## Ray Tracing

## Last Time? • Keyframing • Procedural Animation • Physically-Based Animation • Forward and Inverse Kinematics • Motion Capture

### Reading for Today

"Artist-Directed Dynamics for 2D Animation", Bai, Kaufman, Liu, & Popović, SIGGRAPH 2016

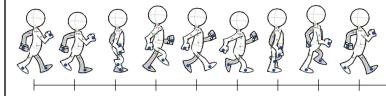


Figure 6: Keyframes used in the articulated character walk example. The artist only specifies keyframes for a subset of handles (handles at hands and feet) which are shown as blue dots. Nine keyframes are used to create a walking cycle. Their timing is visualized by the black lines at the bottom. The artworks are adapted from Angryanimator.com(http://www.angryanimator.com/)

### Reading for Today

"Articulated Swimming Creatures" Jie Tan, Yuting Gu, Greg Turk, and C. Karen Liu, SIGGRAPH 2011

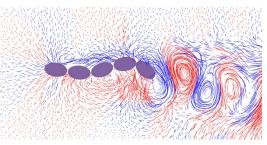


Figure 8: A five-link eel swims in a 2D fluid environment. In contrast to the simulation in 3D, an eel swimming in 2D fluid sheds only one single vortex street. Red traces show the counter-clockwise vortices while blue traces show the clockwise vortices.

http://www.cc.gatech.edu/~jtan34/project/articulatedSwimmingCreatures.html

### Reading for Today

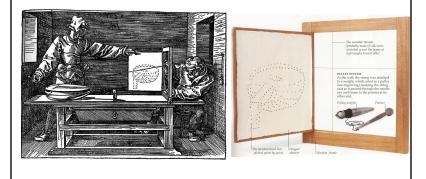
"Flexible Muscle-Based Locomotion for Bipedal Creatures", Geijtenbeek, van de Panne, van der Stappen, SIGGRAPH Asia 2013



Figure 1: Physics-based simulation of locomotion for a variety of creatures driven by 3D muscle-based control. The synthesized controllers can locomote in real time at a range of speeds, be steered to a target heading, and can traverse variable terrain.

### Durer's Ray Casting Machine

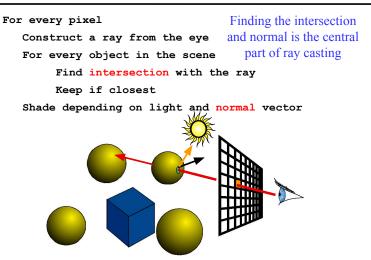
• Albrecht Durer, 16<sup>th</sup> century

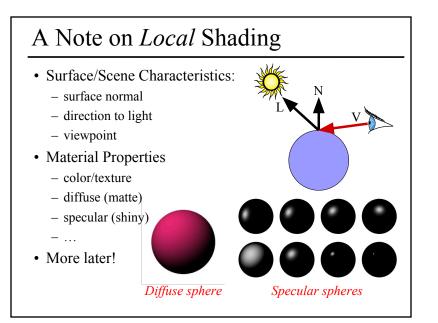


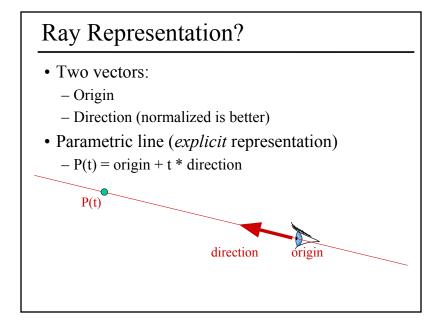
### Today

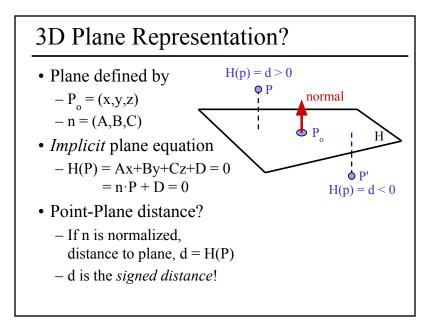
- Ray Casting
  - Ray-Plane Intersection
  - Ray-Sphere Intersection
  - Point in Polygon
- Ray Tracing
- Recursive Ray Tracing
- Distribution Ray Tracing

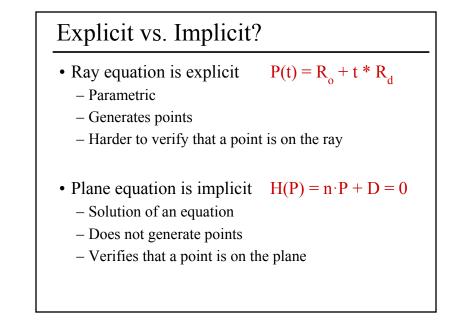
### Ray Casting





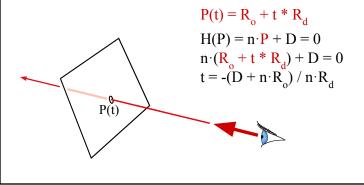






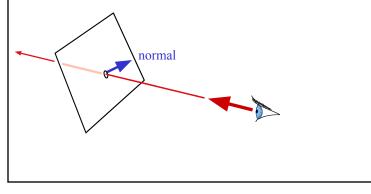
### **Ray-Plane Intersection**

- Intersection means both are satisfied
- So, insert explicit equation of ray into implicit equation of plane & solve for t



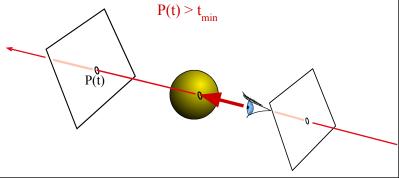
### Normal at Surface Intersection

- Needed for shading
  - diffuse: dot product between light and normal
- Normal of a plane is constant!

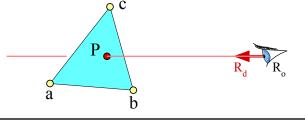


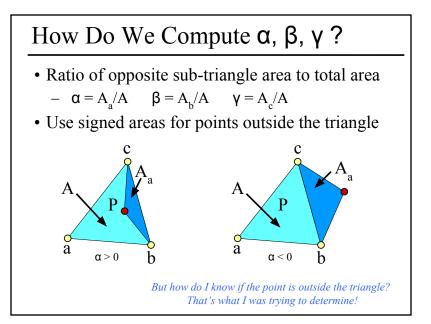
## Additional Housekeeping

- Verify that intersection is closer than previous  $P(t) < t_{current}$
- Verify that it is not out of range (behind eye)



### • Intersect with the plane... • Intersect with the plane... • Then use barycentric coordinates: $-P(\alpha, \beta, \gamma) = \alpha a + \beta b + \gamma c$ with $\alpha + \beta + \gamma = 1$ $- If \ 0 < \alpha < 1 & 0 < \beta < 1 & 0 < \gamma < 1$ then the point is inside the triangle!





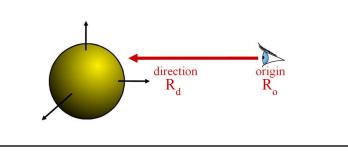
### Using Cramer's Rule...

• Used to solve for one variable at a time in system of equations

$\beta = \frac{\begin{vmatrix} a_x - R_{ox} & a_x - c_x & R_{dx} \\ a_y - R_{oy} & a_y - c_y & R_{dy} \\ a_z - R_{oz} & a_z - c_z & R_{dz} \end{vmatrix}}{ A }$	$\gamma = \frac{\begin{vmatrix} a_x - b_x & a_x - R_{ox} & R_{dx} \\ a_y - b_y & a_y - R_{oy} & R_{dy} \\ a_z - b_z & a_z - R_{oz} & R_{dz} \end{vmatrix}}{ A }$
$a_x - b_x$ $a_x - c_x$ $a_x - b_x$	R <sub>ox</sub>     denotes the determinant
$t = \frac{\begin{vmatrix} a_x - b_x & a_x - c_x & a_x - b_x \\ a_y - b_y & a_y - c_y & a_y - b_x \\ a_z - b_z & a_z - c_z & a_z - b_x \\ \hline  A  \end{vmatrix}}{ A }$	Roy     Can be copied       Roz     mechanically       into code

### Sphere Representation?

- Implicit sphere equation
  - Assume centered at origin (easy to translate)
  - $-\operatorname{H}(\operatorname{P}) = \operatorname{P} \cdot \operatorname{P} \cdot \operatorname{r}^2 = 0$



## **Ray-Sphere Intersection**

• Insert explicit equation of ray into implicit equation of sphere & solve for t  $P(t) = R_o + t^*R_d \qquad H(P) = P \cdot P - r^2 = 0$  $(R_o + tR_d) \cdot (R_o + tR_d) - r^2 = 0$ 

$$R_{d} \cdot R_{d} t^{2} + 2R_{d} \cdot R_{o} t + R_{o} \cdot R_{o} - r^{2} = 0$$

direction

R<sub>d</sub>

origin

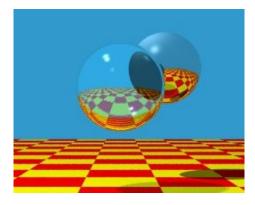
### **Ray-Sphere Intersection**

- Quadratic:  $at^2 + bt + c = 0$  -a = 1 (remember,  $||\mathbf{R}_d|| = 1$ )  $-b = 2\mathbf{R}_d \cdot \mathbf{R}_o$   $-c = \mathbf{R}_o \cdot \mathbf{R}_o - r^2$ • with discriminant  $d = \sqrt{b^2 - 4ac}$ • and solutions  $t_{\pm} = \frac{-b \pm d}{c}$
- What does it mean if there are no solutions, 1 solution, or 2 solutions?

# <figure>Questions?Image: depth de

### Reading for Next Friday

• "An improved illumination model for shaded display" Turner Whitted, 1980.

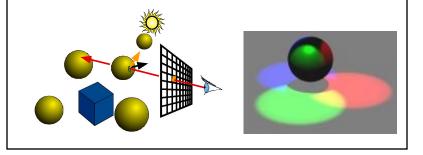


### Today

- Ray Casting
- Ray Tracing
  - Shadows
  - Reflection
  - Refraction
- Recursive Ray Tracing
- Distribution Ray Tracing

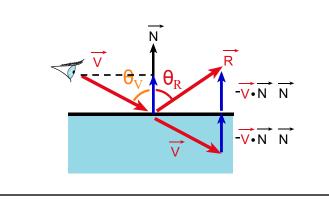
### How Can We Add Shadows?

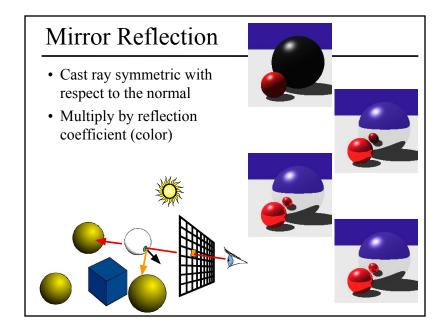
Find the point to be shaded
For every light,
Construct ray from point to light
For every object
find intersection of ray with object
If no objects between point and light
Add contribution from light



### Reflection

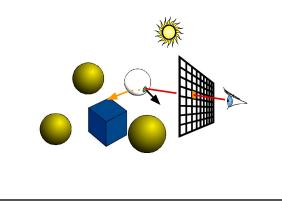
- Reflection angle = view angle
- $\mathbf{R} = \mathbf{V} 2 (\mathbf{V} \cdot \mathbf{N}) \mathbf{N}$

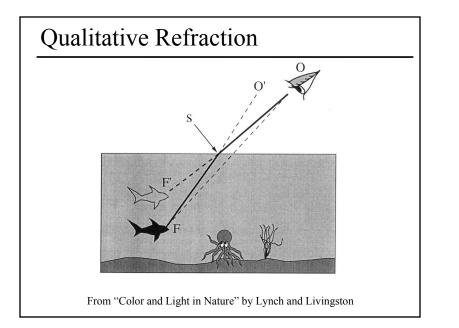


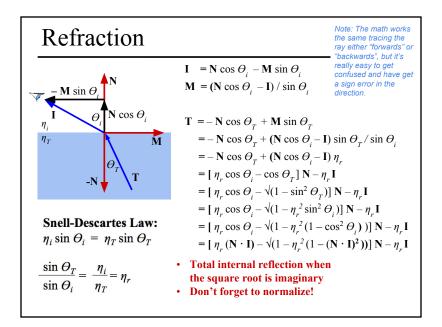


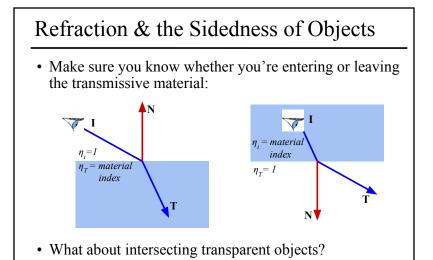
### Transparency

- Cast ray in refracted direction
- Multiply by transparency coefficient (color)









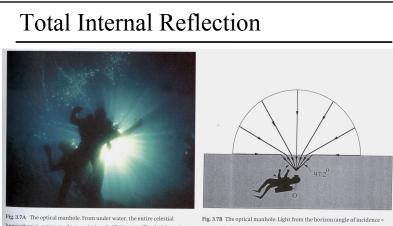
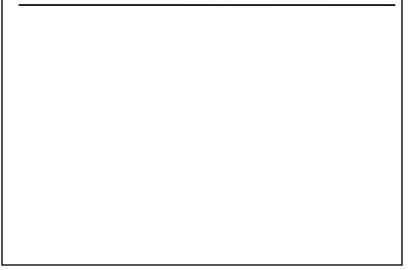


Fig. 37A The optical manhole. From under water, the entire celestial hemisphere is compressed into a circle only 927-across. The dark boundary defining the edges of the manhole is not sharp due to surface waves. The rays are analogous to the crepuscular type seen in hazy air. Section 1.9. (Photo by D. Granger) Fig. 3.7B The optical manhole. Light from the horizon (angle of incidence = 90°) is refracted downward at an angle of 48.6°. This compresses the sky into a circle with a diameter of 97.2° instead of its usual 180°.

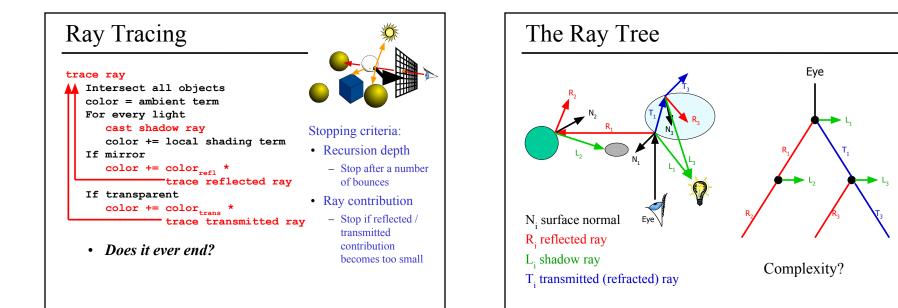
From "Color and Light in Nature" by Lynch and Livingston

### Questions?



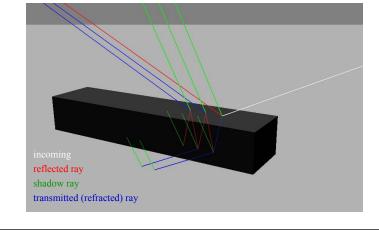
### Today

- Ray Casting
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- Recursive Ray Tracing
- Distribution Ray Tracing



### Ray Debugging

• Visualize the ray tree for single image pixel



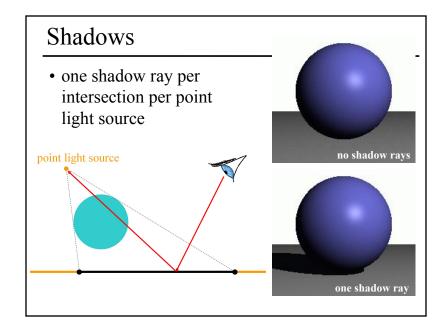
### Today

- Ray Casting
- Ray Tracing
- Recursive Ray Tracing
- Distribution Ray Tracing
  - Soft shadows
  - Antialiasing (getting rid of jaggies)
  - Glossy reflection
  - Motion blur
  - Depth of field (focus)

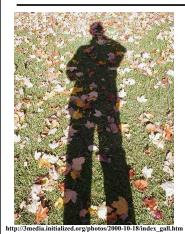
### Other Reading for Next Friday

• "Distributed Ray Tracing", Cook, Porter, & Carpenter, SIGGRAPH 1984.

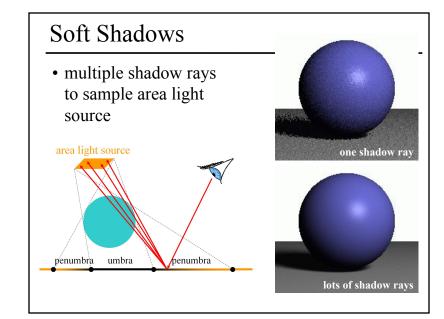


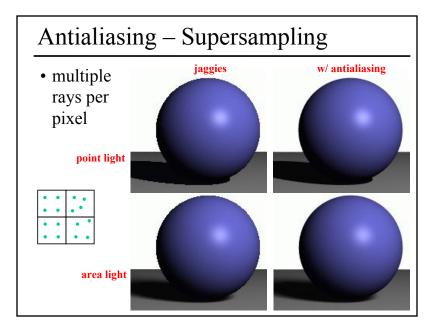


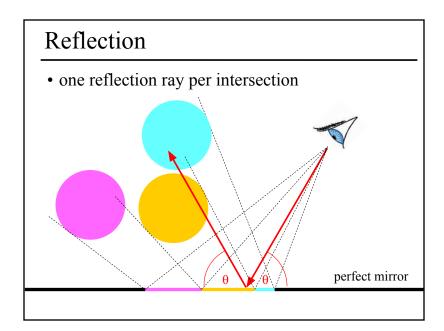
### Shadows & Light Sources

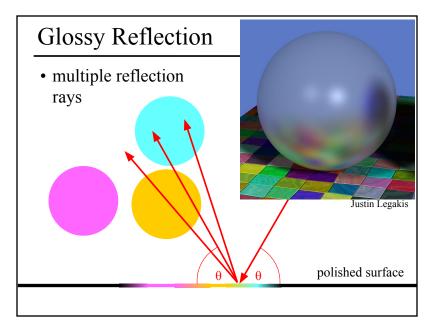












### Motion Blur • Sample objects temporally • Objects • Obje

