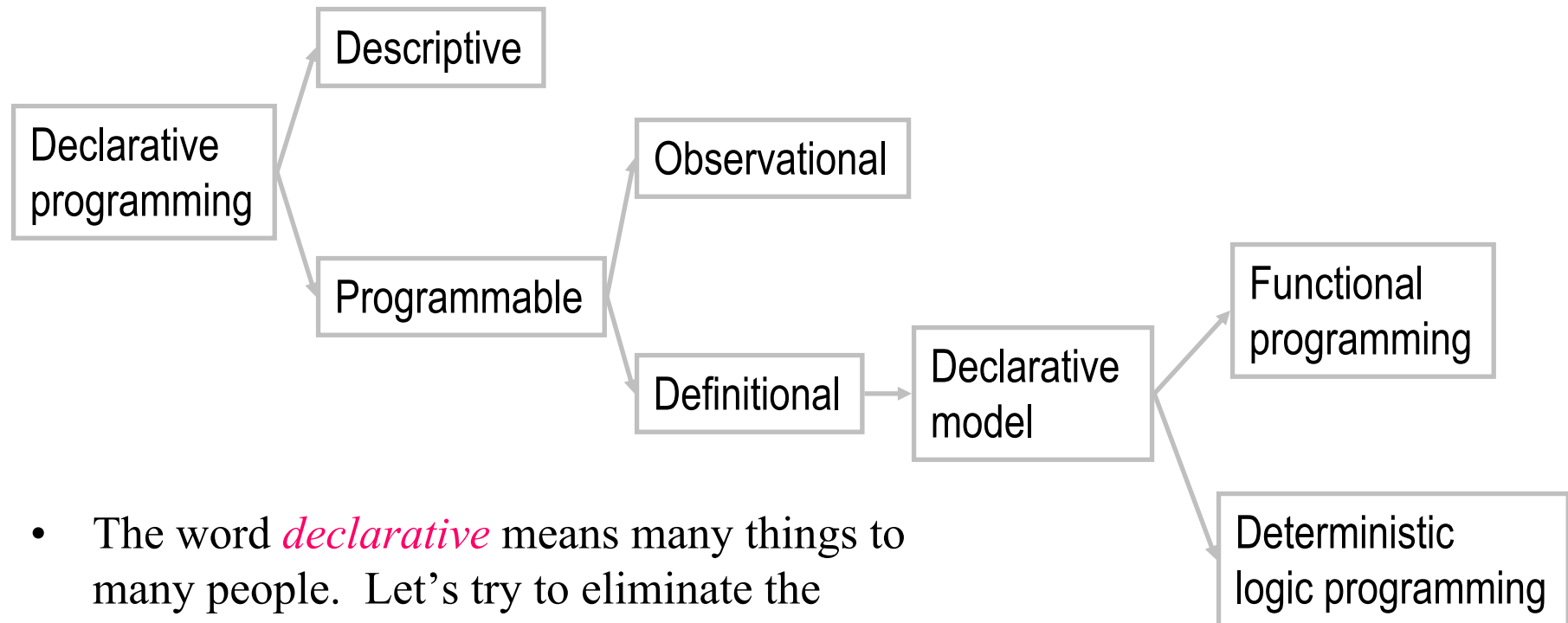
Given

$$f(a) = a^2$$

We can replace  $f(a)$  in any other equation

$$b = 7f(a)^2 \text{ becomes } b = 7a^4$$

# Classification of declarative programming



- The word *declarative* means many things to many people. Let's try to eliminate the confusion.
- The basic intuition is to program by defining the *what* without explaining the *how*

# Descriptive language

$\langle s \rangle ::=$	<code>skip</code>	<i>empty statement</i>
	<code><math>\langle x \rangle = \langle y \rangle</math></code>	<i>variable-variable binding</i>
	<code><math>\langle x \rangle = \langle \text{record} \rangle</math></code>	<i>variable-value binding</i>
	<code><math>\langle s_1 \rangle \langle s_2 \rangle</math></code>	<i>sequential composition</i>
	<code>local <math>\langle x \rangle</math> in <math>\langle s_1 \rangle</math> end</code>	<i>declaration</i>

Other descriptive languages include HTML and XML



# Descriptive language

```
<person id = "530101-xxx">  
  <name> Seif </name>  
  <age> 48 </age>  
</person>
```

Other descriptive languages include HTML and XML

# Kernel language

The following defines the syntax of a statement,  $\langle s \rangle$  denotes a statement

$\langle s \rangle ::=$	<code>skip</code>	<i>empty statement</i>
	<code><math>\langle x \rangle = \langle y \rangle</math></code>	<i>variable-variable binding</i>
	<code><math>\langle x \rangle = \langle v \rangle</math></code>	<i>variable-value binding</i>
	<code><math>\langle s_1 \rangle \langle s_2 \rangle</math></code>	<i>sequential composition</i>
	<code>local <math>\langle x \rangle</math> in <math>\langle s_1 \rangle</math> end</code>	<i>declaration</i>
	<code>proc '{<math>\langle x \rangle \langle y_1 \rangle \dots \langle y_n \rangle</math> }' <math>\langle s_1 \rangle</math> end</code>	<i>procedure introduction</i>
	<code>if <math>\langle x \rangle</math> then <math>\langle s_1 \rangle</math> else <math>\langle s_2 \rangle</math> end</code>	<i>conditional</i>
	<code>'{<math>\langle x \rangle \langle y_1 \rangle \dots \langle y_n \rangle</math> }'</code>	<i>procedure application</i>
	<code>case <math>\langle x \rangle</math> of <math>\langle \text{pattern} \rangle</math> then <math>\langle s_1 \rangle</math> else <math>\langle s_2 \rangle</math> end</code>	<i>pattern matching</i>

# Why the KL is declarative

- All basic operations are declarative
- Given the components (sub-statements) are declarative,
  - sequential composition
  - local statement
  - procedure definition
  - procedure call
  - if statement
  - case statement

are all declarative (independent, stateless, deterministic).

# Iterative computation

- An iterative computation is one whose execution stack is bounded by a constant, independent of the length of the computation
- Iterative computation starts with an initial state  $S_0$ , and transforms the state in a number of steps until a final state  $S_{\text{final}}$  is reached:

$$S_0 \longrightarrow S_1 \longrightarrow \dots \longrightarrow S_{\text{final}}$$

# The general scheme

```
fun {Iterate  $S_i$ }  
  if {IsDone  $S_i$ } then  $S_i$   
  else  $S_{i+1}$  in  
     $S_{i+1} = \{Transform\ S_i\}$   
    {Iterate  $S_{i+1}$ }  
  end  
end
```

- *IsDone* and *Transform* are problem dependent

# The computation model

- STACK : [ R={Iterate  $S_0$ } ]
- STACK : [  $S_1 = \{Transform\ S_0\}$ ,  
R={Iterate  $S_1$ } ]
- STACK : [ R={Iterate  $S_i$ } ]
- STACK : [  $S_{i+1} = \{Transform\ S_i\}$ ,  
R={Iterate  $S_{i+1}$ } ]
- STACK : [ R={Iterate  $S_{i+1}$ } ]

# Newton's method for the square root of a positive real number

- Given a real number  $x$ , start with a guess  $g$ , and improve this guess iteratively until it is accurate enough
- The improved guess  $g'$  is the average of  $g$  and  $x/g$ :

$$g' = (g + x / g) / 2$$

$$\varepsilon = g - \sqrt{x}$$

$$\varepsilon' = g' - \sqrt{x}$$

For  $g'$  to be a better guess than  $g$ :  $\varepsilon' < \varepsilon$

$$\varepsilon' = g' - \sqrt{x} = (g + x / g) / 2 - \sqrt{x} = \varepsilon^2 / 2g$$

$$\text{i.e. } \varepsilon^2 / 2g < \varepsilon, \quad \varepsilon / 2g < 1$$

$$\text{i.e. } \varepsilon < 2g, \quad g - \sqrt{x} < 2g, \quad 0 < g + \sqrt{x}$$

# Newton's method for the square root of a positive real number

- Given a real number  $x$ , start with a guess  $g$ , and improve this guess iteratively until it is accurate enough
- The improved guess  $g'$  is the average of  $g$  and  $x/g$ :
- Accurate enough is defined as:

$$|x - g^2| / x < 0.00001$$



# SqrtIter

```
fun {SqrtIter Guess X}
  if {GoodEnough Guess X} then Guess
  else
    Guess1 = {Improve Guess X} in
    {SqrtIter Guess1 X}
  end
end
```

- Compare to the general scheme:
  - The state is the pair `Guess` and `X`
  - *IsDone* is implemented by the procedure `GoodEnough`
  - *Transform* is implemented by the procedure `Improve`

# The program version 1

```
fun {Sqrt X}
  Guess = 1.0
in {SqrtIter Guess X}
end
fun {SqrtIter Guess X}
  if {GoodEnough Guess X} then
    Guess
  else
    {SqrtIter {Improve Guess X} X}
  end
end
end
```

```
fun {Improve Guess X}
  (Guess + X/Guess)/2.0
end
fun {GoodEnough Guess X}
  {Abs X - Guess*Guess}/X < 0.00001
end
```

# Using local procedures

- The main procedure Sqrt uses the helper procedures SqrtIter, GoodEnough, Improve, and Abs
- SqrtIter is only needed inside Sqrt
- GoodEnough and Improve are only needed inside SqrtIter
- Abs (absolute value) is a general utility
- The general idea is that helper procedures should not be visible globally, but only locally

# Sqrt version 2

```
local
  fun {SqrtIter Guess X}
    if {GoodEnough Guess X} then Guess
    else {SqrtIter {Improve Guess X} X} end
  end
  fun {Improve Guess X}
    (Guess + X/Guess)/2.0
  end
  fun {GoodEnough Guess X}
    {Abs X - Guess*Guess}/X < 0.000001
  end
in
  fun {Sqrt X}
    Guess = 1.0
  in {SqrtIter Guess X} end
end
```

# Sqrt version 3

- Define GoodEnough and Improve inside SqrtIter

local

```
fun {SqrtIter Guess X}
  fun {Improve}
    (Guess + X/Guess)/2.0
  end
  fun {GoodEnough}
    {Abs X - Guess*Guess}/X < 0.000001
  end
```

in

```
  if {GoodEnough} then Guess
  else {SqrtIter {Improve} X} end
```

end

in fun {Sqrt X}

```
  Guess = 1.0 in
  {SqrtIter Guess X}
```

end

end

# Sqrt version 3

- Define GoodEnough and Improve inside SqrtIter

local

```
fun {SqrtIter Guess X}
  fun {Improve}
    (Guess + X/Guess)/2.0
  end
  fun {GoodEnough}
    {Abs X - Guess*Guess}/X < 0.000001
  end
  in
    if {GoodEnough} then Guess
    else {SqrtIter {Improve} X} end
  end
end
```

```
in fun {Sqrt X}
  Guess = 1.0 in
  {SqrtIter Guess X}
end
end
```

The program has a single drawback: on each iteration two procedure values are created, one for Improve and one for GoodEnough

# Sqrt final version

```
fun {Sqrt X}
  fun {Improve Guess}
    (Guess + X/Guess)/2.0
  end
  fun {GoodEnough Guess}
    {Abs X - Guess*Guess}/X < 0.000001
  end
  fun {SqrtIter Guess}
    if {GoodEnough Guess} then Guess
    else {SqrtIter {Improve Guess}} end
  end
  Guess = 1.0
in {SqrtIter Guess}
end
```

The final version is  
a compromise between  
abstraction and efficiency

# From a general scheme to a control abstraction (1)

```
fun {Iterate  $S_i$ }  
  if {IsDone  $S_i$ } then  $S_i$   
  else  $S_{i+1}$  in  
     $S_{i+1} = \{Transform\ S_i\}$   
    {Iterate  $S_{i+1}$ }  
  end  
end
```

- *IsDone* and *Transform* are problem dependent



# From a general scheme to a control abstraction (2)

```
fun {Iterate S IsDone Transform}
  if {IsDone S} then S
  else S1 in
    S1 = {Transform S}
    {Iterate S1 IsDone Transform}
  end
end
```

```
fun {Iterate  $S_i$ }
  if {IsDone  $S_i$ } then  $S_i$ 
  else  $S_{i+1}$  in
     $S_{i+1} = \{Transform S_i\}$ 
    {Iterate  $S_{i+1}$ }
  end
end
```

# Sqrt using the Iterate abstraction

```
fun {Sqrt X}
  fun {Improve Guess}
    (Guess + X/Guess)/2.0
  end
  fun {GoodEnough Guess}
    {Abs X - Guess*Guess}/X < 0.000001
  end
  Guess = 1.0
in
  {Iterate Guess GoodEnough Improve}
end
```

# Sqrt using the control abstraction

```
fun {Sqrt X}  
  {Iterate  
    1.0  
    fun {$ G} {Abs X - G*G}/X < 0.000001 end  
    fun {$ G} (G + X/G)/2.0 end  
  }  
end
```

Iterate could become a linguistic abstraction

# Higher-order programming

- **Higher-order programming** = the set of programming techniques that are possible with procedure values (lexically-scoped closures)
- Basic operations
  - **Procedural abstraction**: creating procedure values with lexical scoping
  - **Genericity**: procedure values as arguments
  - **Instantiation**: procedure values as return values
  - **Embedding**: procedure values in data structures
- Control abstractions
  - Integer and list loops, accumulator loops, folding a list (left and right)
- Data-driven techniques
  - List filtering, tree folding
- Explicit lazy evaluation, currying
- Higher-order programming is the foundation of component-based programming and object-oriented programming

# Procedural abstraction

- Procedural abstraction is the ability to convert any statement into a procedure value
  - A procedure value is usually called a **closure**, or more precisely, a **lexically-scoped closure**
  - A procedure value is a pair: it combines the procedure code with the environment where the procedure was created (the contextual environment)
- Basic scheme:
  - Consider any statement  $\langle s \rangle$
  - Convert it into a procedure value:  $P = \text{proc } \{\$ \} \langle s \rangle \text{ end}$
  - Executing  $\{P\}$  has **exactly the same effect** as executing  $\langle s \rangle$

# Procedural abstraction

```
fun {AndThen B1 B2}  
  if B1 then B2 else false  
  end  
end
```

# Procedural abstraction

```
fun {AndThen B1 B2}  
  if {B1} then {B2} else false  
  end  
end
```

# A common limitation

- Most popular imperative languages (C, Pascal) do **not** have procedure values
- They have only **half** of the pair: variables can reference procedure code, but there is no contextual environment
- This means that **control abstractions cannot be programmed** in these languages
  - They provide a predefined set of control abstractions (for, while loops, if statement)
- Generic operations are still possible
  - They can often get by with just the procedure code. The contextual environment is often empty.
- The limitation is due to **the way memory is managed** in these languages
  - Part of the store is put on the stack and deallocated when the stack is deallocated
  - This is supposed to make memory management simpler for the programmer on systems that have no garbage collection
  - It means that contextual environments cannot be created, since they would be full of dangling pointers
- Object-oriented programming languages can use objects to encode procedure values by making external references (contextual environment) instance variables.



# Genericity

- Replace specific entities (zero 0 and addition +) by function arguments
- The same routine can do the sum, the product, the logical or, etc.

```
fun {SumList L}
  case L
  of nil then 0
  [] X|L2 then X+{SumList L2}
  end
end
```



```
fun {FoldR L F U}
  case L
  of nil then U
  [] X|L2 then {F X {FoldR L2 F U}}
  end
end
```

# Instantiation

```
fun {FoldFactory F U}
  fun {FoldR L}
    case L
    of nil then U
    [] X|L2 then {F X {FoldR L2}}
    end
  end
in
  FoldR
end
```

- Instantiation is when a procedure returns a procedure value as its result
- Calling {FoldFactory fun {\$ A B} A+B end 0} returns a function that behaves identically to SumList, which is an « **instance** » of a folding function

# Embedding

- Embedding is when procedure values are put in data structures
- Embedding has many uses:
  - **Modules**: a module is a record that groups together a set of related operations
  - **Software components**: a software component is a generic function that takes a set of modules as its arguments and returns a new module. It can be seen as **specifying** a module in terms of the modules it needs.
  - **Delayed evaluation** (also called **explicit lazy evaluation**): build just a small part of a data structure, with functions at the extremities that can be called to build more. The consumer can control explicitly how much of the data structure is built.

# Control Abstractions

declare

proc {For I J P}

  if I  $\geq$  J then skip

  else {P I} {For I+1 J P}

  end

end

{For 1 10 Browse}

for I in 1..10 do {Browse I} end

# Control Abstractions

```
proc {ForAll Xs P}  
  case Xs  
  of nil then skip  
  [] X|Xr then  
    {P X} {ForAll Xr P}  
  end  
end
```

```
{ForAll [a b c d]  
  proc {$ I} {System.showInfo "the item is: " # I} end}
```

```
for I in [a b c d] do  
  {System.showInfo "the item is: " # I}  
end
```

# Control Abstractions

```
fun {FoldL Xs F U}  
  case Xs  
  of nil then U  
  [] X|Xr then {FoldL Xr F {F X U}}  
  end  
end
```

Assume a list  $[x1\ x2\ x3\ \dots]$

$$S0 \rightarrow S1 \rightarrow S2$$
$$U \rightarrow \{F\ x1\ U\} \rightarrow \{F\ x2\ \{F\ x1\ U\}\} \rightarrow \dots \rightarrow$$

# Control Abstractions

```
fun {FoldL Xs F U}  
  case Xs  
  of nil then U  
  [] X|Xr then {FoldL Xr F {F X U}}  
  end  
end
```

What does this program do ?

```
{Browse {FoldL [1 2 3]  
  fun {$ X Y} X|Y end nil}}
```

# List-based techniques

```
fun {Map Xs F}
  case Xs
  of nil then nil
  [] X|Xr then
    {F X}|{Map Xr F}
  end
end
```

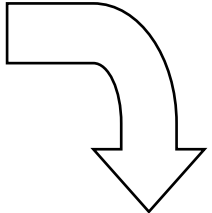
```
fun {Filter Xs P}
  case Xs
  of nil then nil
  [] X|Xr andthen {P X} then
    X|{Filter Xr P}
  [] X|Xr then {Filter Xr P}
  end
end
```



# Tree-based techniques

```
proc {DFS Tree}
  case Tree of tree(node:N sons:Sons ...) then
    {Browse N}
    for T in Sons do {DFS T} end
  end
end
```

Call {P T} at each node T



```
proc {VisitNodes Tree P}
  case Tree of tree(node:N sons:Sons ...) then
    {P N}
    for T in Sons do {VisitNodes T P} end
  end
end
```

# Explicit lazy evaluation

- Supply-driven evaluation. (e.g. The list is completely calculated independent of whether the elements are needed or not. )
- Demand-driven execution.(e.g. The consumer of the list structure asks for new list elements when they are needed.)
- Technique: a programmed trigger.
- How to do it with higher-order programming? The consumer has a function that it calls when it needs a new list element. The function call returns a pair: the list element and a new function. The new function is the new trigger: calling it returns the next data item and another new function. And so forth.

# Currying

- Currying is a technique that can simplify programs that heavily use higher-order programming.
- The idea: function of n arguments  $\Rightarrow$  n nested functions of one argument.
- Advantage: The intermediate functions can be useful in themselves.

```
fun {Max X Y}
  if X>=Y then X else Y end
end
```



```
fun {Max X}
  fun {$ Y}
    if X>=Y then X else Y end
  end
end
```

# Abstract data types

- A datatype is a set of values and an associated set of operations
- A datatype is abstract only if it is completely described by its set of operations regardless of its implementation
- This means that it is possible to change the implementation of the datatype without changing its use
- The datatype is thus described by a set of procedures
- These operations are the only thing that a user of the abstraction can assume

# Example: A Stack

- Assume we want to define a new datatype  $\langle \text{stack } T \rangle$  whose elements are of any type  $T$

fun {NewStack}:  $\langle \text{Stack } T \rangle$

fun {Push  $\langle \text{Stack } T \rangle \langle T \rangle$  }:  $\langle \text{Stack } T \rangle$

fun {Pop  $\langle \text{Stack } T \rangle \langle T \rangle$  }:  $\langle \text{Stack } T \rangle$

fun {IsEmpty  $\langle \text{Stack } T \rangle$  }:  $\langle \text{Bool} \rangle$

- These operations normally satisfy certain conditions:

$\{\text{IsEmpty } \{\text{NewStack}\}\} = \text{true}$

for any  $E$  and  $S0$ ,  $S1 = \{\text{Push } S0 E\}$  and  $S0 = \{\text{Pop } S1 E\}$  hold

$\{\text{Pop } \{\text{NewStack}\} E\}$  raises error

# Stack (implementation)

```
fun {NewStack} nil end
```

```
fun {Push S E} E|S end
```

```
fun {Pop S E} case S of X|S1 then E = X S1 end end
```

```
fun {IsEmpty S} S==nil end
```

# Stack (another implementation)

```
fun {NewStack} nil end
```

```
fun {Push S E} E|S end
```

```
fun {Pop S E} case S of X|S1 then E = X S1 end end
```

```
fun {IsEmpty S} S==nil end
```

---

```
fun {NewStack} emptyStack end
```

```
fun {Push S E} stack(E S) end
```

```
fun {Pop S E} case S of stack(X S1) then E = X S1 end end
```

```
fun {IsEmpty S} S==emptyStack end
```

# Dictionaries

- The datatype dictionary is a finite mapping from a set  $T$  to  $\langle \text{value} \rangle$ , where  $T$  is either  $\langle \text{atom} \rangle$  or  $\langle \text{integer} \rangle$
- fun {NewDictionary}
  - returns an empty mapping
- fun {Put D Key Value}
  - returns a dictionary identical to  $D$  except  $\text{Key}$  is mapped to  $\text{Value}$
- fun {CondGet D Key Default}
  - returns the value corresponding to  $\text{Key}$  in  $D$ , otherwise returns  $\text{Default}$
- fun {Domain D}
  - returns a list of the keys in  $D$



# Implementation

```
fun {Put Ds Key Value}
  case Ds
  of nil then [Key#Value]
  [] (K#V)|Dr andthen Key==K then
    (Key#Value) | Dr
  [] (K#V)|Dr andthen K>Key then
    (Key#Value)|(K#V)|Dr
  [] (K#V)|Dr andthen K<Key then
    (K#V)|{Put Dr Key Value}
  end
end
```

# Implementation

```
fun {CondGet Ds Key Default}
  case Ds
  of nil then Default
  [] (K#V)|Dr andthen Key==K then
    V
  [] (K#V)|Dr andthen K>Key then
    Default
  [] (K#V)|Dr andthen K<Key then
    {CondGet Dr Key Default}
  end
end
fun {Domain Ds}
  {Map Ds fun {$ K#_} K end}
end
```

# Further implementations

- Because of abstraction, we can replace the dictionary ADT implementation using a list, whose complexity is linear (i.e.,  $O(n)$ ), for a binary tree implementation with logarithmic operations (i.e.,  $O(\log(n))$ ).
- Data abstraction makes clients of the ADT unaware (other than through perceived efficiency) of the internal implementation of the data type.
- It is important that clients do not use anything about the internal representation of the data type (e.g., using `{Length Dictionary}` to get the size of the dictionary). Using only the interface (defined ADT operations) ensures that different implementations can be used in the future.

# Secure abstract data types: Stack is not secure

```
fun {NewStack} nil end
fun {Push S E} E|S end
fun {Pop S E}
  case S of X|S1 then E=X S1 end
end
fun {IsEmpty S} S==nil end
```

# Secure abstract data types II

- The representation of the stack is visible:

[a b c d]

- Anyone can use an incorrect representation, i.e., by passing other language entities to the stack operation, causing it to malfunction (like  $a|b|X$  or  $Y=a|b|Y$ )
- Anyone can write new operations on stacks, thus breaking the abstraction-representation barrier
- How can we guarantee that the representation is invisible?

# Secure abstract data types III

- The model can be extended. Here are two ways:
  - By adding a new basic type, an **unforgeable constant** called a **name**
  - By adding **encapsulated state**.
- A **name** is like an atom except that it **cannot be typed in on a keyboard or printed!**
  - The only way to have a name is if one is given it explicitly
- There are just two operations on names:
  - $N = \{\text{NewName}\}$  : returns a fresh name
  - $N1 == N2$  : returns true or false

# Secure abstract datatypes IV

- We want to « wrap » and « unwrap » values
- Let us use names to define a wrapper & unwrapper

```
proc {NewWrapper ?Wrap ?Unwrap}
  Key={NewName}
in
  fun {Wrap X}
    fun {$ K} if K==Key then X end end
  end
  fun {Unwrap C}
    {C Key}
  end
end
```

# Secure abstract data types: A secure stack

With the wrapper & unwrapper we can build a secure stack

```
local Wrap Unwrap in
  {NewWrapper Wrap Unwrap}
  fun {NewStack} {Wrap nil} end
  fun {Push S E} {Wrap E|{Unwrap S}} end
  fun {Pop S E}
    case {Unwrap S} of X|S1 then E=X {Wrap S1} end
  end
  fun {IsEmpty S} {Unwrap S}==nil end
end
```



# Capabilities and security

- We say a computation is **secure** if it has well-defined and controllable properties, independent of the existence of other (possibly malicious) entities (either computations or humans) in the system
- What properties must a language have to be secure?
- One way to make a language secure is to base it on **capabilities**
  - A **capability** is an unforgeable language entity (« ticket ») that gives its owner the right to perform a particular action and only that action
  - In our model, **all values are capabilities** (records, numbers, procedures, names) since they give the right to perform operations on the values
  - Having a procedure gives the right to **call** that procedure. Procedures are very general capabilities, since what they do depends on their argument
  - Using names as procedure arguments allows very precise control of rights; for example, it allows us to build secure abstract data types
- Capabilities originated in operating systems research
  - A capability can give a process the right to create a file in some directory

# Secure abstract datatypes V

- We add two new concepts to the computation model
- {NewChunk Record}
  - returns a value similar to record but its arity cannot be inspected
  - recall {Arity foo(a:1 b:2)} is [a b]
- {NewName}
  - a function that returns a new symbolic (unforgeable, i.e. cannot be guessed) name
  - foo(a:1 b:2 {NewName}:3) makes impossible to access the third component, if you do not know the arity
- {NewChunk foo(a:1 b:2 {NewName}:3) }
  - Returns what ?

# Secure abstract datatypes VI

```
proc {NewWrapper ?Wrap ?Unwrap}
  Key={NewName}
in
  fun {Wrap X}
    {NewChunk foo(Key:X)}
  end
  fun {Unwrap C}
    C.Key
  end
end
```

# Secure abstract data types: Another secure stack

With the new wrapper & unwrapper we can build another secure stack (since we only use the interface to wrap and unwrap, the code is identical to the one using higher-order programming)

```
local Wrap Unwrap in
  {NewWrapper Wrap Unwrap}
  fun {NewStack} {Wrap nil} end
  fun {Push S E} {Wrap E|{Unwrap S}} end
  fun {Pop S E}
    case {Unwrap S} of X|S1 then E=X {Wrap S1} end
  end
  fun {IsEmpty S} {Unwrap S}==nil end
end
```

# Exercises

58. Modify the Pascal function to use local functions for AddList, ShiftLeft, ShiftRight. Think about the abstraction and efficiency tradeoffs.
59. CTM Exercise 3.10.2 (page 230)
60. CTM Exercise 3.10.3 (page 230)
61. Develop a control abstraction for iterating over a list of elements.

# Exercises

62. Implement the function  $\{\text{FilterAnd } Xs\ P\ Q\}$  that returns all elements of  $Xs$  in order for which  $P$  and  $Q$  return true. Hint: Use  $\{\text{Filter } Xs\ P\}$ .
63. Compute the maximum element from a nonempty list of numbers by folding.
64. Suppose you have two sorted lists. Merging is a simple method to obtain an again sorted list containing the elements from both lists. Write a Merge function that is generic with respect to the order relation.
65. CTM Exercise 3.10.17 (pg. 232). You do not need to implement it using gump, simply specify how you would add currying to Oz (syntax and semantics).