

CONCURRENCY ISSUES

ADVANTAGES

- Reactive Programming
- Availability of Services
- Controllability.
- Active Objects (Actors)
- Asynchronous Messages
- Parallelism

CONCURRENCE ISSUES

LIMITATIONS

- Safety "Nothing bad ever happens"
 - Liveness "Anything ever happens at all"
 - Nondeterminism
 - Inherent sequencing in algorithms
 - Resource consumption
 - Threads are expensive
 - Scheduling overhead
 - Synchronization overhead
- ∴ Concurrent programs can run more slowly than sequential ones even if you have multiple CPUs.

THEORY AND PRACTICE

"In theory, theory and practice are very related. In practice,..."

λ -Calculus

Predicate
Calculus

π -Calculus &
Actor Model

Functional Programming
& Imperative

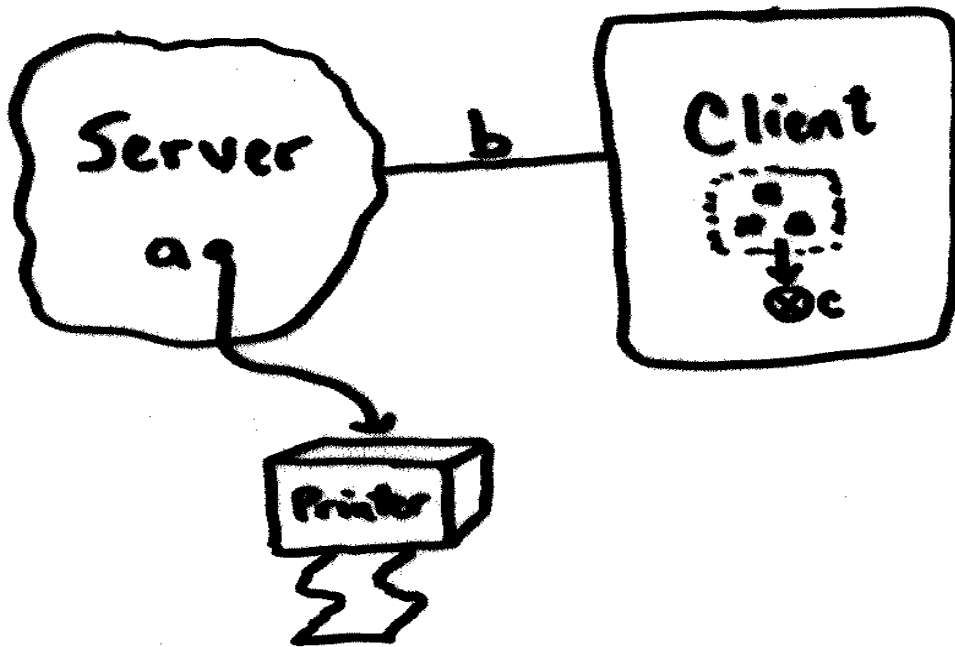
Logic Programming

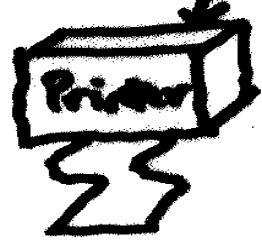
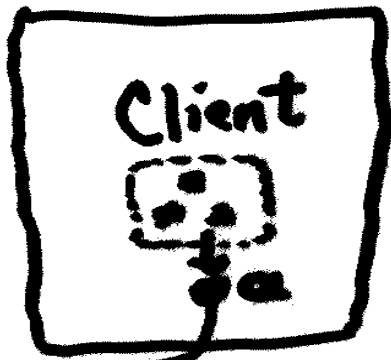
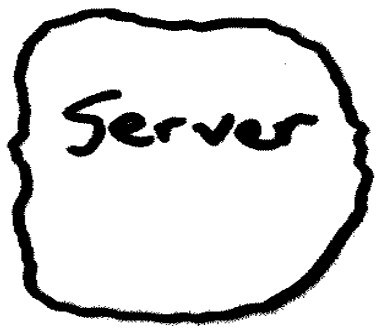
Concurrent &
Distributed Programming

Those theoretically inclined, check out:

A Theory of Objects, by Abadi &
Cardelli.

PI-CALCULUS


$$\bar{b}a.S \mid b(c).\bar{c}d.P$$
$$\xrightarrow{\tau} S \mid \bar{c}d.P\{a/c\}$$
$$S \mid \bar{a}d.P$$



S | ad.P

π -CALCULUS NOTATION

CHANNELS / NAMES

a, b, c, \dots

PROCESSES / AGENTS

P, Q, R, \dots

e.g.:

$\bar{b}a.S \mid b(c).\bar{e}d.P$

$\xrightarrow{\tau} S \mid \bar{e}d.P\{a/c\}$

$S \mid \bar{a}d.P\{a/c\}$

π -CALCULUS SYNTAX

Prefixes

$\alpha ::= \bar{a}x$
 $a(x)$
 τ

Output
Input
Silent

Agents

$P ::= 0$
 $\alpha.P$
 $P+P$
 $P|P$
if $x=y$ then P
if $x \neq y$ then P
 $(\nu x)P$
 $A(y_1, \dots, y_n)$

Nil
Prefix
Sum
Parallel
Match
Mismatch
Restriction
Identifier

Definitions

$A(x_1, \dots, x_n) \stackrel{\text{def}}{=} P$ (where $i \neq j \Rightarrow x_i \neq x_j$)

FREE AND BOUND OCCURRENCES

$a(x).P$
 $(\lambda x)P$ } bind x on P

$\bar{a}x.P$ } does NOT bind
 x on P

EXERCISE

$$fn(a(x).P) =$$

$$fn(\exists x.P) =$$

$$fn(\bar{a}x.P) =$$

$$bn(a(x).P) =$$

$$bn(\exists x.P) =$$

$$bn(\bar{a}x.P) =$$

to be defined
in terms of
 $a, x,$
 $fn(P)$ and
 $bn(P).$

STRUCTURAL CONGRUENCE

P and Q are structurally congruent, if they represent the same thing, although syntactically different. We write $P \equiv Q$, if

① P and Q are variants of α -conversion.

② Abelian laws for $|$ and $+$.

$$P|Q \equiv Q|P$$

$$(P|Q)|R \equiv P|(Q|R)$$

$$P|0 \equiv P$$

③ Unfolding law

$$A(\tilde{y}) \equiv P\{\tilde{y}/\tilde{x}\} \text{ if } A(\tilde{x}) \stackrel{\text{def}}{=} P.$$

④ Scope extension laws

$$(\nu x) 0$$

$$(\nu x) (P|Q)$$

$$(\nu x) (P+Q)$$

$$(\nu x) \text{ if } u=v \text{ then } P$$

$$(\nu x) \text{ if } u \neq v \text{ then } P$$

$$(\nu x) (\nu y) P$$

$$\equiv 0$$

$$\equiv P|(\nu x)Q$$

$$\equiv P+(\nu x)Q$$

$$\equiv \text{if } u=v \text{ then } (\nu x)P$$

$$\equiv \text{if } u \neq v \text{ then } (\nu x)P$$

$$\equiv (\nu y)(\nu x)P$$

$$\left. \begin{array}{l} \equiv 0 \\ \equiv P|(\nu x)Q \\ \equiv P+(\nu x)Q \end{array} \right\} \text{ if } x \notin \text{fn}(P)$$

SCOPE EXTRUSION

$a(x).P \mid (\nu b) \bar{a}b.Q$, $b \notin \text{fn}(P)$

$\equiv (\nu b) (a(x).P \mid \bar{a}b.Q)$

$\xrightarrow{\tau} (\nu b) (P\{b/x\} \mid Q)$

If $b \in \text{fn}(P)$, rename b to $b' \notin \text{fn}(P)$

$$a(x). \bar{e}x \mid (\forall b) \bar{a}b$$

$$\equiv (\forall b) (a(x). \bar{e}x \mid \bar{a}b)$$

$$\xrightarrow{\exists} (\forall b) (\bar{e}b \mid 0)$$

$$\xrightarrow{\exists} (\forall b) \bar{e}b$$

$$a(b). \bar{e}b \mid (\forall b) \bar{a}b$$

$$\equiv a(b). \bar{e}b \mid (\forall d) \bar{a}d$$

$$\equiv (\forall d) (a(b). \bar{e}b \mid \bar{a}d)$$

$$\xrightarrow{\exists} (\forall d) \bar{e}d$$

EXERCISES:

Q:

1. $(\forall a) \bar{a}b.P \mid \bar{a}c.Q \mid a(x).R$

2. $(\forall b) \bar{a}b \mid \exists a(x). \bar{b}x$

$\xrightarrow{\exists} \textcircled{?}$

EXECUTOR EXAMPLE

$$\text{Exec}(x) = x(y).\bar{y}$$

$$A(x) = (\nu z)(\bar{x}z | z.P)$$

Agent $A(x)$ will behave as P when combined with $\text{Exec}(x)$.

Proof.

$$A(x) | \text{Exec}(x)$$



REPLICATION

$(!P) \stackrel{\text{def}}{=} P \mid !P$

A REFERENCE CELL IN π -CALCULUS

$$\text{Ref}(r, w, i) = (\nu l) (\bar{l}i \mid \text{ReadServer}(l, r) \mid \text{WriteServer}(l, w))$$

$$\text{ReadServer}(l, r) = ! r(c). l(v). (\bar{c}v \mid \bar{l}v)$$

$$\text{WriteServer}(l, w) = ! w(c, v'). l(v). (\bar{c} \mid \bar{l}v')$$

Example using reference cell:

$$(\nu c) \bar{w}\langle c, v \rangle. c. (\nu d) \bar{F}d. d(e). Q$$

will receive the value v over the channel d assuming no other processes interacting with the reference cell.