Ray Tracing

Announcements: Quiz

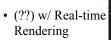
- On Tuesday (2/26), in class
- One 8.5x11 sheet of notes allowed
- Sample quiz (from last year) is posted online
- Mostly "reading comprehension" (?)
- Will be curved ©

Announcements: Final Projects

- Everyone should post one or more ideas for a final project on the discussion forum
- Connect with potential teammates (teams of 2 recommended)
- Start reading background papers
- Detailed proposal & summary of background research due March 20^{th}

Announcements: Summer Research

- Architectural Daylighting & Virtual Reality
 - w/ Yu Sheng & Me!
- · Biomedical Imaging
 - w/ Prof Badri Roysam (ECSE)



w/ Prof ShawnLawson (Arts)



Last Time?

- Rigid Body
- Finite Element Method
 - Stress/Strain
- Fracture
- Deformation
 - Level of Detail
 - Haptics



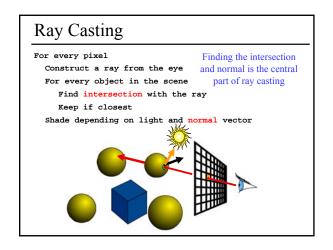


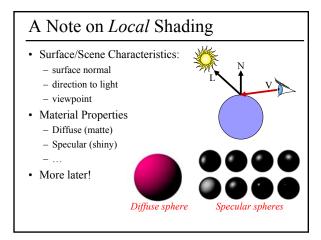


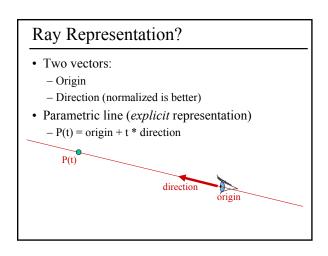
Today

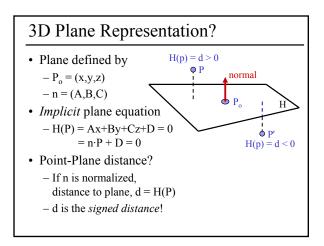
- Ray Casting
 - Ray-Plane Intersection
 - Ray-Sphere Intersection
 - Point in Polygon
- · Ray Tracing
- Recursive Ray Tracing
- Distribution Ray Tracing

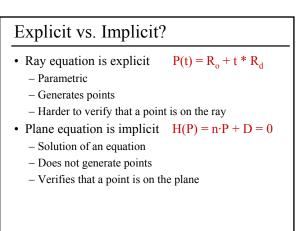
• Albrecht Durer, 16th century





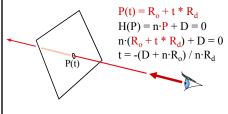






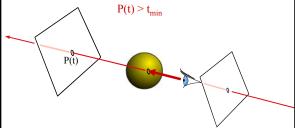
Ray-Plane Intersection

- Intersection means both are satisfied
- So, insert explicit equation of ray into implicit equation of plane & solve for t



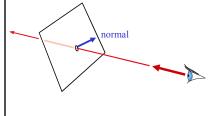
Additional Housekeeping

- Verify that intersection is closer than previous $P(t) < t_{current}$
- Verify that it is not out of range (behind eye)



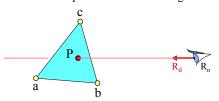
Normal

- For shading
 - diffuse: dot product between light and normal
- Normal is constant



Ray-Triangle Intersection

- Use barycentric coordinates:
 - $-P(\alpha, \beta, \gamma) = \alpha a + \beta b + \gamma c$ with $\alpha + \beta + \gamma = 1$
 - If $0 < \alpha < 1$ & $0 < \beta < 1$ & $0 < \gamma < 1$ then the point is inside the triangle!



How Do We Compute α , β , γ ?

- Ratio of opposite sub-triangle area to total area $-\alpha = A_a/A \qquad \beta = A_b/A \qquad \gamma = A_c/A$
- Use signed areas for points outside the triangle



Using Cramer's Rule...

• Used to solve for one variable at a time in system of equations

$$\beta = \frac{\begin{vmatrix} a_x - R_{ox} & a_x - c_x & R_{dx} \\ a_y - R_{oy} & a_y - c_y & R_{dy} \\ a_z - R_{oz} & a_z - c_z & R_{dz} \end{vmatrix}}{|A|} \qquad \gamma = \frac{\begin{vmatrix} a_x - b_x & a_x - R_{ox} & R_{dx} \\ a_y - b_y & a_y - R_{oy} & R_{dy} \\ a_z - b_z & a_z - R_{oz} & R_{dz} \end{vmatrix}}{|A|}$$

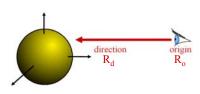
$$t = \frac{\begin{vmatrix} a_x - b_x & a_x - c_x & a_x - R_{ox} \\ a_y - b_y & a_y - c_y & a_y - R_{oy} \\ a_z - b_z & a_z - c_z & a_z - R_{oz} \end{vmatrix}}{|A|}$$

determinant

Can be copied mechanically into code

Sphere Representation?

- Implicit sphere equation
 - Assume centered at origin (easy to translate)
 - $-H(P) = P \cdot P r^2 = 0$



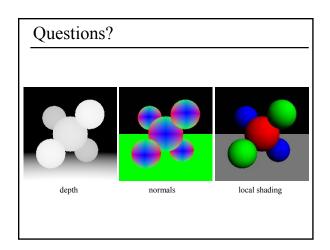
Ray-Sphere Intersection

• Insert explicit equation of ray into implicit equation of sphere & solve for t

$$\begin{split} P(t) &= R_o + t*R_d & H(P) = P \cdot P - r^2 = 0 \\ (R_o + tR_d) \cdot (R_o + tR_d) - r^2 = 0 \\ R_d \cdot R_d t^2 + 2R_d \cdot R_o t + R_o \cdot R_o - r^2 = 0 \\ \end{split}$$

Ray-Sphere Intersection

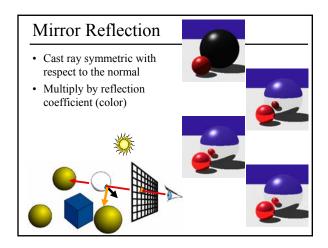
- Quadratic: $at^2 + bt + c = 0$
 - -a = 1 (remember, $||R_d|| = 1$)
 - $-b = 2R_d \cdot R_o$
 - $-c = R_o \cdot R_o r^2$
- with discriminant $d = \sqrt{b^2 4ac}$
- and solutions
- $t_{\pm} = \frac{-b \pm d}{2a}$
- What does it mean if there are no solutions, 1 solution, or 2 solutions?

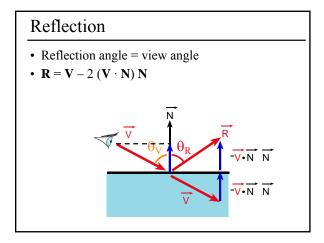


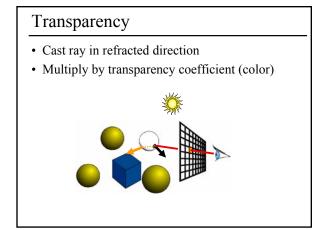
Today

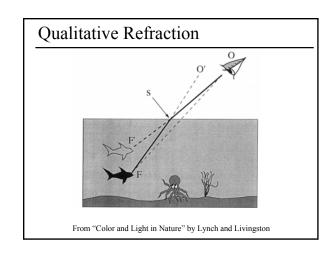
- Ray Casting
- Ray Tracing
 - Shadows
 - Reflection
 - Refraction
- Recursive Ray Tracing
- Distribution Ray Tracing

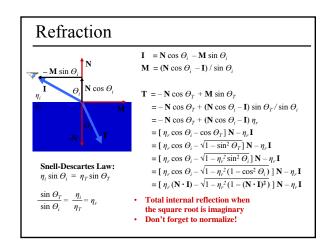
How Can We Add Shadows? Find the point to be shaded For every light, Construct ray from point to light For every object find intersection of ray with object If no objects between point and light Add contribution from light

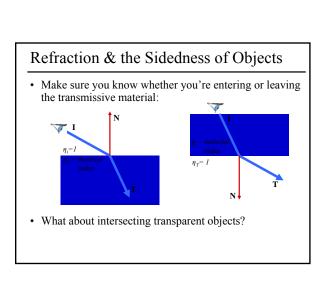


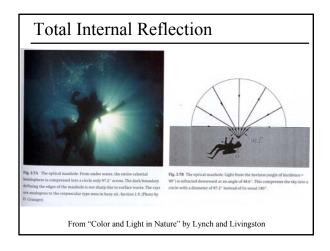


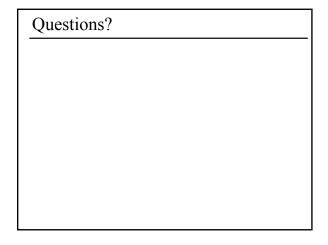










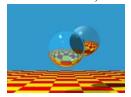


Today

- Ray Casting
- Ray Tracing
- Recursive Ray Tracing
- Distribution Ray Tracing

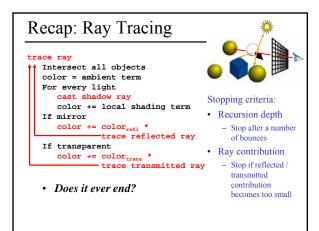
Reading for Today:

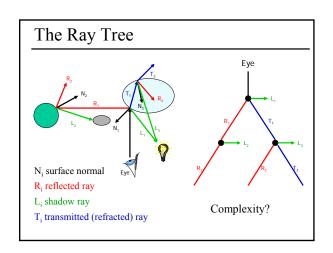
- "An improved illumination model for shaded display" Turner Whitted, 1980.
- ("Distributed Ray Tracing", Cook, Porter, & Carpenter, SIGGRAPH 1984.)

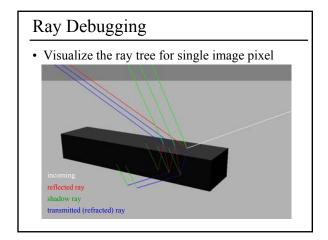




 Post a comment or question on the LMS discussion by 10am on Friday 2/22







Today

- Ray Casting
- Ray Tracing
- Recursive Ray Tracing
- Distribution Ray Tracing
 - Soft shadows
 - Antialiasing (getting rid of jaggies)
 - Glossy reflection
 - Motion blur
 - Depth of field (focus)

