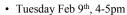
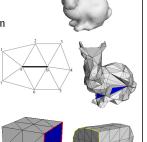
Subdivision Surfaces

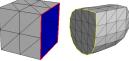
Misc...

- Homework 1: Simplification & Subdivision
 - Questions/Comments?



- Julie Dorsey
 Yale University
- "Studies in Sketch-Based Modeling"
- CII (LOW) 3051

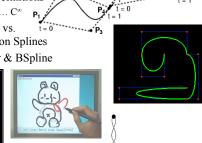




Last Time?

- · Curves & Surfaces
- Continuity Definitions - C⁰, G¹, C¹, ... C[∞] P₁
- Interpolation vs. t= Approximation Splines
- · Cubic Bezier & BSpline





Today

- Spline Surfaces / Patches
 - Tensor Product
 - Bilinear Patches
 - Bezier Patches
 - Trimming Curves
- Subdivision Surface "Zoo"
- · Seams In Subdivision
- Misc. Mesh/Surface Vocabulary
- "Subdivision Surfaces in Character Animation"

Tensor Product

• Of two vectors:

$$\begin{bmatrix} a_1 & a_2 & a_3 \end{bmatrix} \otimes \begin{bmatrix} b_1 & b_2 & b_3 & b_4 \end{bmatrix} = \begin{bmatrix} a_1b_1 & a_2b_1 & a_3b_1 \\ a_1b_2 & a_2b_2 & a_3b_2 \\ a_1b_3 & a_2b_3 & a_3b_3 \\ a_1b_4 & a_2b_4 & a_3b_4 \end{bmatrix}$$

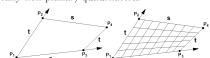
 Similarly, we can define a surface as the tensor product of two curves....



Computer Aided Geometric Design

Bilinear Patch

Bi-lerp a (typically non-planar) quadrilateral

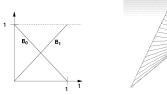


Notation: $\mathbf{L}(P_1, P_2, \alpha) \equiv (1 - \alpha)P_1 + \alpha P_2$

$$Q(s,t) = \mathbf{L}(\mathbf{L}(P_1, P_2, t), L(P_3, P_4, t), s)$$

Bilinear Patch

• Smooth version of quadrilateral with non-planar vertices...



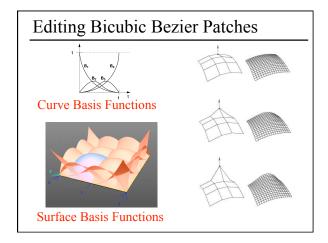
- But will this help us model smooth surfaces?
- Do we have control of the derivative at the edges?

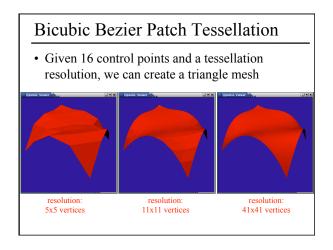
Ruled Surfaces in Art & Architecture http://www.bergenwood.no/wp-content/media/images/frozenmusic.jpg Chiras Iulia Astri Isabella Matiss Shteinerts Lonetyplanclimages com Antoni Gaudi Children's School Barcelona

Today

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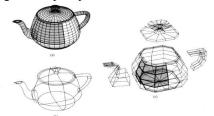
Notation: $CB(P_1, P_2, P_3, P_4, \alpha)$ is Bézier curve with control points P_i evaluated at α Define "Tensor-product" Bézier surface $Q(s,t) = CB(\quad CB(P_{00}, P_{01}, P_{02}, P_{03}, t), \quad CB(P_{10}, P_{11}, P_{12}, P_{13}, t), \quad CB(P_{20}, P_{21}, P_{22}, P_{23}, t), \quad CB(P_{30}, P_{31}, P_{32}, P_{33}, t),$ s)



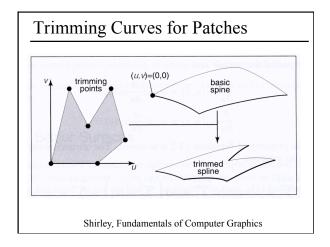


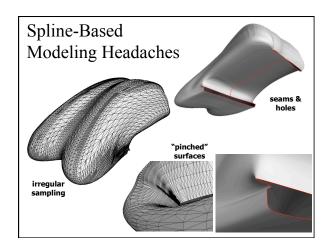
Modeling with Bicubic Bezier Patches

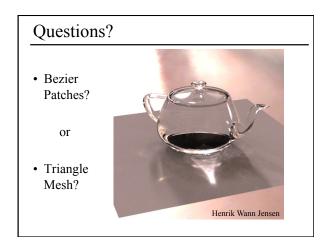
• Original Teapot specified with Bezier Patches



• But it's not "watertight": it has intersecting surfaces at spout & handle, no bottom, a hole at the spout tip, a gap between lid & base

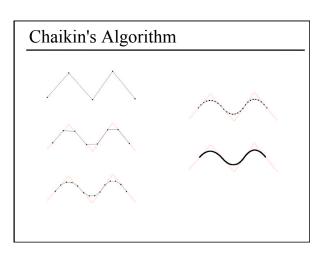


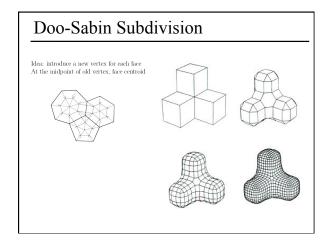


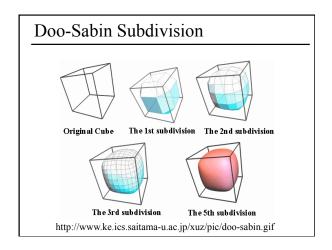


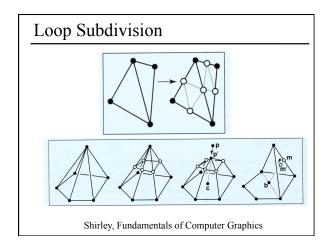
Today

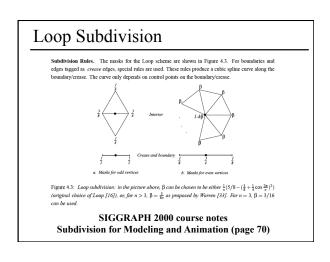
- Spline Surfaces / Patches
- Subdivision Surface "Zoo"
 - Doo Sabin (anything!)
 - Loop (triangles only)
 - Catmull Clark (turns everything into quads)
 - ... many others!
- Seams In Subdivision
- Misc. Mesh/Surface Vocabulary
- "Subdivision Surfaces in Character Animation"

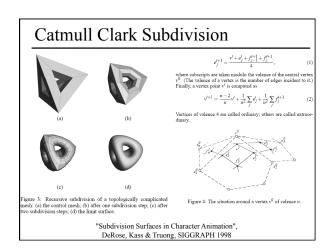


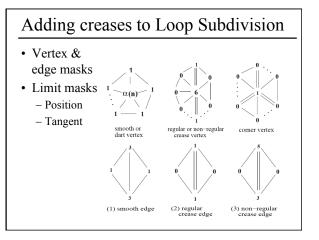




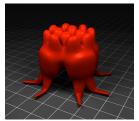


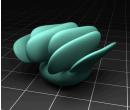






Questions?



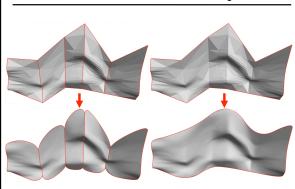


Justin Legakis

Today

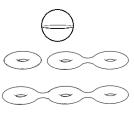
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Seams don't Subdivide as Expected



Misc. Mesh/Surface Vocabulary

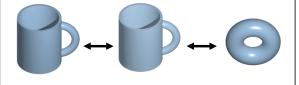
• Genus: The maximum number of disjoint simple closed curves which can be cut from an orientable surface of genus g without disconnecting it is g.





Misc. Mesh/Surface Vocabulary

• Homeomorphic/Topological equivalence: a continuous stretching and bending of the object into a new shape



 $http://en.wikipedia.org/wiki/Image:Mug_and_Torus_morph.gif$

Misc. Mesh/Surface Vocabulary

- Dihedral Angle:
 - the angle between the planes of two triangular faces
 - "looking down the edge" between two faces, the angle between the faces.

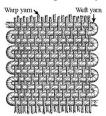




• Valence (a.k.a. degree): the number of edges incident to the vertex.

Misc. Mesh/Surface Vocabulary

• *Warp & weft:* Yarns used in weaving. Because the weft does not have to be stretched in the way that the warp is, it can generally be less strong.



http://en.wikipedia.org/wiki/Weft

Today

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Reading for Today

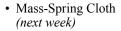
• DeRose, Kass, & Truong, "Subdivision Surfaces in Character Animation", SIGGRAPH 1998



Figure 5: Geri's hand as a piecewise smooth Catmull-Clark surface Infinitely sharp creases are used between the skin and the finger pails.

Subdivision Surfaces in Character Animation

- Catmull Clark Subdivision Rules
- Semi-sharp vs. Infinitely-sharp creases



- Hierarchical Mesh for Collision
- Texturing Subdivision Surfaces









Figure 11: (a) A texture mapped regular pentagon comprised of 5 triangles; (b) the pentagonal model with its vertices moved; (c A subdivision surface whose control mesh is the same 5 triangles in (a), and where boundary edges are marked as creases; (d) the

Catmull-Clark in Pixar Production

- Based on quadrilaterals
 - Like NURBS, specifically cubic bsplines
 - Implicit adjacency in subdivided microgeometry
 - Better than triangles for symmetric objects











Readings for Tuesday (pick one)

 Hoppe et al., "Piecewise Smooth Surface Reconstruction" SIGGRAPH 1994

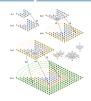






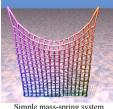


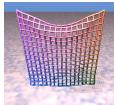
- Shiue, Jones, and Peters,
 "A Realtime GPU Subdivision Kernel", SIGGRAPH 2005
- Post a comment or question on the LMS discussion by 10am on Tuesday



Reading for Friday

• "Deformation Constraints in a Mass-Spring Model to Describe Rigid Cloth Behavior", Provot, 1995.





Improved solution

• Post a comment or question on the LMS discussion by 10am on Friday