CSCI-4530/6530 Advanced Computer Graphics

http://www.cs.rpi.edu/~cutler/classes/advancedgraphics/S17/

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1

Luxo Jr.



Pixar Animation Studios, 1986

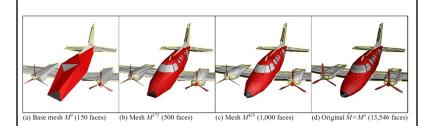
2

Topics for the Semester

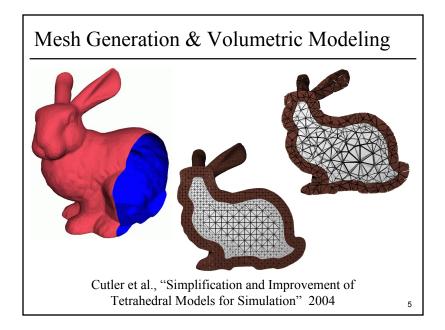
- Meshes
 - representation
 - simplification
 - subdivision surfaces
 - construction/generation
 - volumetric modeling
- Simulation
 - particle systems, cloth
 - rigid body, deformation
 - wind/water flows
 - collision detection
 - weathering

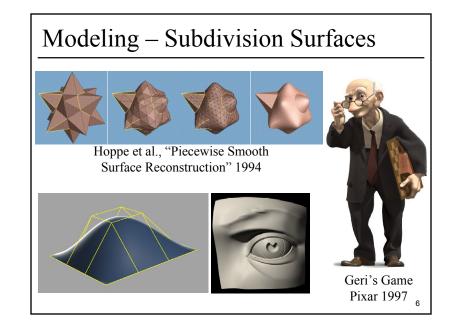
- Rendering
 - ray tracing, shadows
 - appearance models
 - local vs. global illumination
 - radiosity, photon mapping, subsurface scattering, etc.
- procedural modeling
- · texture synthesis
- non-photorealistic rendering
- hardware & more ...

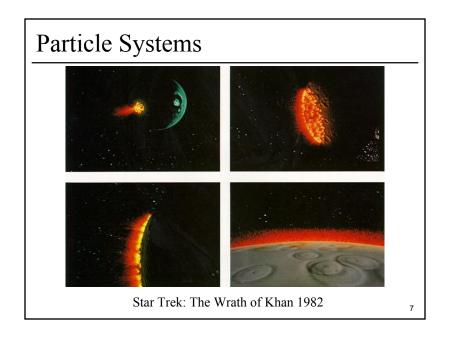
Mesh Simplification

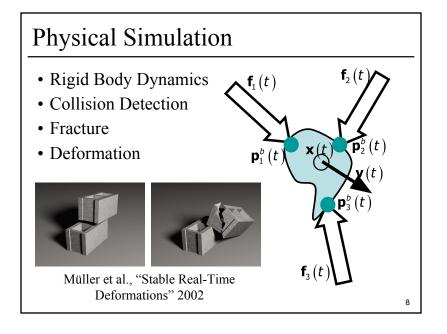


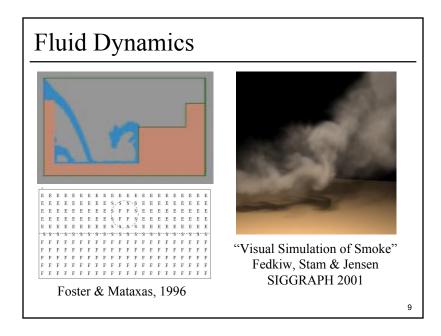
Hoppe "Progressive Meshes" SIGGRAPH 1996

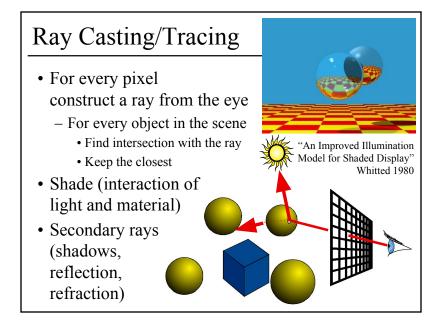


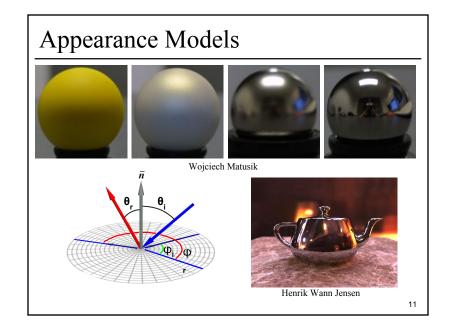


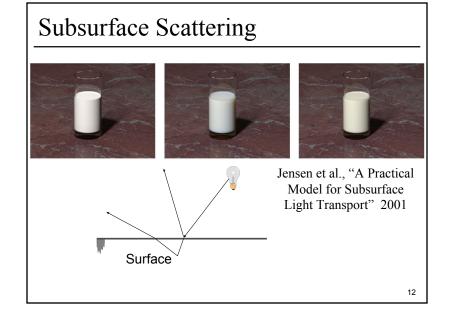












Syllabus & Course Website

http://www.cs.rpi.edu/~cutler/classes/advancedgraphics/S17/

• Which version should I register for?

- CSCI 6530 : 3 units of graduate credit

- CSCI 4530 : 4 units of undergraduate credit

(same lectures, assignments, quizzes, & grading criteria)

• This is an intensive course aimed at graduate students and undergraduates interested in graphics research, involving significant reading & programming each week. Taking this course in a 5 course overload semester is discouraged.

13

Grades

http://www.cs.rpi.edu/~cutler/classes/advancedgraphics/S17/

- This course counts as "communications intensive" for undergraduates. As such, you must satisfactorily complete all readings, presentations, project reports to pass the course.
- As this is an elective (not required) course, I expect to grade this course: "A", "A-", "B+", "B", "B-", or "F"
 - Don't expect C or D level work to "pass"
 - I don't want to give any "F"s

14

Participation/Laptops in Class Policy

http://www.cs.rpi.edu/~cutler/classes/advancedgraphics/S17/

- Lecture is intended to be discussion-intensive
- Laptops, tablet computers, smart phones, and other internet-connected devices are not allowed
 - Except during the discussion of the day's assigned paper: students may use their laptop/tablet to view an electronic version of the paper
 - Other exceptions to this policy are negotiable; please see the instructor in office hours

Questions?

Outline

- Course Overview
- Classes of Transformations
- Representing Transformations
- Combining Transformations
- Orthographic & Perspective Projections
- Example: Iterated Function Systems (IFS)

17

What is a Transformation?

 Maps points (x, y) in one coordinate system to points (x', y') in another coordinate system

$$x' = ax + by + c$$

$$y' = dx + ey + f$$

• For example, Iterated Function System (IFS):





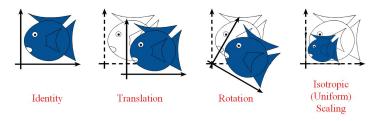






18

Simple Transformations



Yes, except scale = 0

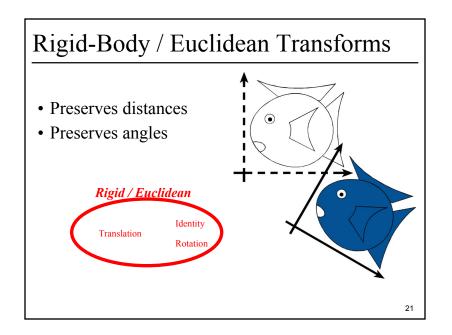
Transformations are used to:

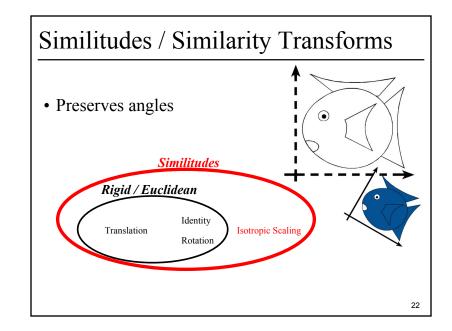
- Position objects in a scene
- Change the shape of objects
- Create multiple copies of objects
- Projection for virtual cameras
- Describe animations

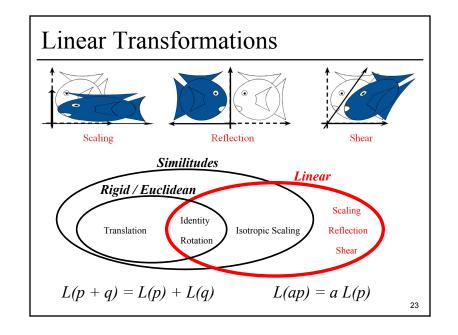


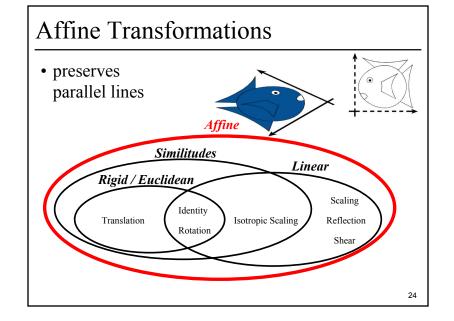


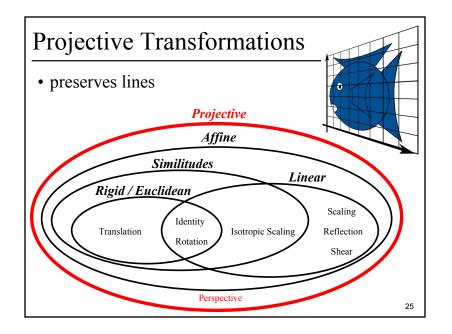






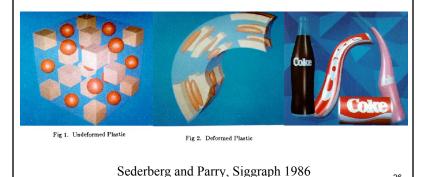






General (Free-Form) Transformation

- Does not preserve lines
- Not as pervasive, computationally more involved



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27

How are Transforms Represented?

$$x' = ax + by + c$$
$$y' = dx + ey + f$$

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} a & b \\ d & e \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} + \begin{pmatrix} c \\ f \end{pmatrix}$$

$$p' = Mp + t$$

Homogeneous Coordinates

- Add an extra dimension
 - in 2D, we use 3 x 3 matrices
 - In 3D, we use 4 x 4 matrices
- Each point has an extra value, w

$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ m & n & o & p \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

$$n' = Mn$$

29

Translation in homogeneous coordinates

$$x' = ax + by + c$$
$$y' = dx + ey + f$$

Affine formulation

Homogeneous formulation

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{pmatrix} a & b \\ d & e \end{pmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{pmatrix} c \\ f \end{bmatrix} \qquad \begin{bmatrix} x' \\ y' \\ I \end{bmatrix} = \begin{pmatrix} a & b & c \\ d & e & f \\ 0 & 0 & I \end{pmatrix} \begin{bmatrix} x \\ y \\ I \end{bmatrix}$$
$$p' = Mp + t \qquad p' = Mp$$

30

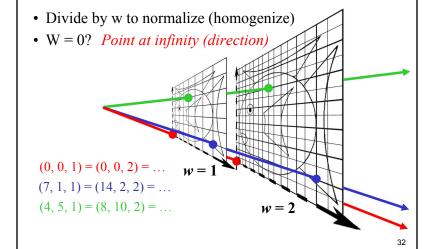
Homogeneous Coordinates

• Most of the time w = 1, and we can ignore it

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

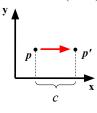
• If we multiply a homogeneous coordinate by an *affine matrix*, w is unchanged

Homogeneous Visualization



Translate (tx, ty, tz)

Why bother with the extra dimension?
 Because now translations



Translate(c, θ , θ)

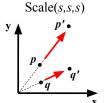
can be encoded in the matrix!

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

33

Scale (sx, sy, sz)

• Isotropic (uniform) scaling: $S_x = S_y = S_z$

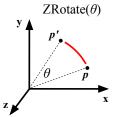


$$\begin{pmatrix} x' \\ y' \\ z' \\ 1 \end{pmatrix} = \begin{pmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix}$$

34

Rotation

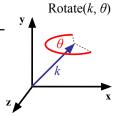
• About z axis



$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 & 0 \\ \sin \theta & \cos \theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

Rotation

• About (k_x , k_y , k_z), a unit vector on an arbitrary axis (Rodrigues Formula)



$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} k_x k_x (1-c) + c & k_z k_x (1-c) - k_z s & k_x k_z (1-c) + k_y s & 0 \\ k_y k_x (1-c) + k_z s & k_z k_x (1-c) + c & k_y k_z (1-c) - k_x s & 0 \\ k_z k_x (1-c) - k_y s & k_z k_x (1-c) - k_x s & k_z k_z (1-c) + c & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

where $c = \cos \theta$ & $s = \sin \theta$

Storage

- Often, w is not stored (always 1)
- Needs careful handling of direction vs. point
 - Mathematically, the simplest is to encode directions with w = 0
 - In terms of storage, using a 3-component array for both direction and points is more efficient
 - Which requires to have special operation routines for points vs. directions

31

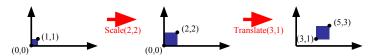
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38

How are transforms combined?

Scale then Translate



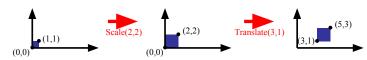
Use matrix multiplication: p' = T(Sp) = TSp

$$TS = \begin{pmatrix} 1 & 0 & 3 \\ 0 & 1 & I \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 2 & 0 & 3 \\ 0 & 2 & I \\ 0 & 0 & 1 \end{pmatrix}$$

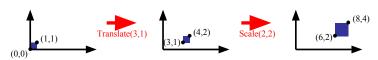
Caution: matrix multiplication is NOT commutative!

Non-commutative Composition

Scale then Translate: p' = T(Sp) = TSp



Translate then Scale: p' = S(Tp) = STp



Non-commutative Composition

Scale then Translate: p' = T(Sp) = TSp

$$TS = \begin{pmatrix} 1 & 0 & 3 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 2 & 0 & 3 \\ 0 & 2 & 1 \\ 0 & 0 & 1 \end{pmatrix}$$

Translate then Scale: p' = S(Tp) = STp

$$ST = \begin{pmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 3 \\ 0 & 1 & I \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 2 & 0 & 6 \\ 0 & 2 & 2 \\ 0 & 0 & 1 \end{pmatrix}$$

Exercise!

Form teams of 2. Use 1 piece of paper. Put both names on the top. Work together. Both people should write. Hand in to TA Jeramey Tyler after we discuss.

Write down the 3x3 matrix that transforms this set of 4 points:

A:(0,0)

B: (1,0)

C: (1,1)

D:(0,1)

to these new positions:

A': (-1, 1) B': (-1, 0) C': (0, 0) D': (0, 1)

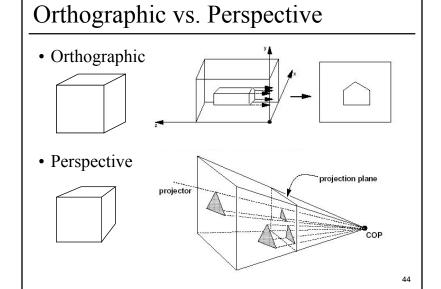
Show your work.

If you finish early...

Solve the problem using a different technique.

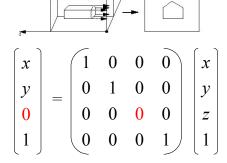
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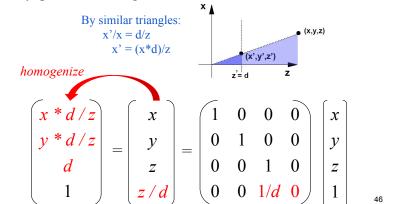
Simple Orthographic Projection

• Project all points along the z axis to the z = 0 plane



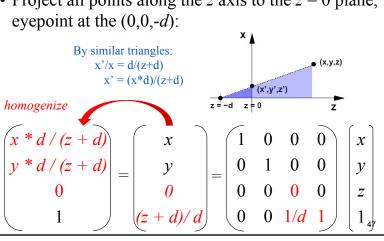
Simple Perspective Projection

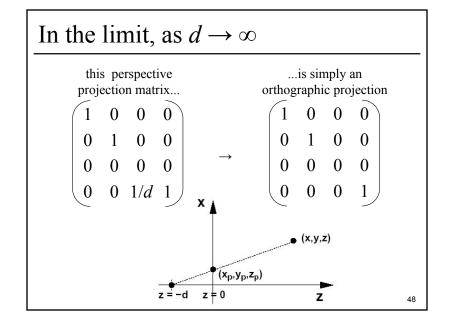
• Project all points along the z axis to the z = d plane, eyepoint at the origin:



Alternate Perspective Projection

• Project all points along the z axis to the z = 0 plane, eyepoint at the (0,0,-d):





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49

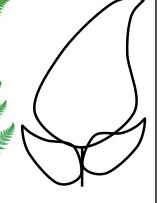
Iterated Function Systems (IFS)

• Capture self-similarity

• Contraction (reduce distances)

• An attractor is a fixed point

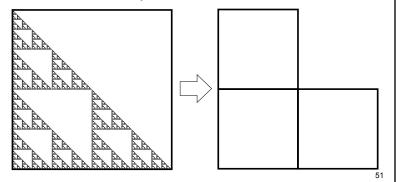
$$A = \prod f_i(A)$$



5

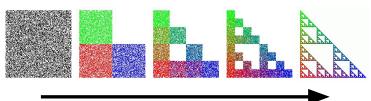
Example: Sierpinski Triangle

- Described by a set of *n* affine transformations
- In this case, n = 3
 - translate & scale by 0.5

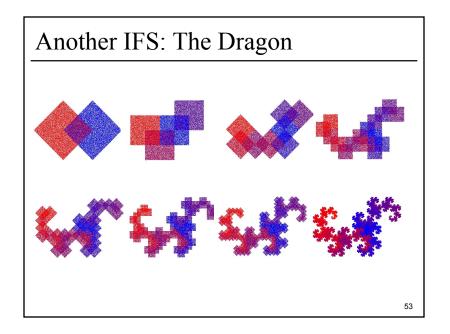


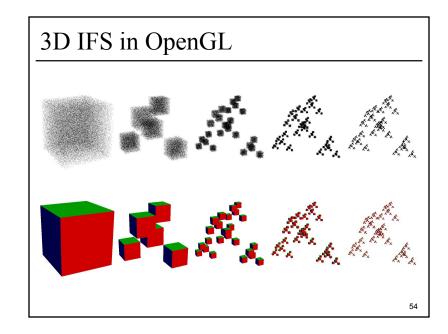
Example: Sierpinski Triangle

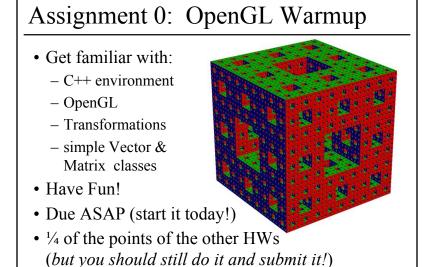
for "lots" of random input points $(\mathbf{x}_0, \mathbf{y}_0)$ for j=0 to num_iters randomly pick one of the transformations $(\mathbf{x}_{k+1}, \mathbf{y}_{k+1}) = \mathbf{f}_i (\mathbf{x}_k, \mathbf{y}_k)$ display $(\mathbf{x}_k, \mathbf{y}_k)$

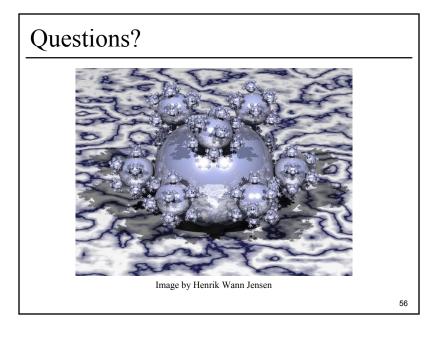


Increasing the number of iterations





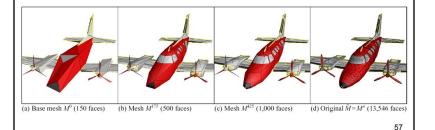




For Next Time:

Volunteer to be "Discussant"? Note: This is not a "presentation". Be sure to read blurb (& linked webpage) on course webpage about Assigned Readings & Discussants.

- Read Hugues Hoppe "Progressive Meshes" SIGGRAPH 1996
- Post a comment or question on the course WebCT/LMS discussion by 10am on Friday



Questions to think about:

- How do we represent meshes?
- How to automatically decide what parts of the mesh are important / worth preserving?
- Algorithm performance: memory, speed?
- What were the original target applications? Are those applications still valid? Are there other modern applications that can leverage this technique?