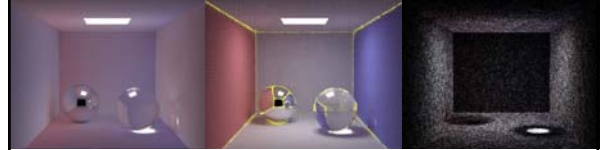
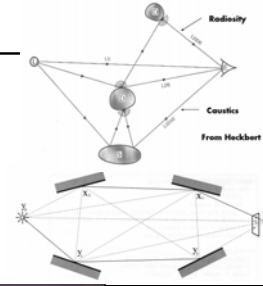


# Subsurface Scattering

## Last Time?

- Bi-Directional Path Tracing
- Irradiance Caching
- Photon Mapping
- Ray Grammar



## Today

- **Measuring BRDFs**
- 3D Digitizing & Scattering
- Fresnel Reflection
- Importance of Participating Media
- BSSRDFs
- Other Complex Materials

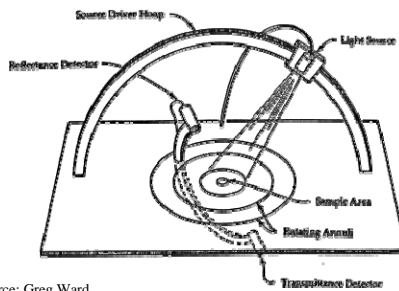
## BRDFs in the Movie Industry

- <http://www.virtualcinematography.org/publications/acrobat/BRDF-s2003.pdf>
- For the Matrix movies
- Agent Smith clothes are CG, with measured BRDF



## How Do We Obtain BRDFs?

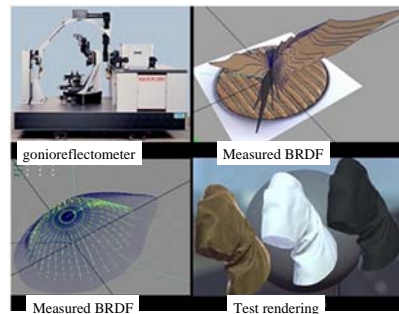
- Gonioreflectometer
  - 4 degrees of freedom



Source: Greg Ward

## BRDFs in the Movie Industry

- <http://www.virtualcinematography.org/publications/acrobat/BRDF-s2003.pdf>
- For the Matrix movies



## BRDFs in the Movie Industry



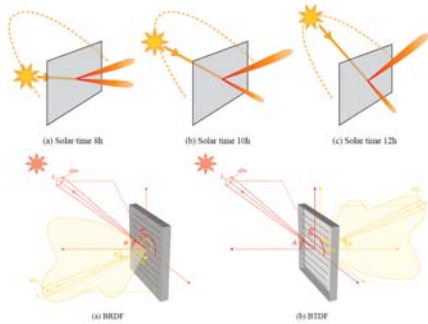
Photo CG Photo CG

## Not just a BRDF...



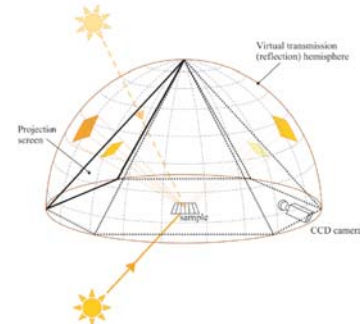
From presentation by  
J.P. Lewis and George Borshukov

## Materials – BRDF & BTDF



M. Andersen, "Innovative bi-directional video-goniophotometer for advanced fenestration systems", 2004.

## Measuring Materials



M. Andersen, "Innovative bi-directional video-goniophotometer for advanced fenestration systems", 2004.

## Today

- Measuring BRDFs
- **3D Digitizing & Scattering**
- Fresnel Reflection
- Importance of Participating Media
- BSSRDFs
- Other Complex Materials

## 3D Digitizing



Cyberware

*The Digital Michelangelo Project:  
3D Scanning of Large Statues,  
Levoy et al., SIGGRAPH 2000*

## Scattering & Scanning

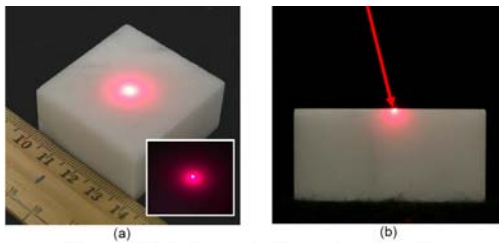


Figure 1: Diffusion in a sample of Carrara Statuario marble.

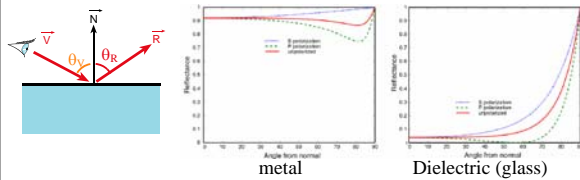
*An Assessment of Laser Range Measurement of Marble Surfaces*, Godin et al, 2001.

## Today

- Measuring BRDFs
- 3D Digitizing & Scattering
- **Fresnel Reflection**
- **Importance of Participating Media**
- BSSRDFs
- Other Complex Materials

## Amount of Reflection

- Traditional ray tracing (hack)
  - Constant **reflectionColor**
- More realistic:
  - Fresnel reflection term (more reflection at grazing angle)
  - Schlick's approximation:  $R(\theta) = R_0 + (1 - R_0)(1 - \cos \theta)^5$



## Dusty Surfaces & Retro-Reflection

- Viewed perpendicular to the surface, there is little scattering off dust
- At grazing angles, there is increased scattering with the dust making the surface appear brighter
- Similarly, the earth viewed from space appears brighter near the edges, because of increased scattering of the atmosphere.

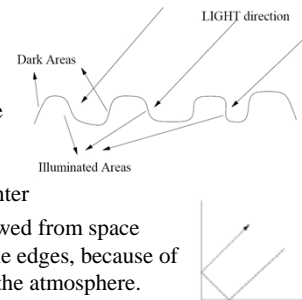
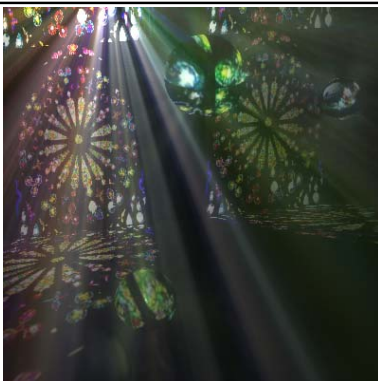


Figure 5: Showing retro-reflection from a very rough surface (left). Only areas with normals close to the light direction are well lit, so there is a strong retroreflective peak. On the right, we see a corner reflector (the inside corner of 3 planes is the 3D analog) which produces the same effect.

## Light Rays in a Dusty Room



Annie Ding, MIT  
6.837 Final Project  
December, 2004

## Participating Media

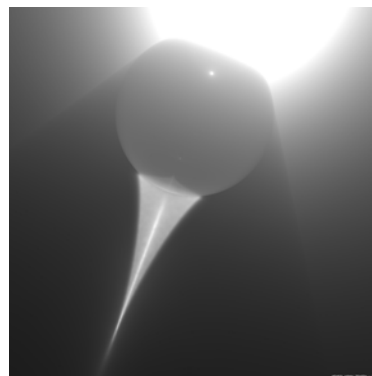


Image by Henrik  
Wann Jensen

## Today

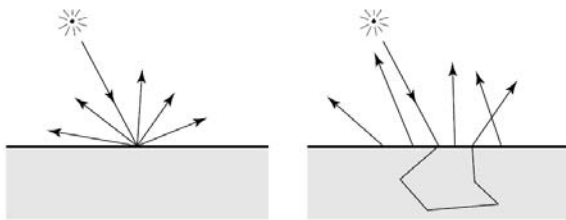
- Measuring BRDFs
- 3D Digitizing & Scattering
- Fresnel Reflection
- Importance of Participating Media
- **BSSRDFs**
- Other Complex Materials

## Reading For Today



*A Practical Model for Subsurface Light Transport*,  
Jensen, Marschner, Levoy, & Hanrahan, SIGGRAPH 2001

## BRDF vs. BSSRDF



Images from "A Practical Model for Subsurface Light Transport"  
Jensen, Marschner, Levoy, & Hanrahan SIGGRAPH 2001

## Subsurface Scattering Variables

Name	Symbol	Units	Description
Scattering Coeff.	$\sigma_s$	(length) <sup>-1</sup>	Probability of scattering per unit length
Absorption Coeff.	$\sigma_a$	(length) <sup>-1</sup>	Probability of absorption per unit length
Phase Function	$p(x, \vec{\omega}', \vec{\omega})$		Angular distribution of scattering
Extinction Coeff. (Scattering) Albedo	$\sigma_t$ $A$	(length) <sup>-1</sup>	$\sigma_s + \sigma_a$ $\frac{\sigma_s}{\sigma_t}$
Optical Depth	$\tau(0, d)$		$\int_0^d \sigma_t dx$
Transmittance	$t(0, d)$		$e^{-\tau(0, d)}$

- Albedo: first approximation of BDDF, % of light reflected off the surface
  - When the albedo = 1, no absorption occurs and light is only transmitted or scattered. This is an ok approximation for snow or clouds.

## Sampling a BSSRDF

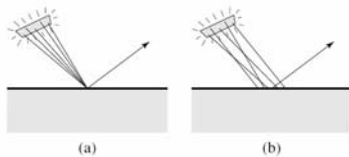
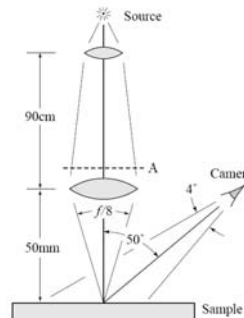


Figure 7: (a) Sampling a BRDF (traditional sampling), (b) sampling a BSSRDF (the sample points are distributed both over the surface as well as the light).

Images from "A Practical Model for Subsurface Light Transport"  
Jensen, Marschner, Levoy, & Hanrahan SIGGRAPH 2001

## BSSRDF Measurement



Images from "A Practical Model for Subsurface Light Transport"  
Jensen, Marschner, Levoy, & Hanrahan SIGGRAPH 2001

## Single Scattering

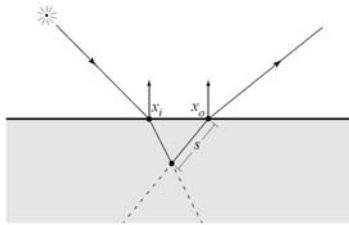


Figure 4: Single scattering occurs only when the refracted incoming and outgoing rays intersect, and is computed as an integral over path length  $s$  along the refracted outgoing ray.

Images from "A Practical Model for Subsurface Light Transport"  
Jensen, Marschner, Levoy, & Hanrahan SIGGRAPH 2001

## Dipole Approx. for Diffuse Scattering

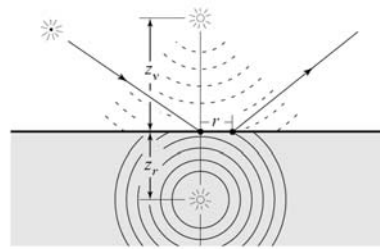


Figure 3: An incoming ray is transformed into a dipole source for the diffusion approximation.

Images from "A Practical Model for Subsurface Light Transport"  
Jensen, Marschner, Levoy, & Hanrahan SIGGRAPH 2001

## Today

- Measuring BRDFs
- 3D Digitizing & Scattering
- Fresnel Reflection
- Importance of Participating Media
- BSSRDFs
- **Other Complex Materials**

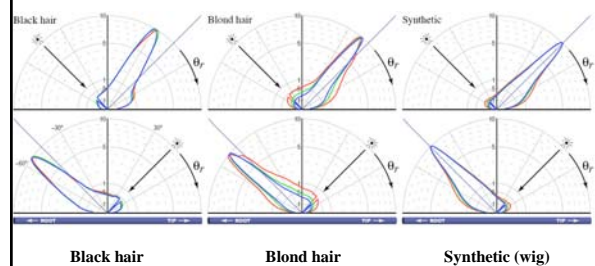


## Measuring BSSRDF by Dilution

"Acquiring Scattering Properties of Participating Media by Dilution"  
Narasimhan et al. SIGGRAPH 2006



## Measuring Hair



"Light Scattering from Human Hair Fibers"  
Marschner et al., SIGGRAPH 2003

## Rendering Hair

Old Method

New Method

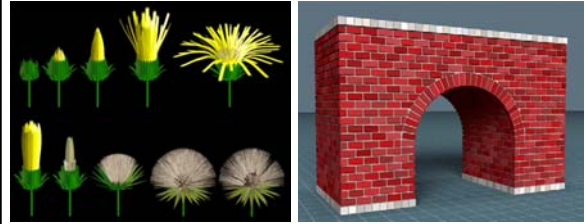
Photo



Figure 12: A comparison of Kajiyu and Kay's model (left) under a single point source, our proposed model (center) with the same lighting, and the hair from the photograph in Figure 11 (removed from context to simplify the comparison). The Kajiyu model's diffuse term results in a flat appearance, while the secondary highlight in our model correctly captures the colored shading of the real hair.

"Light Scattering from Human Hair Fibers"  
Marschner et al., SIGGRAPH 2003

## Readings For Friday



*Animation of Plant  
Development*  
Prusinkiewicz et al.,  
SIGGRAPH 1993

*Feature-Based Cellular Texturing  
for Architectural Models*  
Legakis et al.  
SIGGRAPH 2001