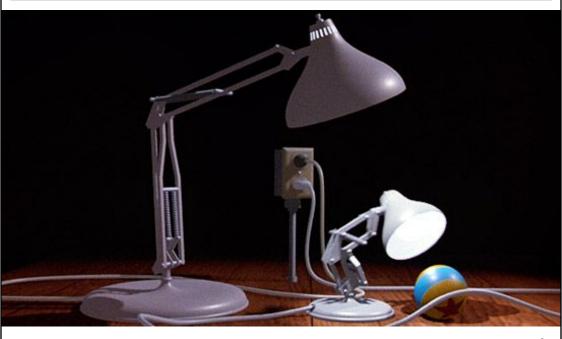
CSCI-4530/6530 Advanced Computer Graphics

http://www.cs.rpi.edu/~cutler/classes/advancedgraphics/S23/

Barb Cutler cutler@cs.rpi.edu

1

Luxo Jr., Pixar Animation Studios, 1986



Luxo Jr., Pixar Animation Studios, 1986

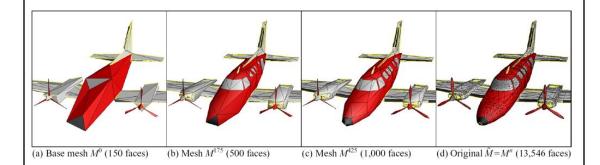


Topics for the Semester

- Meshes
 - representation
 - simplification
 - subdivision surfaces
 - construction/generation
 - volumetric modeling
- Simulation
 - particle systems, cloth
 - rigid body, deformation
 - wind/water flows
 - collision detection
 - weathering

- Rendering
 - ray tracing, shadows
 - appearance models
 - local vs. global illumination
 - radiosity, photon mapping, subsurface scattering, etc.
- · procedural modeling
- texture synthesis
- non-photorealistic rendering
- hardware & more ...

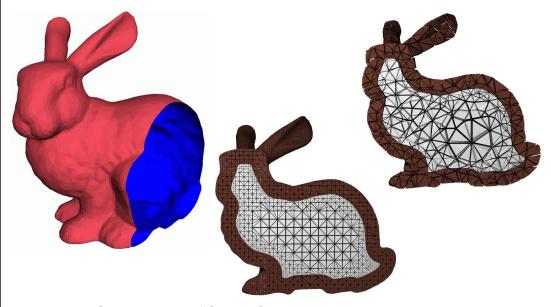
Mesh Simplification



Hoppe "Progressive Meshes" SIGGRAPH 1996

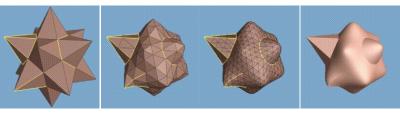
5

Mesh Generation & Volumetric Modeling

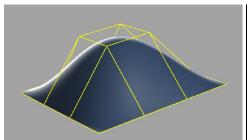


Cutler et al., "Simplification and Improvement of Tetrahedral Models for Simulation" 2004

Modeling – Subdivision Surfaces



Hoppe et al., "Piecewise Smooth Surface Reconstruction" 1994



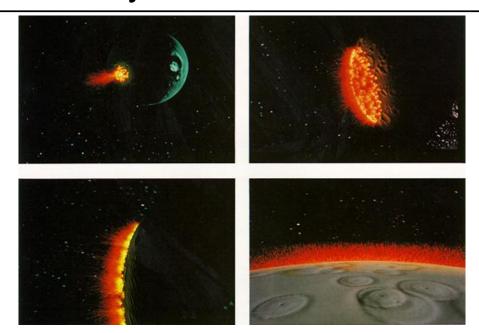




Geri's Game Pixar 1997

7

Particle Systems



Star Trek: The Wrath of Khan 1982

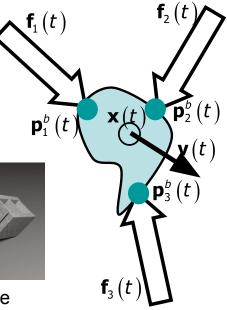
Physical Simulation

- Rigid Body Dynamics
- Collision Detection
- Fracture
- Deformation



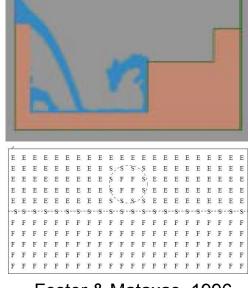






9

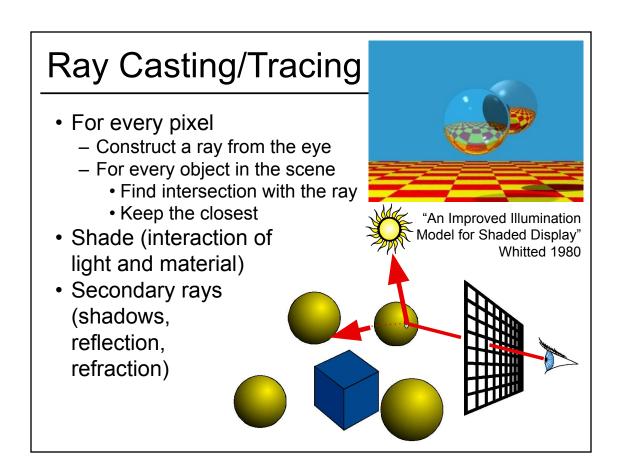
Fluid Dynamics

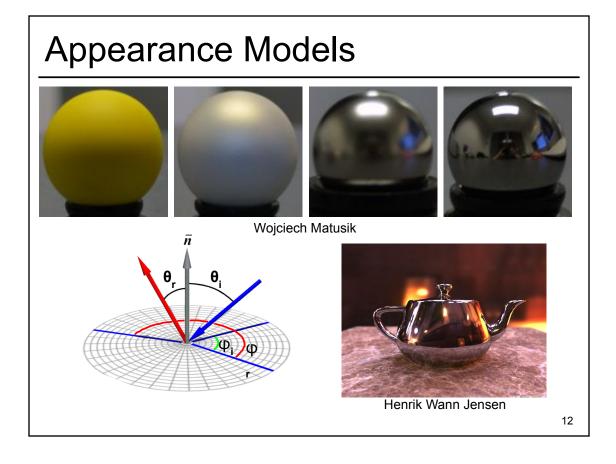


Foster & Mataxas, 1996



"Visual Simulation of Smoke" Fedkiw, Stam & Jensen SIGGRAPH 2001



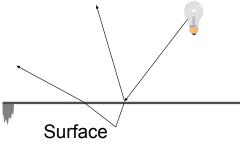


Subsurface Scattering









Jensen et al.,
"A Practical Model for
Subsurface Light Transport"
SIGGRAPH 2001

13

Syllabus & Course Website

http://www.cs.rpi.edu/~cutler/classes/advancedgraphics/S23/

Which version should I register for?

CSCI 6530: 4 units of graduate credit

CSCI 4530 : 4 units of undergraduate credit

 This is an intensive course aimed at graduate students and undergraduates interested in graphics research, involving significant reading & programming each week. Taking this course in a 5 course / overload semester is discouraged.

Grades

http://www.cs.rpi.edu/~cutler/classes/advancedgraphics/S23/

- This course counts as "communications intensive" for undergraduates. As such, you must satisfactorily complete all readings, presentations, project reports to pass the course.
- As this is an elective (not required) course, I expect to grade this course: "A", "A-", "B+", "B", "B-", or "F"
 - Don't expect C or D level work to "pass"
 - I don't want to give any "F"s

15

Lecture Attendance/Participation

http://www.cs.rpi.edu/~cutler/classes/advancedgraphics/S23/

- Lecture will be discussion-intensive
 - We will discuss research papers
 - We will do worksheets in groups of 2 or 3
- You are expected to regularly attend and participate during in person lectures
 - Recorded lectures from a prior term will be recorded & posted on the calendar.
 - If illness or other appropriate absence force you to miss more than 2 lectures throughout the term, a formal excused absence will be required.

Questions?

Outline

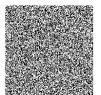
- Course Overview
- Classes of Transformations
- Representing Transformations
- Combining Transformations
- Orthographic & Perspective Projections
- Example: Iterated Function Systems (IFS)

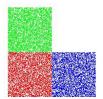
What is a Transformation?

 Maps points (x, y) in one coordinate system to points (x', y') in another coordinate system

$$x' = ax + by + c$$
$$y' = dx + ey + f$$

• For example, Iterated Function System (IFS):





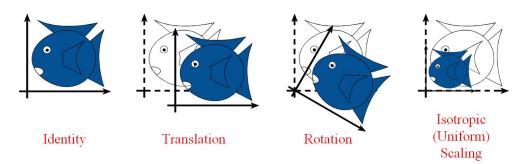






19

Simple Transformations

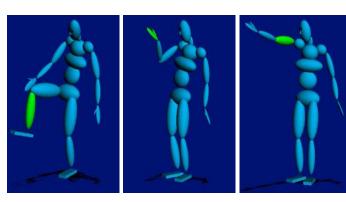


- Can be combined
- Are these operations invertible?

Yes, except scale = 0

Transformations are used to:

- Position objects in a scene
- Change the shape of objects
- Create multiple copies of objects
- Projection for virtual cameras
- Describe animations

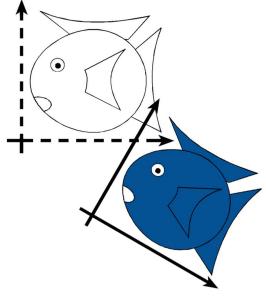


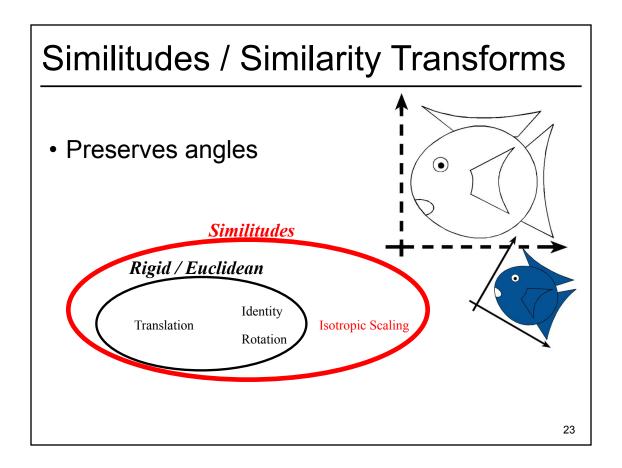
21

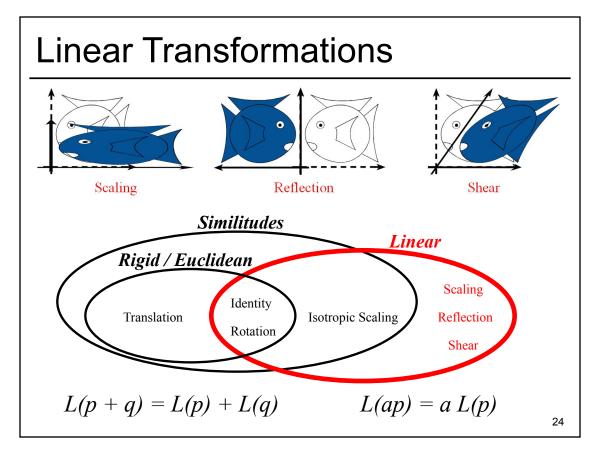
Rigid-Body / Euclidean Transforms

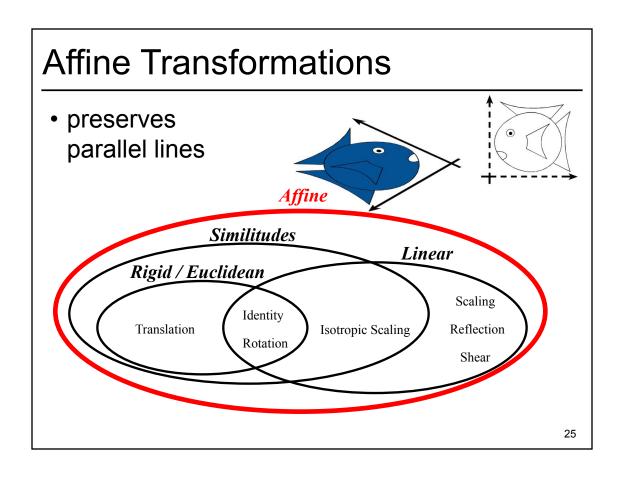
- Preserves distances
- Preserves angles

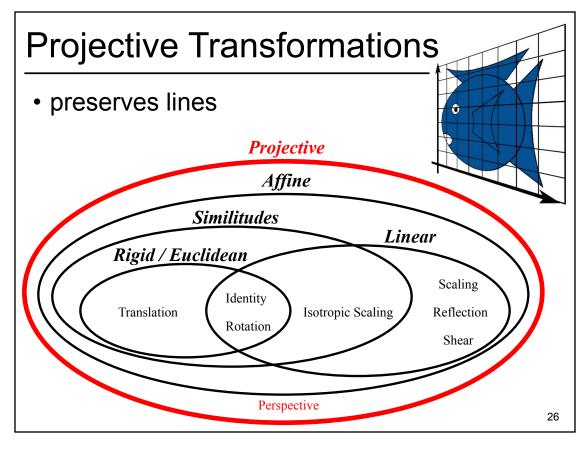












General (Free-Form) Transformation

- Does not preserve lines
- Not as pervasive, computationally more involved



Fig 1. Undeformed Plastic

Fig 2. Deformed Plastic

Sederberg and Parry, Siggraph 1986

27

Outline

- Course Overview
- Classes of Transformations
- Representing Transformations
- Combining Transformations
- Orthographic & Perspective Projections
- Example: Iterated Function Systems (IFS)

How are Transforms Represented?

$$x' = ax + by + c$$
$$y' = dx + ey + f$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ d & e \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} c \\ f \end{bmatrix}$$

$$p' = Mp + t$$

29

Homogeneous Coordinates

- Add an extra dimension
 - in 2D, we use 3 x 3 matrices
 - In 3D, we use 4 x 4 matrices
- Each point has an extra value, w

$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ m & n & o & p \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

$$p' = Mp$$

Translation in homogeneous coordinates

$$x' = ax + by + c$$
$$y' = dx + ey + f$$

Affine formulation

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ d & e \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} c \\ f \end{bmatrix}$$

$$p' = Mp + p$$

Homogeneous formulation

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ d & e \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} c \\ f \end{bmatrix} \qquad \begin{bmatrix} x' \\ y' \\ I \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & I \end{bmatrix} \begin{bmatrix} x \\ y \\ I \end{bmatrix}$$
$$p' = Mp + t \qquad p' = Mp$$

$$p' = Mp$$

31

Homogeneous Coordinates

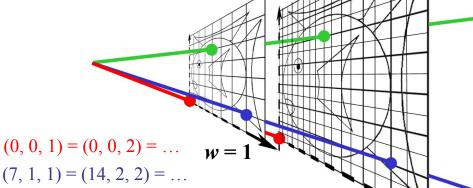
• Most of the time w = 1, and we can ignore it

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

 If we multiply a homogeneous coordinate by an affine matrix, w is unchanged

Homogeneous Visualization

- Divide by w to normalize (homogenize)
- W = 0? Point at infinity (direction)



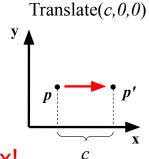
 $(4, 5, 1) = (8, 10, 2) = \dots$

33

Translate (tx, ty, tz)

Why bother with the extra dimension?

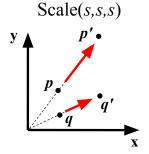
Because now translations can be encoded in the matrix!



$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

Scale (sx, sy, sz)

• Isotropic (uniform) scaling: $s_x = s_y = s_z$

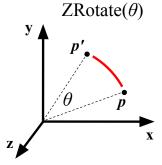


$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

35

Rotation

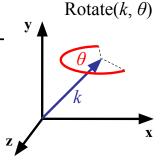
About z axis



$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 & 0 \\ \sin \theta & \cos \theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

Rotation

 About (kx, ky, kz), a unit vector on an arbitrary axis (Rodrigues Formula)



$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} k_x k_x (1-c) + c & k_z k_x (1-c) - k_z s & k_x k_z (1-c) + k_y s & 0 \\ k_y k_x (1-c) + k_z s & k_z k_x (1-c) + c & k_y k_z (1-c) - k_x s & 0 \\ k_z k_x (1-c) - k_y s & k_z k_x (1-c) - k_x s & k_z k_z (1-c) + c & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

where $c = \cos \theta$ & $s = \sin \theta$

37

Storage

- Often, w is not stored (always 1)
- Needs careful handling of direction vs. point
 - Mathematically, the simplest is to encode directions with w = 0
 - In terms of storage, using a 3-component array for both direction and points is more efficient
 - Which requires to have special operation routines for points vs. directions

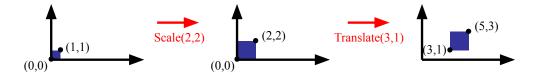
Outline

- Course Overview
- Classes of Transformations
- Representing Transformations
- Combining Transformations
- Orthographic & Perspective Projections
- Example: Iterated Function Systems (IFS)

39

How are transforms combined?

Scale then Translate



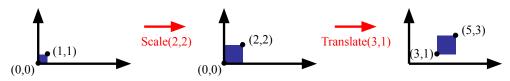
Use matrix multiplication: p' = T(Sp) = TSp

$$TS = \begin{pmatrix} 1 & 0 & 3 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 2 & 0 & 3 \\ 0 & 2 & 1 \\ 0 & 0 & 1 \end{pmatrix}$$

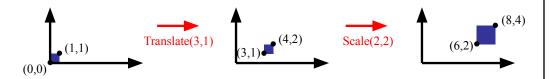
Caution: matrix multiplication is NOT commutative!

Non-commutative Composition

Scale then Translate: p' = T(Sp) = TSp



Translate then Scale: p' = S(Tp) = STp



41

Non-commutative Composition

Scale then Translate: p' = T(Sp) = TSp

$$TS = \begin{pmatrix} 1 & 0 & 3 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 2 & 0 & 3 \\ 0 & 2 & 1 \\ 0 & 0 & 1 \end{pmatrix}$$

Translate then Scale: p' = S(Tp) = STp

$$ST = \begin{pmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 3 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 2 & 0 & 6 \\ 0 & 2 & 2 \\ 0 & 0 & 1 \end{pmatrix}$$

Worksheet!

Write down the 3x3 matrix that transforms this set of 4 points:

to th

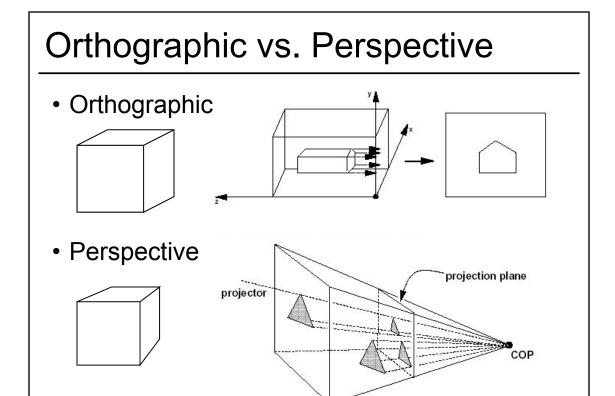
NOTE: We'll be doing pair worksheets throughout the term. We'll randomize the groups so you work with lots of different partners.

Show your work.

If you finish early...
Solve the problem using a different technique.

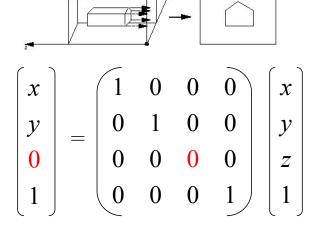
Outline

- Course Overview
- Classes of Transformations
- Representing Transformations
- Combining Transformations
- Orthographic & Perspective Projections
- Example: Iterated Function Systems (IFS)



Simple Orthographic Projection

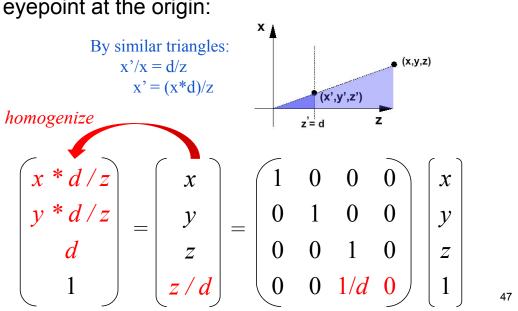
• Project all points along the z axis to the z = 0 plane



46

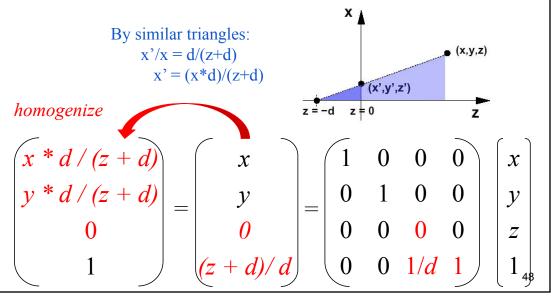
Simple Perspective Projection

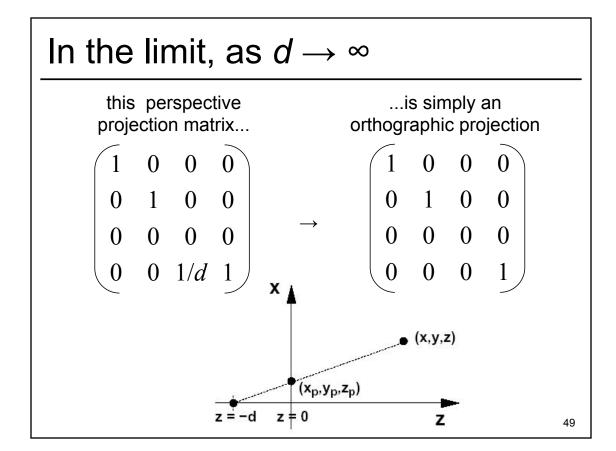
• Project all points along the z axis to the z = d plane, eyepoint at the origin:



Alternate Perspective Projection

• Project all points along the z axis to the z = 0 plane, eyepoint at the (0,0,-d):





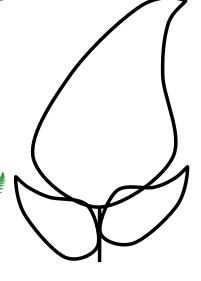
Outline

- Course Overview
- Classes of Transformations
- Representing Transformations
- Combining Transformations
- Orthographic & Perspective Projections
- Example: Iterated Function Systems (IFS)

Iterated Function Systems (IFS)

- Capture self-similarity
- Contraction (reduce distances)
- An attractor is a fixed point

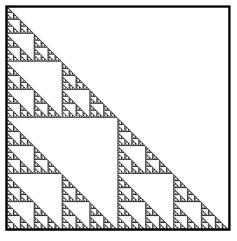
$$A = \prod f_i(A)$$

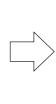


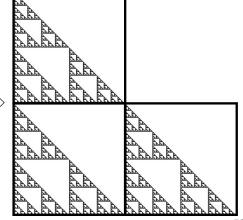
51

Example: Sierpinski Triangle

- Described by a set of *n* affine transformations
- In this case, n = 3
 - translate & scale by 0.5

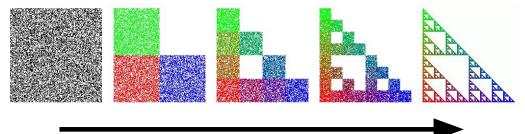






Example: Sierpinski Triangle

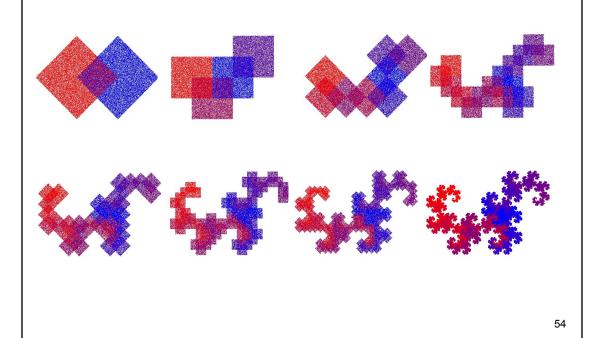
```
for "lots" of random input points (\mathbf{x}_0, \mathbf{y}_0)
for j=0 to num_iters
randomly pick one of the transformations
(\mathbf{x}_{k+1}, \mathbf{y}_{k+1}) = \mathbf{f}_i (\mathbf{x}_k, \mathbf{y}_k)
display (\mathbf{x}_k, \mathbf{y}_k)
```



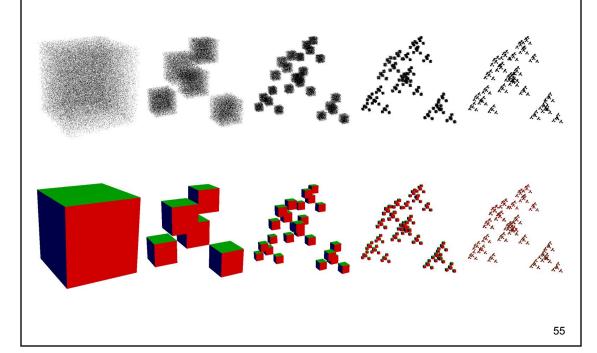
Increasing the number of iterations

53

Another IFS: The Dragon

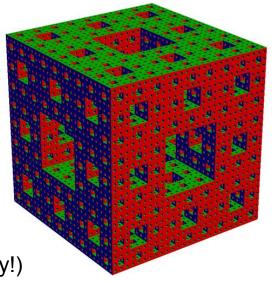


3D IFS in OpenGL / Apple Metal



Assignment 0: OpenGL/Metal Warmup

- · Get familiar with:
 - C++ environment
 - OpenGL / Metal
 - Transformations
 - simple Vector & Matrix classes
- Have Fun!
- Due ASAP (start it today!)
- 1/4 of the points of the other HWs (but you should still do it and submit it!)



Questions?

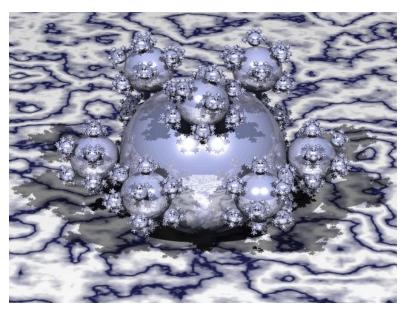


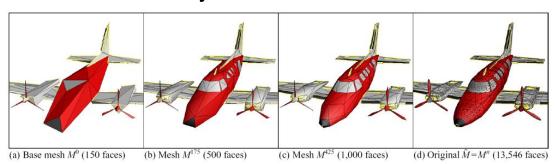
Image by Henrik Wann Jensen

57

For Next Time:

We need 2 volunteers to be "Discussants" Note: This is not a "presentation". Don't make slides! Be sure to read blurb (& linked webpage) on course webpage about Assigned Readings & Discussants.

- Read Hugues Hoppe "Progressive Meshes" SIGGRAPH 1996
- Everyone will a comment or question on the course Submitty discussion forum before 10am on Friday



Questions to think about:

- How do we represent meshes?
- How to automatically decide what parts of the mesh are important / worth preserving?
- Algorithm performance: memory, speed?
- What were the original target applications?
 Are those applications still valid?
 Are there other modern applications that can leverage this technique?