## Homework 1

## Submission

Submit your individual solution at the beginning of the class on Monday, September 11.

## Problems

1. Prove by induction that the number of vertices in a binary tree of height n is at most $2^{n+1}-1$.
2. Problem 18 on page 14.
3. Problem 2 on page 26.
4. Show that for languages $L_{1}, L_{2}, L_{3}$, if $w \in L_{1}\left(L_{2} \cap L_{3}\right)$, then $w \in L_{1} L_{2} \cap L_{1} L_{3}$. Find $L_{1}, L_{2}, L_{3}$ such that there is a $w: w \in L_{1} L_{2} \cap L_{1} L_{3}$ and $w \notin L_{1}\left(L_{2} \cap L_{3}\right)$.
5. Problem 2 on page 47.

## Good luck!

