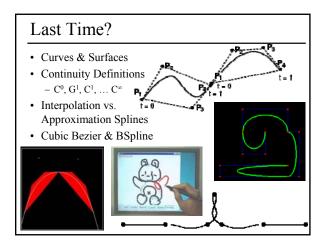
Subdivision Surfaces



Today

- Spline Surfaces / Patches
 - Tensor Product
 - Bilinear Patches
 - Bezier Patches
 - Trimming Curves
- Subdivision Surface "Zoo"
- · Seams In Subdivision
- Misc. Mesh/Surface Vocabulary
- "Piecewise Smooth Surface Reconstruction"

Tensor Product

· Of two vectors:

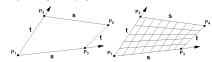
$$\begin{bmatrix} a_1 & a_2 & a_3 \end{bmatrix} \otimes \begin{bmatrix} b_1 & b_2 & b_3 & b_4 \end{bmatrix} = \begin{bmatrix} a_1b_1 & a_2b_1 & a_3b_1 \\ a_1b_2 & a_2b_2 & a_3b_2 \\ a_1b_3 & a_2b_3 & a_3b_3 \\ a_1b_4 & a_2b_4 & a_3b_4 \end{bmatrix}$$

 Similarly, we can define a surface as the tensor product of two curves....



Bilinear Patch

Bi-lerp a (typically non-planar) quadrilateral



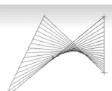
Notation: $\mathbf{L}(P_1, P_2, \alpha) \equiv (1 - \alpha)P_1 + \alpha P_2$

$$Q(s,t) = \mathbf{L}(\mathbf{L}(P_1,P_2,t),L(P_3,P_4,t),s)$$

Bilinear Patch

• Smooth version of quadrilateral with non-planar vertices...

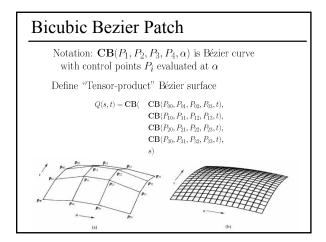


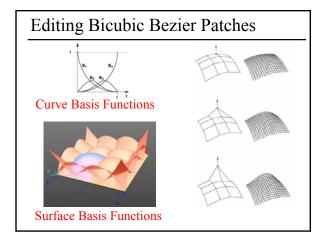


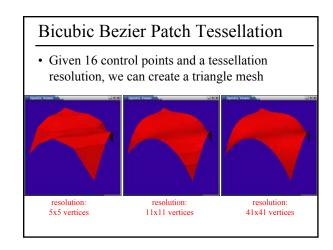
- But will this help us model smooth surfaces?
- Do we have control of the derivative at the edges?

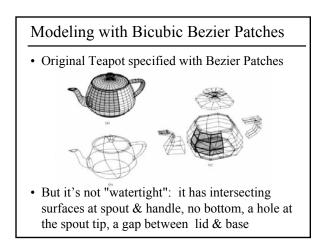
Today

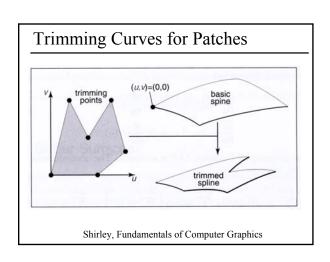
- Spline Surfaces / Patches
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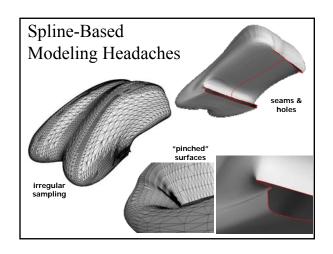


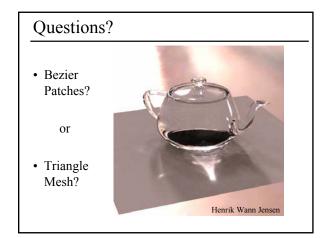






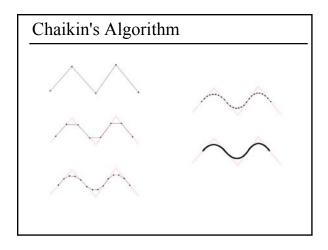


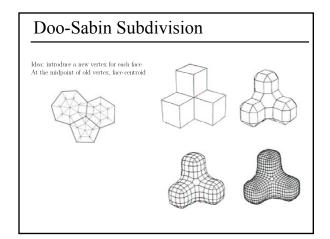


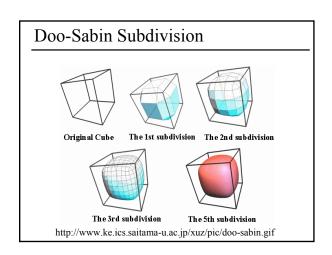


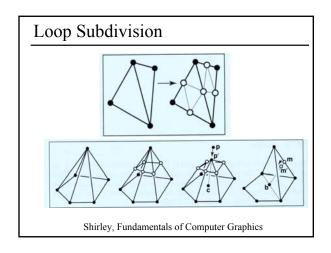
Today

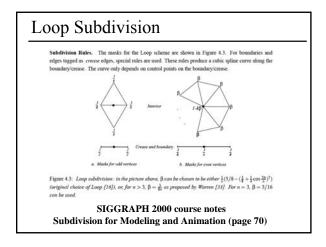
- Spline Surfaces / Patches
- Subdivision Surface "Zoo"
 - Doo Sabin (anything!)
 - Loop (triangles only)
 - Catmull Clark (turns everything into quads)
 - ... many others!
- Seams In Subdivision
- Misc. Mesh/Surface Vocabulary
- "Piecewise Smooth Surface Reconstruction"

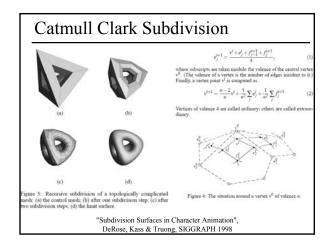


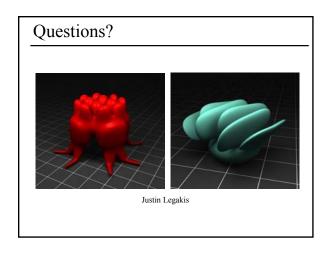






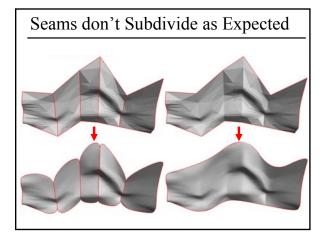






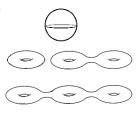
Today

- Spline Surfaces / Patches
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- "Piecewise Smooth Surface Reconstruction"



Misc. Mesh/Surface Vocabulary

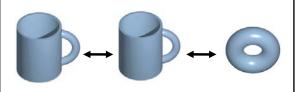
• Genus: The maximum number of disjoint simple closed curves which can be cut from an orientable surface of genus g without disconnecting it is g.





Misc. Mesh/Surface Vocabulary

 Homeomorphic/Topological equivalence: a continuous stretching and bending of the object into a new shape



http://en.wikipedia.org/wiki/Image:Mug_and_Torus_morph.git

Misc. Mesh/Surface Vocabulary

- · Dihedral Angle:
 - the angle between the planes of two triangular faces
 - "looking down the edge" between two faces, the angle between the faces.





Today

- Spline Surfaces / Patches
- Subdivision Surface "Zoo"
- · Seams In Subdivision
- Misc. Mesh/Surface Vocabulary
- "Piecewise Smooth Surface Reconstruction"

Reading for Today

• Hoppe et al., "Piecewise Smooth Surface Reconstruction" SIGGRAPH 1994









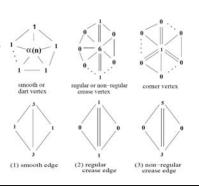
Piecewise Smooth Surface Reconstruction

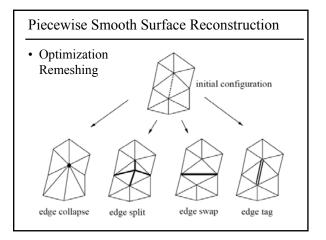
- From input: scanned mesh points
 - Estimate topological type (genus)
 - Mesh optimization (a.k.a. simplification)
 - Smooth surface optimization





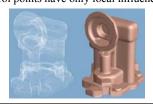
- Vertex & edge masks
- · Limit masks
- Position
 - Tangent





Piecewise Smooth Surface Reconstruction

- Crease subdivision masks *decouple* behavior of surface on either side of crease
- · Crease rules cannot model a cone
- Optimization can be done locally
 subdivision control points have only local influence
- Results
 - Noise?
 - Applicability?
 - Limitations?
 - Running Time



Reading for Tuesday (1/29)

 DeRose, Kass, & Truong, "Subdivision Surfaces in Character Animation", SIGGRAPH 1998



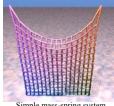
igure 5: Geri's hand as a piecewise smooth Catmull-Clark surface.

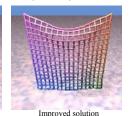
Infinitely sharp creases are used between the skin and the finger

 Post a comment or question on the LMS discussion by 10am on Tuesday 1/29

Reading for Friday (2/1)

 "Deformation Constraints in a Mass-Spring Model to Describe Rigid Cloth Behavior", Provot, 1995.



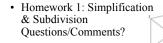


Simple mass-spring system

 Post a comment or question on the LMS discussion by 10am on Tuesday 1/29

Other...

- · Assigned readings & discussion
- · Anonymous homework discussion





- drand48/srand48 vs. rand/srand
- #include <Assert.h> vs. #include <cassert>

