

CSCI-1200 Data Structures — Spring 2023

Lecture 17 – Trees, Part I

Review from Lecture 16

- Maps containing more complicated values. Example: index mapping words to the text line numbers on which they appear.
- Maps whose keys are class objects. Example: maintaining student records.
- Intro to Binary Trees, Binary Search Trees, & Balanced Trees

Today's Lecture

- STL `set` container class (like STL `map`, but without the pairs!) (leetcode 1207)
- Implementation of `ds_set` class using binary search trees
- In-order, pre-order, and post-order traversal (leetcode 230)

17.1 Standard Library Sets

- STL sets are *ordered* containers storing unique “keys”. An ordering relation on the keys, which defaults to `operator<`, is necessary. Because STL sets are ordered, they are technically not traditional mathematical sets.
- Sets are like maps except they have only keys, there are no associated values. Like maps, the keys are **constant**. This means you can't change a key while it is in the set. You must remove it, change it, and then reinsert it.
- Access to items in sets is extremely fast! $O(\log n)$, just like maps, but sets do not have the `[]` operator, and you shouldn't use `[]` to access elements in a set.
- Like other containers, sets have the usual constructors as well as the `size` member function.

17.2 Set iterators

- Set iterators, similar to map iterators, are bidirectional: they allow you to step forward (`++`) and backward (`--`) through the set. Sets provide `begin()` and `end()` iterators to delimit the bounds of the set.
- Set iterators refer to const keys (as opposed to the pairs referred to by map iterators). For example, the following code outputs all strings in the set `words`:

```
for (set<string>::iterator p = words.begin(); p!= words.end(); ++p)
    cout << *p << endl;
```

17.3 Set insert

- There are two different versions of the `insert` member function. The first version inserts the entry into the set and returns a pair. The first component of the returned pair refers to the location in the set containing the entry. The second component is true if the entry wasn't already in the set and therefore was inserted. It is false otherwise. The second version also inserts the key if it is not already there. The iterator `pos` is a “hint” as to where to put it. This makes the insert faster if the hint is good.

```
pair<iterator,bool> set<Key>::insert(const Key& entry);
iterator set<Key>::insert(iterator pos, const Key& entry);
```

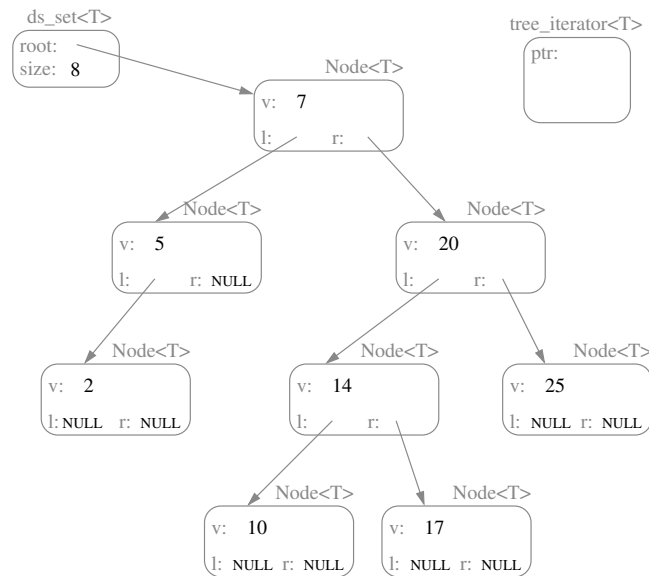
17.4 Set erase

- There are three versions of `erase`. The first `erase` returns the number of entries removed (either 0 or 1). The second and third erase functions are just like the corresponding erase functions for maps. Note that the `erase` functions do not return iterators. This is different from the `vector` and `list` erase functions.

```
size_type set<Key>::erase(const Key& x);
void set<Key>::erase(iterator p);
void set<Key>::erase(iterator first, iterator last);
```


17.9 ds_set: Class Overview

- There is two auxiliary classes, `TreeNode` and `tree_iterator`. All three classes are templated.
- The only member variables of the `ds_set` class are the root and the size (number of tree nodes).
- The iterator class is declared internally, and is effectively a wrapper on the `TreeNode` pointers.
 - Note that `operator*` returns a `const` reference because the keys can't change.
 - The increment and decrement operators are missing (we'll fill this in next week in lecture!).
- The main public member functions just call a private (and often recursive) member function (passing the root node) that does all of the work.
- Because the class stores and manages dynamically allocated memory, a copy constructor, `operator=`, and destructor must be provided.



17.10 Exercises

1. Provide the implementation of the member function `ds_set<T>::begin`. This is essentially the problem of finding the node in the tree that stores the smallest value.

2. Write a recursive version of the function `find`.

17.11 In-order, Pre-Order, Post-Order Traversal

- One of the fundamental tree operations is “traversing” the nodes in the tree and doing something at each node. The “doing something”, which is often just printing, is referred to generically as “visiting” the node.
- There are three general orders in which binary trees are traversed: pre-order, in-order and post-order.
- In order to explain these, let’s first draw an “exactly balanced” binary search tree with the elements 1-7:

– What is the *in-order traversal* of this tree? Hint: it is monotonically increasing, which is always true for an in-order traversal of a binary search tree!

– What is the *post-order traversal* of this tree? Hint, it ends with “4” and the 3rd element printed is “2”.

– What is the *pre-order traversal* of this tree? Hint, the last element is the same as the last element of the in-order traversal (but that is not true in general! why not?)

```

// Partial implementation of binary-tree based set class similar to std::set.
// The iterator increment & decrement operations have been omitted.
#ifndef ds_set_h_
#define ds_set_h_
#include <iostream>
#include <utility>

// -----
// TREE NODE CLASS
template <class T>
class TreeNode {
public:
    TreeNode() : left(NULL), right(NULL) {}
    TreeNode(const T& init) : value(init), left(NULL), right(NULL) {}
    T value;
    TreeNode* left;
    TreeNode* right;
};

template <class T> class ds_set;

// -----
// TREE NODE ITERATOR CLASS
template <class T>
class tree_iterator {
public:
    tree_iterator() : ptr_(NULL) {}
    tree_iterator(TreeNode<T>* p) : ptr_(p) {}
    tree_iterator(const tree_iterator& old) : ptr_(old.ptr_) {}
    ~tree_iterator() {}
    tree_iterator& operator=(const tree_iterator& old) { ptr_ = old.ptr_; return *this; }
    // operator* gives constant access to the value at the pointer
    const T& operator*() const { return ptr_->value; }
    // comparison operators are straightforward
    bool operator==(const tree_iterator& r) { return ptr_ == r.ptr_; }
    bool operator!=(const tree_iterator& r) { return ptr_ != r.ptr_; }
    // increment & decrement will be discussed in Lecture 18 and Lab 11

private:
    // representation
    TreeNode<T>* ptr_;
};

// -----
// DS SET CLASS
template <class T>
class ds_set {
public:
    ds_set() : root_(NULL), size_(0) {}
    ds_set(const ds_set<T>& old) : size_(old.size_) {
        root_ = this->copy_tree(old.root_); }
    ~ds_set() { this->destroy_tree(root_); root_ = NULL; }
    ds_set& operator=(const ds_set<T>& old) {
        if (&old != this) {
            this->destroy_tree(root_);
            root_ = this->copy_tree(old.root_);
            size_ = old.size_;
        }
        return *this;
    }

    typedef tree_iterator<T> iterator;

    int size() const { return size_; }
    bool operator==(const ds_set<T>& old) const { return (old.root_ == this->root_); }

```

```

// FIND, INSERT & ERASE
iterator find(const T& key_value) { return find(key_value, root_); }
std::pair< iterator, bool > insert(T const& key_value) { return insert(key_value, root_); }
int erase(T const& key_value) { return erase(key_value, root_); }

// OUTPUT & PRINTING
friend std::ostream& operator<< (std::ostream& ostr, const ds_set<T>& s) {
    s.print_in_order(ostr, s.root_);
    return ostr;
}
void print_as_sideways_tree(std::ostream& ostr) const { print_as_sideways_tree(ostr, root_, 0); }

// ITERATORS
iterator begin() const {
    // Implemented in Lecture 17

}
iterator end() const { return iterator(NULL); }

private:
// REPRESENTATION
TreeNode<T>* root_;
int size_;

// PRIVATE HELPER FUNCTIONS
TreeNode<T>* copy_tree(TreeNode<T>* old_root) { /* Implemented in Lab 9 */ }
void destroy_tree(TreeNode<T>* p) { /* Implemented in Lecture 18 */ }

iterator find(const T& key_value, TreeNode<T>* p) {
    // Implemented in Lecture 17

}

std::pair<iterator,bool> insert(const T& key_value, TreeNode<T>*& p) { /* Discussed in Lecture 18 */ }
int erase(T const& key_value, TreeNode<T>* &p) { /* Implemented in Lecture 19 */ }

void print_in_order(std::ostream& ostr, const TreeNode<T>* p) const {
    // Discussed in Lecture 18
    if (p) {
        print_in_order(ostr, p->left);
        ostr << p->value << "\n";
        print_in_order(ostr, p->right);
    }
}

void print_as_sideways_tree(std::ostream& ostr, const TreeNode<T>* p, int depth) const {
    /* Discussed in Lecture 17 */ }
};

#endif

```