

Belief Networks

Artificial Intelligence: A Modern Approach
by Russell & Norvig
Chapter 15, 19

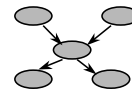
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Belief Network (Bayesian Network)

A graph which represents the dependence
between variables



Bayes' rule:

$$P(B/A) = P(A/B) P(B) / P(A)$$

$$P(B/A) = (0.5 * 1/50000) / (1/20) = 0.0002$$

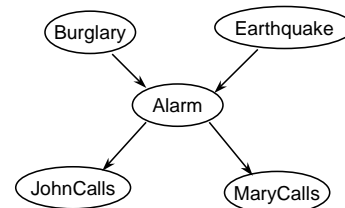
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Properties of Belief Nets

- 1) A set of random variables make up the nodes of the network
- 2) A set of direct links or arrows connect pairs of nodes. An arrow from node X to node Y means that X has a direct influence on Y
- 3) Each node has a conditional probability table that quantifies the effects that the parents have on the node
- 4) The graph has no directed cycles

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Example



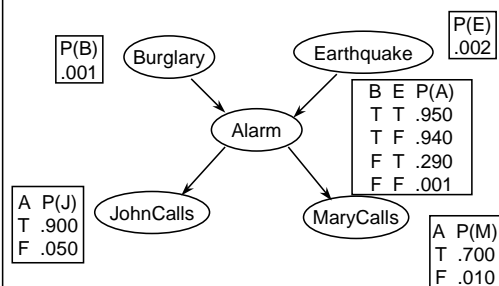
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Example

Burglary	Quake	P(Alarm Burglary, Quake)	
		True	False
True	True	0.950	0.050
True	False	0.940	0.060
False	True	0.290	0.710
False	False	0.001	0.999

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Example



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Derivative-Free Optimization

Example - using the network

$P(x_1, \dots, x_n) = \sum P(x_i | \text{Parents}(x_i))$ for all i

Probability that alarm sounded, but neither a burglary nor an earthquake has occurred, and both John and Mary call.

$$P(J \wedge M \wedge A \wedge \text{not } B \wedge \text{not } E)$$

$$= P(J|A) P(M|A) P(A|\text{not } B \wedge \text{not } E) P(\text{not } B) P(\text{not } E)$$

$$= 0.90 * 0.70 * 0.001 * 0.999 * 0.998$$

$$= 0.00062$$

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Derivative-Free Optimization

Creating a belief net

Each node must be conditionally independent from its predecessors

$$P(X_i | x_{1-1}, \dots, x_i) = P(X_i | \text{Parents}(x_i))$$

The parents of node x_i should only be the nodes that directly influence it

$$P(M|J, A, B, E) = P(M|A)$$

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Derivative-Free Optimization

Network Construction

- 1) Choose the set of relevant variables, X_i
- 2) Choose an ordering for the variables
- 3) While there are variables left:
 - a) Pick a variable X_i and add a node to the network for it.
 - b) Set $\text{Parents}(X_i)$ to some minimal set of nodes already in the net such that it is conditionally independent from all nodes not in $\text{Parents}(X_i)$
 - c) Define the conditional probability table for X_i

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Derivative-Free Optimization

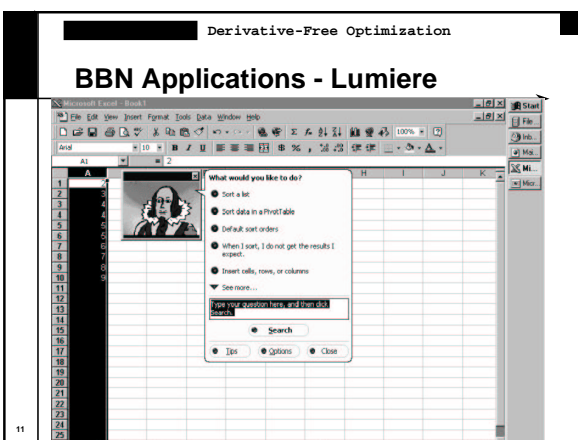
Applications of BBN

GE Power Systems - Diagnosing Power Generators
 GE Transportation - Diagnosing Trains
 Kana - E-mail handling
 Microsoft - Office Assistant

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Derivative-Free Optimization

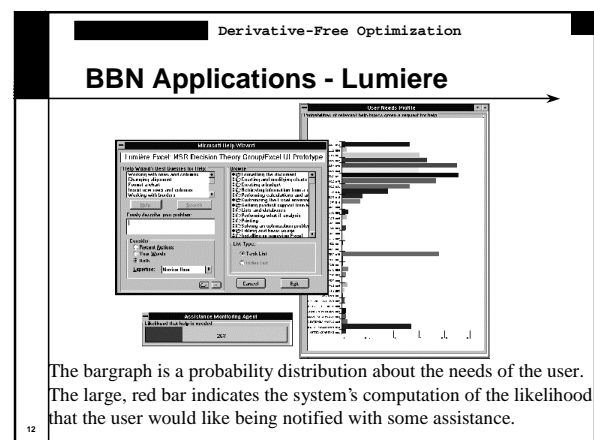
BBN Applications - Lumiere



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Derivative-Free Optimization

BBN Applications - Lumiere



The bargraph is a probability distribution about the needs of the user. The large, red bar indicates the system's computation of the likelihood that the user would like being notified with some assistance.

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Derivative-Free Optimization



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Derivative-Free Optimization

BBN Tools

GeNie - Graphical Network Interface (Pittsburg CMU)
http://www2.sis.pitt.edu/~genie/about_genie.html

Netica - Norsys Software Corporation
<http://www.norsys.com/>

Microsoft Belief Network - Microsoft
<http://www.research.microsoft.com/research/dtg/msbn/default.htm>

matlab - University of California

<http://www.cs.berkeley.edu/~murphyk/Bayes/bnt.html>

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Derivative-Free Optimization

Locomotive Cooling System Belief Network

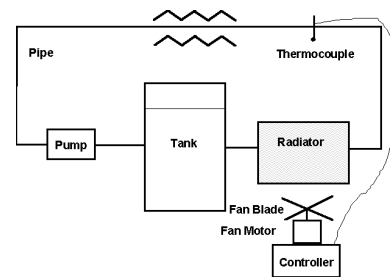
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<http://snook.crd.ge.com/coe/conclusi.htm>

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Derivative-Free Optimization

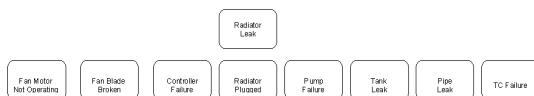
Simplified Model of a Locomotive Cooling System



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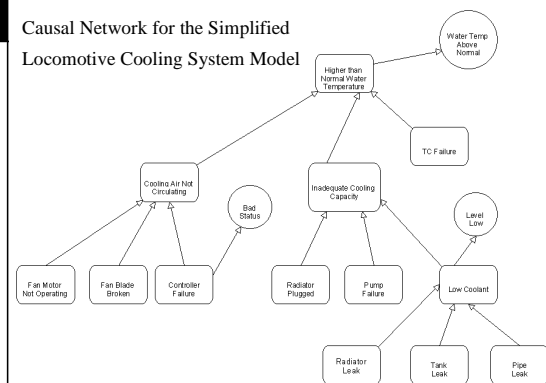
Derivative-Free Optimization

Locomotive Cooling System Model Failure Modes



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Derivative-Free Optimization

Causal Network for the Simplified
Locomotive Cooling System Model

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