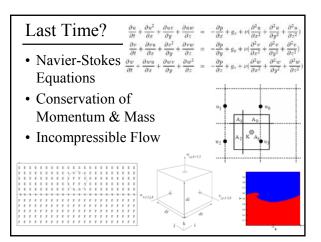
Inverse Kinematics



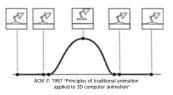
Today

- How do we animate?
 - Keyframing
 - Procedural Animation
 - Physically-Based Animation
 - Forward and Inverse Kinematics
 - Motion Capture
- Rigid Body Dynamics
- Finite Element Method



Keyframing

- Use spline curves to automate the in betweening
 - Good control
 - Less tedious than drawing every frame
- Creating a good animation still requires considerable skill and talent



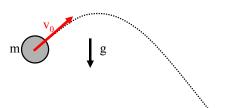
Procedural Animation

- Describes the motion algorithmically, as a function of small number of parameters
- Example: a clock with second, minute and hour hands
 - express the clock motions in terms of a "seconds" variable
 - the clock is animated by varying the seconds parameter
- Example: A bouncing ball
 - $\text{Abs}(\sin(\omega t + \theta_0)) * e^{-kt}$



Physically-Based Animation

- Assign physical properties to objects (masses, forces, inertial properties)
- Simulate physics by solving equations
- Realistic but difficult to control



Articulated Models

- · Articulated models:
 - rigid parts
 - connected by joints
- They can be animated by specifying the joint angles as functions of time.





Skeleton Hierarchy • Each bone transformation described relative X_h , Y_h , Z_h , q_h , f_h , s_h



1 DOF: knee

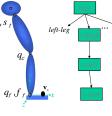
to the parent in



2 DOF: wrist



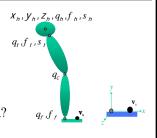




 $X_h, Y_h, Z_h, q_h, f_h, s_h$

Forward Kinematics

· Given skeleton parameters p, and the position of the effecter in local coordinates V_s, what is the position of the effector in the world coordinates V_w?

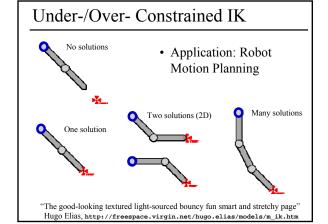


 $V_{w} = T(x_{h}, y_{h}, z_{h})R(q_{h}, f_{h}, s_{h})T_{h}R(q_{t}, f_{t}, s_{t})T_{t}R(q_{c})T_{c}R(q_{f}, f_{f})V_{s}$ $V_{w} = S(p)V_{s}$

Inverse Kinematics (IK)

- Given the position of the effecter in local coordinates V_s and the desired position $V_{\rm w}$ in world coordinates, what are the skeleton parameters p?
- Much harder requires solving the inverse of the non-linear function:

find p such that $S(p)V_s = V_w$



Searching Configuration Space pose space shaded by distance to target • Use gradient descent to walk from starting configuration to target • Angle restrictions & collisions can introduce local minima "The good-looking textured light-sourced bouncy fun smart and stretchy page" Hugo Elias, http://freespace.virgin.net/hugo.elias/models/m_ik2.htm

IK Challenge

- Find a "natural" skeleton configuration for a given collection of pose constraints
- A *vector constraint function C(p) = 0* collects all pose constraints
- A *scalar objective function* g(p) measures the quality of a pose, g(p) is minimum for most natural poses. Example g(p):
 - deviation from natural pose
 - joint stiffness
 - power consumption

Motion Capture

- Optical markers, high-speed cameras, triangulation
 - \rightarrow 3D position



• You must observe someone do something

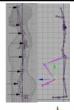






How do they Animate Movies/Games?

- · Keyframing mostly
- Articulated figures, inverse kinematics, motion capture
- Skinning
 - Complex deformable skin, muscle, skin motion
- Hierarchical controls
 - Smile control, eye blinking, etc.
 - Keyframes for these higher-level controls
- A huge time is spent building the 3D models, its skeleton and its controls
- · Physical simulation for secondary motion
 - Hair, cloth, water





Images from the Maya tutoria

Questions?

Reading for Today:

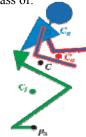
• "Synthesis of Complex Dynamic Character Motion from Simple Animation", Liu & Popović, 2002.



- Rapid prototyping of realistic character motion from rough low-quality animations
- Obey the laws of physics & stay within space of naturally-occurring movements

What's a Natural Pose?

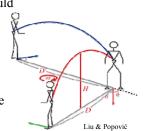
- Training database of ~50 "natural poses"
- For each, compute center of mass of:
 - Upper body
 - Arms
 - Lower body
- The relative COM of each generated pose is matched to most the most similar database example



Liu & Popović

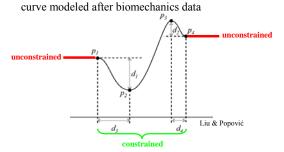
Linear and Angular Momentum

- In unconstrained animation (no contacts), both linear & angular momentum should be conserved
- · The center of mass should follow a parabolic trajectory according to gravity
- The joints should move such that the angular momentum of the whole body remains constant



During Constrained Motion

• During constrained motion (when in contact with the ground), the angular momentum follows a spline



System Features

- Automatically detect point/line/plane constraints
- · Divide animation into constrained portions (e.g., feet in contact with ground) and unconstrained portions (e.g., free flight)
- · Linear and angular momentum constraints without having to compute muscle forces
- · Minimize:
 - Mass displacement
 - Velocity of the degrees of freedom (DOF)
 - "Unbalance" (distance the COM projected to ground is outside of constraints)

Questions?

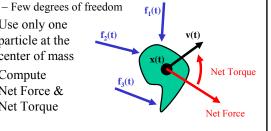
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Rigid Body Dynamics

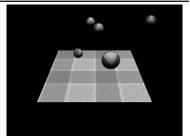
- Could use particles for all points on the object
 - But rigid body does not deform
- Use only one particle at the center of mass
- Compute Net Force & Net Torque



Nice Reference Material: http://www.pixar.com/companyinfo/research/pbm2001/

Rigid Body Dynamics

- Physics
 - Velocity
 - Acceleration
 - AngularMomentum
- · Collisions
- Friction

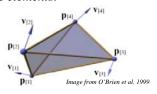


from: Darren Lewis http://www-cs-students.stanford.edu/~dalewis/cs448a/rigidbody.html

See also: http://www.myphysicslab.com/collision.html

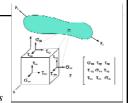
Simulation of Non-Rigid Objects

- We modeled string & cloth using mass-spring systems. Can we do the same?
- Yes...
- But a more physically accurate model uses *volumetric elements:*



Strain & Stress

- Stress
 - the internal distribution of forces within a body that balance and react to the loads applied to it
 - normal stress & shear stress



Strain

http://en.wikipedia.org/wiki/Image:Stress_tensor.png

- material deformation caused by stress.
- measured by the change in length of a line or by the change in angle between two lines

 $\varepsilon = \frac{\Delta_l}{l_0}$

Finite Element Method

- To solve the continuous problem (deformation of all points of the object)
 - Discretize the problem
 - Express the interrelationship
 - Solve a big linear system

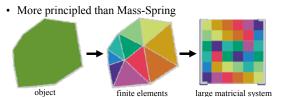
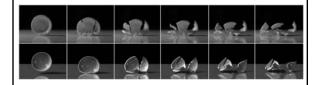


Diagram from Debunne et al. 2001

Reading for Friday 2/15:

• James O'Brien & Jessica Hodgins "Graphical Modeling and Animation of Brittle Fracture" SIGGRAPH 1999.



• Post a comment or question on the LMS discussion by 10am on Friday 2/15