Real-Time Shadows

"Now this is... this is... well, I guess it's another snake."

San Marco - The Crossing and North Transept, with Musicians Singing

Giovanni Antonio Canal, il Canaletto 1766
Last Drawing of Canaletto
Cameron McNall, 2000

The Presentation of the Doge in San Marco
Giovanni Antonio Canal, il Canaletto 1766
The Coronation of the Doge on the Scala dei Giganti, Giovanni Antonio Canal, Canaletto, 1763-1766

Last Time

- Modeling Transformations
- Illumination (Shading)
- Viewing Transformation (Perspective / Orthographic)
- Clipping
- Projection (to Screen Space)
- Scan Conversion (Rasterization)
- Visibility / Display

- Graphics Pipeline
- Clipping
- Rasterization
Reading for Today:


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• “Ray Tracing on Programmable Graphics Hardware Purcell”, Buck, Mark, & Hanrahan SIGGRAPH 2002
Today

• Why are Shadows Important?
• Planar Shadows
• Projective Texture Shadows
• Shadow Maps
• Shadow Volumes

Why are Shadows Important?

• Depth cue
• Scene Lighting
• Realism
• Contact points
Shadows as a Depth Cue

For Intuition about Scene Lighting

- Position of the light (e.g. sundial)
- Hard shadows vs. soft shadows
- Colored lights
- Directional light vs. point light
Today

- Why are Shadows Important?
- Planar Shadows
- Projective Texture Shadows
  - Shadow View Duality
  - Texture Mapping
- Shadow Maps
- Shadow Volumes

Cast Shadows on Planar Surfaces

- Draw the object primitives a second time, projected to the ground plane
Limitations of Planar Shadows

• Does not produce self-shadows, shadows cast on other objects, shadows on curved surfaces, etc.

Shadow/View Duality

• A point is lit if it is visible from the light source

• Shadow computation similar to view computation
Texture Mapping

• Don't have to represent everything with geometry

Fake Shadows using Projective Textures

• Separate obstacle and receiver
• Compute b/w image of obstacle from light
• Use image as projective texture for each receiver

Figure from Moller & Haines “Real Time Rendering”
Projective Texture Shadow Limitations

- Must specify occluder & receiver
- No self-shadows
- Resolution

Figure from Moller & Haines “Real Time Rendering”

Questions?

Plate 52 Grandville, The Shadows (The French Cabinet) from La Caricature, 1830.
Today

- Why are Shadows Important?
- Planar Shadows
- Projective Texture Shadows
- **Shadow Maps**
- Shadow Volumes

Shadow Maps

- In Renderman
  - (High-end production software)
Shadow Mapping

- Texture mapping with depth information
- Requires 2 passes through the pipeline:
  - Compute shadow map (depth from light source)
  - Render final image, *check shadow map to see if points are in shadow*


Shadow Map Look Up

- We have a 3D point \((x,y,z)_{WS}\)
- How do we look up the depth from the shadow map?
- Use the 4x4 perspective projection matrix from the light source to get \((x',y',z')_{LS}\)
- \(\text{ShadowMap}(x',y') < z'\)

Limitations of Shadow Maps

1. Field of View
2. Bias (Epsilon)
3. Aliasing

1. Field of View Problem

- What if point to shadow is outside field of view of shadow map?
  - Use cubical shadow map
  - Use only spot lights!
2. The Bias (Epsilon) Nightmare

- For a point visible from the light source
  \[ \text{ShadowMap}(x', y') \approx z' \]

- How can we avoid erroneous self-shadowing?
  - Add bias (epsilon)

2. Bias (Epsilon) for Shadow Maps

\[ \text{ShadowMap}(x', y') + \text{bias} < z' \]

Choosing a good bias value can be very tricky

Correct image | Not enough bias | Way too much bias
3. Shadow Map Aliasing

- Under-sampling of the shadow map
- Reprojection aliasing – especially bad when the camera & light are opposite each other

3. Shadow Map Filtering

- Should we filter the depth? (weighted average of neighboring depth values)
- No... filtering depth is not meaningful

![Diagram of shadow map filtering]
3. Percentage Closer Filtering

- Instead filter the result of the test (weighted average of comparison results)
- But makes the bias issue more tricky

Sample Transform Step

Surface at $z = 49.8$

- 5x5 samples
- Nice antialiased shadow
- Using a bigger filter produces fake soft shadows
- Setting bias is tricky
**Projective Texturing + Shadow Map**

Light’s View  
Depth/Shadow Map  
Eye’s View

Images from Cass Everitt et al.,  
“Hardware Shadow Mapping”  
NVIDIA SDK White Paper

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**Shadows in Production**

- Often use shadow maps
- Ray casting as fallback in case of robustness issues

Figure 12. Frame from *L lux Jr.*

Figure 13. Shadow maps from *L lux Jr.*
Hardware Shadow Maps

- Can be done with hardware texture mapping
  - Texture coordinates u,v,w generated using 4x4 matrix
  - Modern hardware permits tests on texture values

Questions?
Today

- Why are Shadows Important?
- Planar Shadows
- Projective Texture Shadows
- Shadow Maps
- **Shadow Volumes**
  - The Stencil Buffer

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**Stencil Buffer**

- Tag pixels in one rendering pass to control their update in subsequent rendering passes
  - "For all pixels in the frame buffer" → "For all *tagged* pixels in the frame buffer"
- Can specify different rendering operations for each case:
  - stencil test fails
  - stencil test passes & depth test fails
  - stencil test passes & depth test passes
Stencil Buffer – Real-time Mirror

- Clear frame, depth & stencil buffers
- Draw all non-mirror geometry to frame & depth buffers
- Draw mirror to stencil buffer, where depth buffer passes
- Set depth to infinity, where stencil buffer passes
- Draw reflected geometry to frame & depth buffer, where stencil buffer passes

See NVIDIA's stencil buffer tutorial http://developer.nvidia.com also discusses blending, multiple mirrors, objects behind mirror, etc…

Shadow Volumes

- Explicitly represent the volume of space in shadow
- For each polygon
  - Pyramid with point light as apex
  - Include polygon to cap
- Shadow test similar to clipping
Shadow Volumes

- If a point is inside a shadow volume cast by a particular light, the point does not receive any illumination from that light.

- Cost of naive implementation: \#polygons * \#lights

Shadow Volumes

- Shoot a ray from the eye to the visible point.
- Increment/decrement a counter each time we intersect a shadow volume polygon (check z buffer).
- If the counter \( \neq 0 \), the point is in shadow.
Shadow Volumes w/ the Stencil Buffer

- Initialize stencil buffer to 0
- Draw scene with ambient light only
- Turn off frame buffer & z-buffer updates
- Draw front-facing shadow polygons
  - If z-pass → increment counter
- Draw back-facing shadow polygons
  - If z-pass → decrement counter
- Turn on frame buffer updates
- Turn on lighting and
  - Redraw pixels with counter = 0

If the Eye is in Shadow...

- ... then a counter of 0 does not necessarily mean lit
- 3 Possible Solutions:
  1. Explicitly test eye point with respect to all shadow volumes
  2. Clip the shadow volumes to the view frustum
  3. "Z-Fail" shadow volumes
1. Test Eye with Respect to Volumes

- Adjust initial counter value

2. Clip the Shadow Volumes

- Clip the shadow volumes to the view frustum and include these new polygons
- Messy CSG
3. "Z-Fail" Shadow Volumes

Start at infinity

... 

Draw front-facing shadow polygons
If z-fail, decrement counter

Draw back-facing shadow polygons
If z-fail, increment counter

... 

0 +1

• Introduces problems with far clipping plane
• Solved by clamping the depth during clipping
Optimizing Shadow Volumes

• Use silhouette edges only (edge where a back-facing & front-facing polygon meet)

Limitations of Shadow Volumes

• Introduces a lot of new geometry
• Expensive to rasterize long skinny triangles
• Limited precision of stencil buffer (counters)
  – for a really complex scene/object, the counter can overflow
• Objects must be watertight to use silhouette trick
• Rasterization of polygons sharing an edge must not overlap & must not have gap
Homework 4

• Create some geometry
  – Reflected object & floor
  – Silhouette edges
  – Shadow polygons
    • Make sure your polygons aren’t doubled up
    • Make sure your polygons are oriented consistently

• Mess with the stencil buffer
  – Don’t just blindly copy code from the tutorial
  – Use the web to read the man page for each instruction & its parameters

• Be creative with shaders
  – Hopefully everyone can get the examples to compile & run

Questions?

Reading for HW4:

• “Improving Shadows and Reflections via the Stencil Buffer”, Mark Kilgard, NVIDIA

Reading for Next Time: (pick one)

• "Rendering Fake Soft Shadows with Smoothies", Chan & Durand, EGSR 2003
Reading for Next Time: *(pick one)*

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<th>Opacity Shadow Maps</th>
<th>Density Clustering</th>
<th>Deep Opacity Maps</th>
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<td>(65 fps)</td>
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<td>(50 fps)</td>
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- "Deep Opacity Maps",
  Yuksel and Keyser, Eurographics 2008