

Voxels & Collisions

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Last Time?

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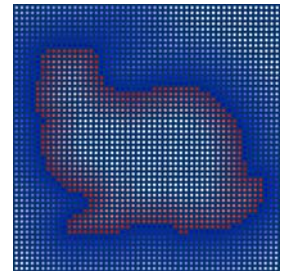
Today

- **Implicit Surfaces**
- **Voxels**
- Collisions
- Implicit Integration

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Implicit Surfaces

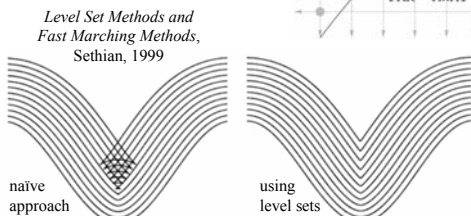
- For a sphere:
 $H(x,y,z) = x^2 + y^2 + z^2 - r^2$
- If $H(x,y,z) = 0$,
on surface
- If $H(x,y,z) > 0$,
outside surface
- If $H(x,y,z) < 0$,
inside surface



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Level Sets

- Efficient method for computing signed distance field

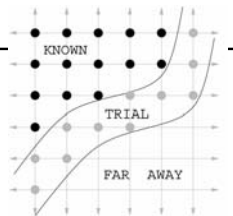


Level Set Methods and Fast Marching Methods,
Sethian, 1999

naïve approach

using level sets

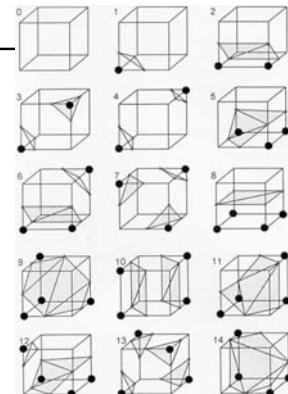
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Marching Cubes

- Polygonization:
extract triangle mesh from signed distance field

"Marching Cubes: A High Resolution 3D Surface Construction Algorithm",
Lorensen and Cline, SIGGRAPH '87.

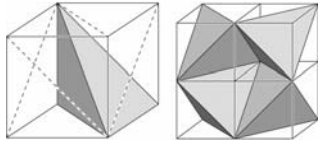


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“Marching Tetrahedra”



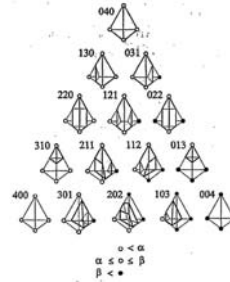
Jules Bloomenthal
“An implicit surface polygonizer”
Graphics Gems IV



“When the Blobs Go
Marching Two by Two”,
Jeff Lander, Gamasutra

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“Marching Tetrahedra”



Similarly, we can create
volumetric models:



“Interval volume tetrahedrization”
Visualization '97
Nielsen & Sung

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Questions?

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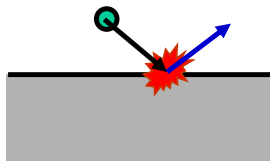
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Collisions

- Detection
- Response
- Overshooting problem
(when we enter the solid)



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Detecting Collisions

- Easy with implicit equations of surfaces
- $H(x,y,z)=0$ at surface
- $H(x,y,z)<0$ inside surface
- So just compute H and you know that you're inside if it's negative

- More complex with other surface definitions

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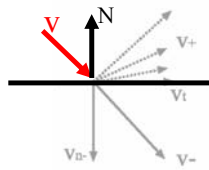
Collision Response

- tangential velocity v_t unchanged
- normal velocity v_n reflects:

$$v = v_t + v_n$$

$$v \leftarrow v_t - \epsilon v_n$$

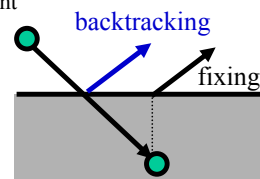
- coefficient of restitution (1 for elastic, 0 for plastic)
- change of velocity = $-(1+\epsilon)v$
- change of momentum *Impulse* = $-m(1+\epsilon)v$



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Collisions - Overshooting

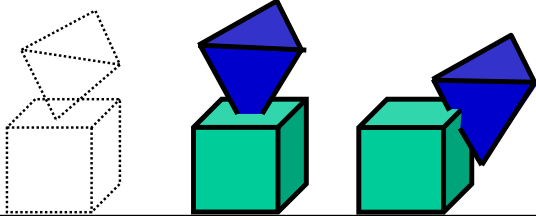
- Usually, we detect collision when it's too late: we're already inside
- Solutions: back up
 - Compute intersection point
 - Compute response there
 - Advance for remaining fractional time step
- Other solution: Quick and dirty fixup
 - Just project back to object closest point



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Collision Detection for Solids

- How to detect collision between 2 polyhedra?
- Need an inside/outside test
- Test if a vertex is inside the other polyhedron
- But treat also edge-edge intersection



Cost of Detection?

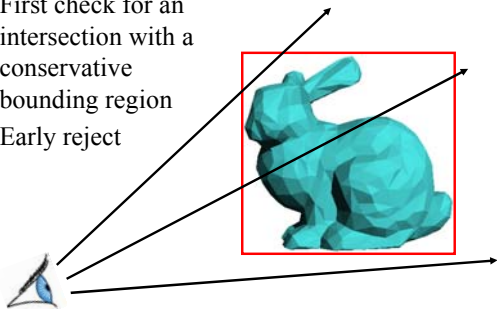
- Test each edge with each face?
 - $O(N^2)$
- How would you detect collision between two bunnies?
 - $O(N^2)$ is too expensive!
 - Use spatial hierarchy



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Conservative Bounding Region

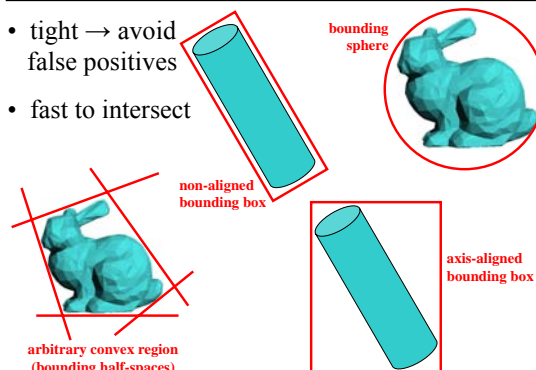
- First check for an intersection with a conservative bounding region
- Early reject



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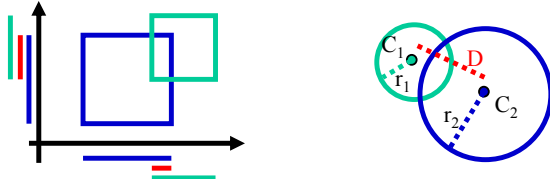
Conservative Bounding Regions

- tight \rightarrow avoid false positives
- fast to intersect



Overlap test

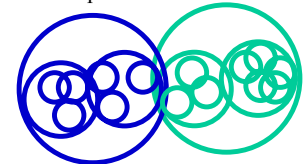
- Overlap between two axis-aligned boxes?
 - Check if the intervals along the 3 dimensions overlap
- Overlap test between two spheres?
 - $D(\text{center}_1, \text{center}_2) < r_1 + r_2$



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General Collision Detection

- Put a hierarchy around your objects
- Use the fast overlap test recursively
- Handle exact case at the leaves (when necessary)
- More difficult for self-collision (e.g. cloth)
 - Because there is more overlap



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Reduced Deformation

Doug L. James & Dinesh K. Pai
BD-Tree: Output-Sensitive Collision Detection for Reduced Deformable Models
 SIGGRAPH 2004

- Collisions are expensive
- Deformation is expensive
- This is a lot of geometry!
- Simplify the simulation model

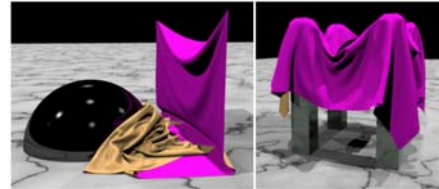


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Cloth Collision

Robert Bridson, Ronald Fedkiw & John Anderson
Robust Treatment of Collisions, Contact and Friction for Cloth Animation
 SIGGRAPH 2002

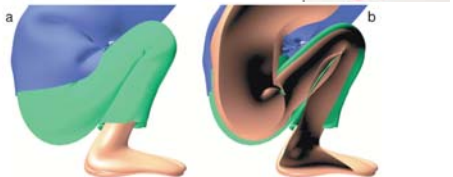
- A cloth has many points of contact
- Stays in contact
- Requires
 - Efficient collision detection
 - Efficient numerical treatment (stability)



Cloth Collision Challenges

- Detecting and resolving prior unavoidable intersections

Baraff, Witkin & Kass,
Untangling Cloth,
 SIGGRAPH 2003



Questions?

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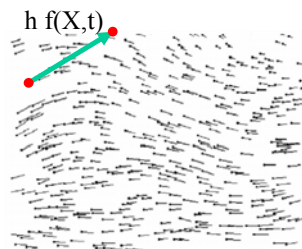
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Euler Integration

- Timestep h , move in the direction of $f(X, t)$



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Stiffness & Stability

- With an explicit/forward integration scheme:
$$\mathbf{y}_{k+1} = \mathbf{y}_k + h \mathbf{g}(\mathbf{y}_k)$$

we must use a very small timestep to simulate *stable, stiff* cloth.
- Alternatively we can use an implicit/backwards scheme:
$$\mathbf{y}_{k+1} = \mathbf{y}_k + h \mathbf{g}(\mathbf{y}_{k+1})$$

$$\mathbf{y}_k = \mathbf{y}_{k+1} - h \mathbf{g}(\mathbf{y}_{k+1})$$

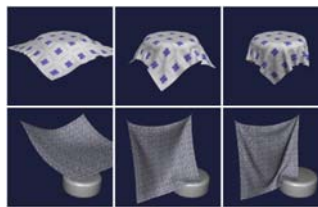
Solving one step is much more expensive (Newton's Method, Conjugate Gradients, ...) but overall faster than the thousands of explicit timesteps required for very stiff springs.

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Cloth

David Baraff & Andrew Witkin
Large Steps in Cloth Simulation
SIGGRAPH 1998

- Dynamic motion driven by animation



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