

Shaders and Procedural Modeling

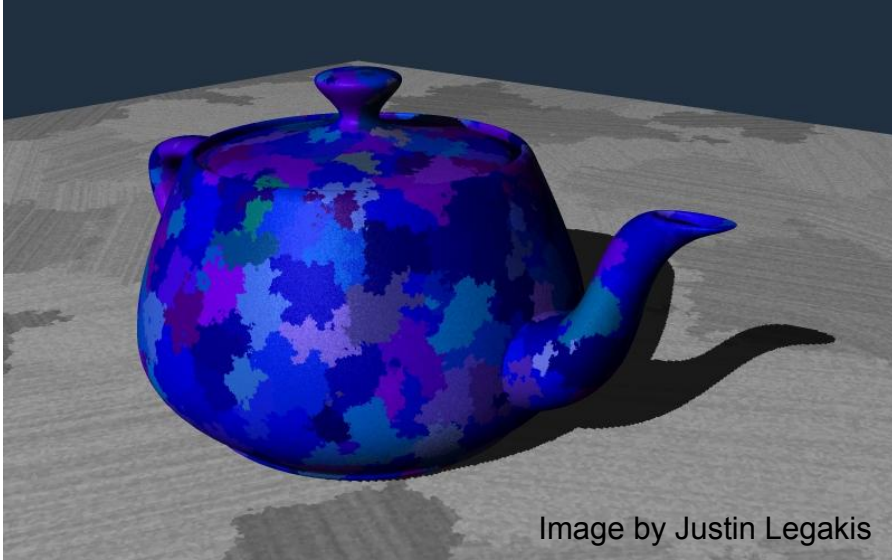


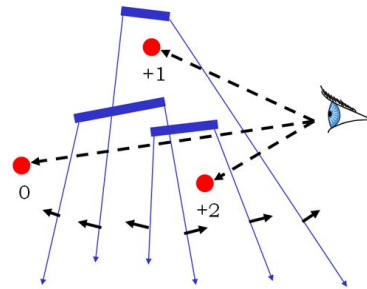
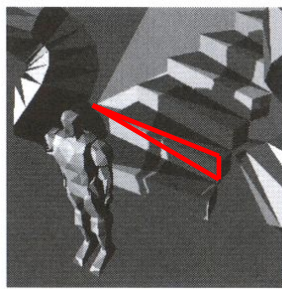
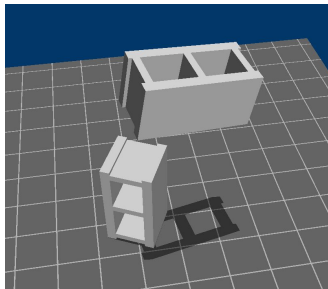
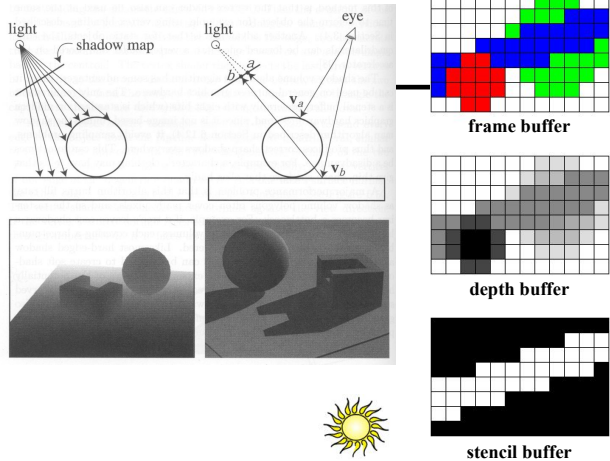
Image by Justin Legakis

For the Birds, Pixar, 2000



Last Time?

- Planar Shadows
- Projective Texture Shadows
- Shadow Maps
- Shadow Volumes
 - Stencil Buffer



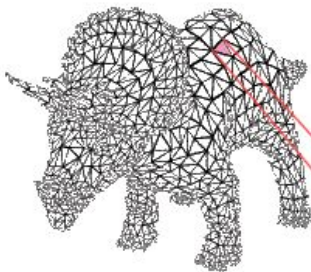
Today

- **Worksheet on Real-Time Shadows**
- Texture Mapping & Other “Mapping” Techniques
 - Bump Mapping
 - Displacement Mapping
 - Environment Mapping
 - Light Mapping
 - Normal Mapping
 - Parallax Mapping
 - Parallax Occlusion Mapping
- Programmable Shader Examples
 - Modern Graphics Hardware
 - Per-Pixel Shading
- Procedural Textures & Modeling
- Papers for Today
- Papers for Next Time

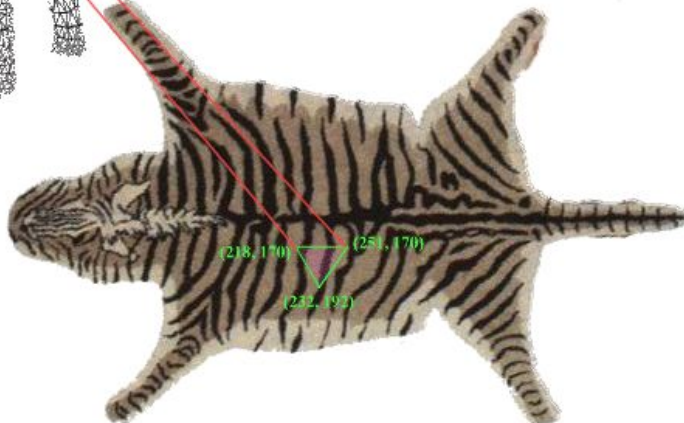
Today

- Worksheet on Real-Time Shadows
- **Texture Mapping** & Other “Mapping” Techniques
 - Bump Mapping
 - Displacement Mapping
 - Environment Mapping
 - Light Mapping
 - Normal Mapping
 - Parallax Mapping
 - Parallax Occlusion Mapping
- Programmable Shader Examples
 - Modern Graphics Hardware
 - Per-Pixel Shading
- Procedural Textures & Modeling
- Papers for Today
- Papers for Next Time

Texture Mapping



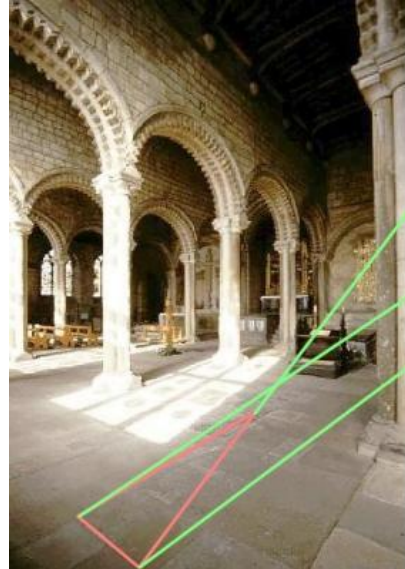
For each triangle in the model establish a corresponding region in the phototexture



During rasterization interpolate the coordinate indices into the texture map

Texture Mapping Difficulties

- Tedious to specify texture coordinates
- Acquiring textures is surprisingly difficult
 - Photographs have projective distortions
 - Variations in reflectance and illumination
 - Tiling problems

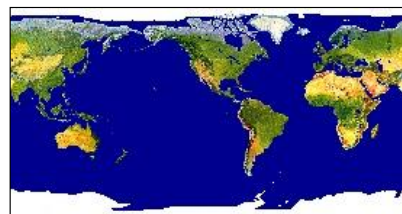


Can't do this!

You can get around this problem for planar surfaces if you specify 4 points...

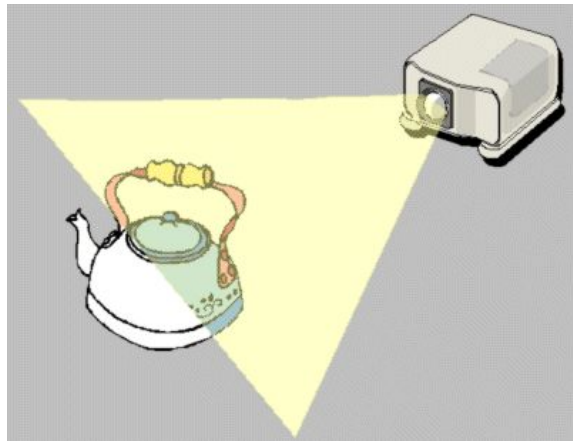
Common Texture Coordinate Mappings

- Orthogonal
- Cylindrical
- Spherical
- Perspective Projection
- Texture Chart



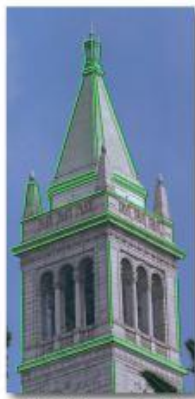
Projective Textures

- Use the texture like a slide projector
- No need to specify texture coordinates explicitly

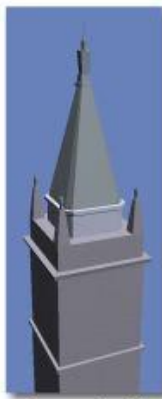


Projective Texture Example

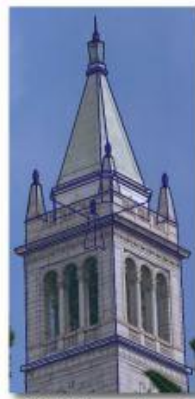
- Modeling from photographs
- Using input photos as textures



Original photograph with marked edges



Recovered model



Model edges projected onto photograph

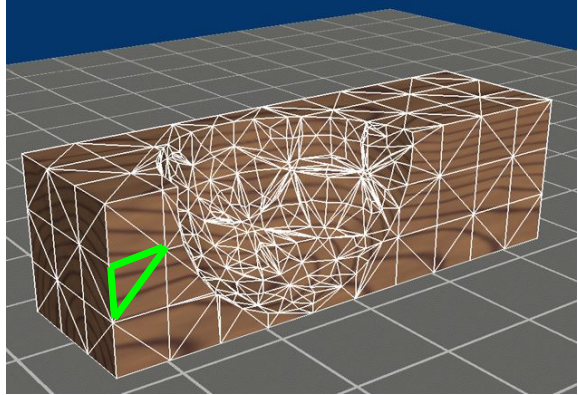
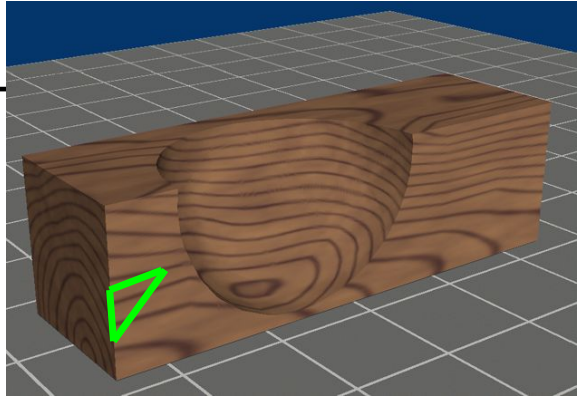
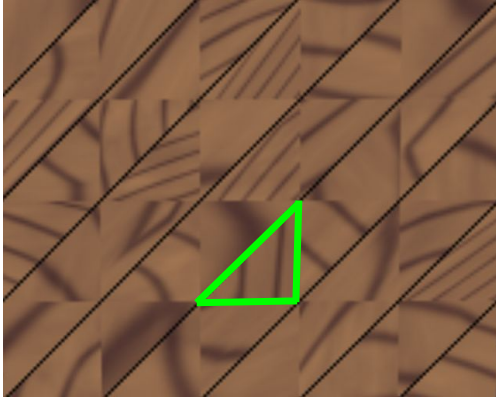


Synthetic rendering

Figure from Debevec, Taylor & Malik
<http://www.debevec.org/Research>

Texture Chart

- Pack triangles into a single image

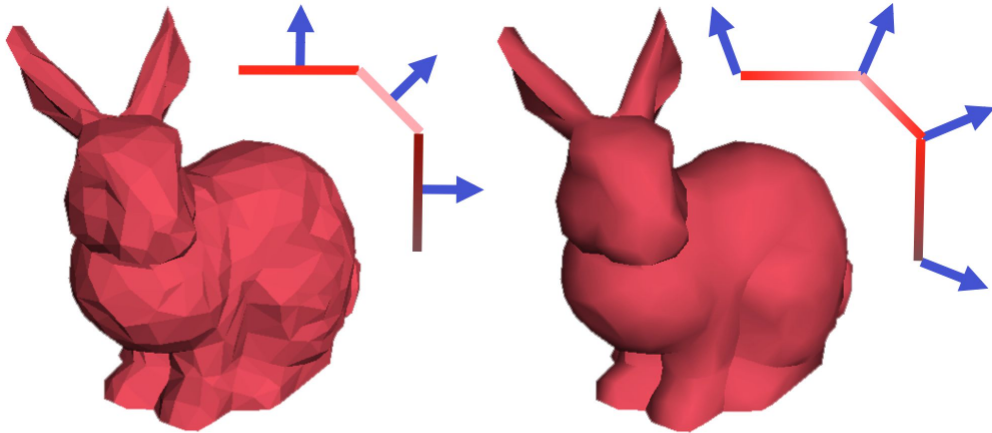


Today

- Worksheet on Real-Time Shadows
- Texture Mapping & Other “Mapping” Techniques
 - Bump Mapping
 - Displacement Mapping
 - Environment Mapping
 - Light Mapping
 - Normal Mapping
 - Parallax Mapping
 - Parallax Occlusion Mapping
- Programmable Shader Examples
 - Modern Graphics Hardware
 - Per-Pixel Shading
- Procedural Textures & Modeling
- Papers for Today
- Papers for Next Time

Remember Gouraud Shading?

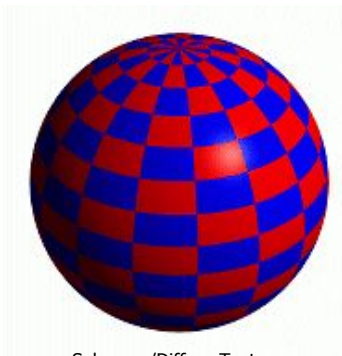
- Instead of shading with the normal of the triangle, we'll shade the vertices with *the average normal* and *interpolate the shaded color* across each face
 - Gives the *illusion of a smooth surface* with smoothly varying normals



Cheat normals to DISGUISE actual geometry

Bump Mapping / Normal Mapping

- Use textures to alter the surface normal
 - Does not change the actual shape of the surface
 - Just shaded as if it were a different shape



Sphere w/Diffuse Texture



Swirly Bump Map

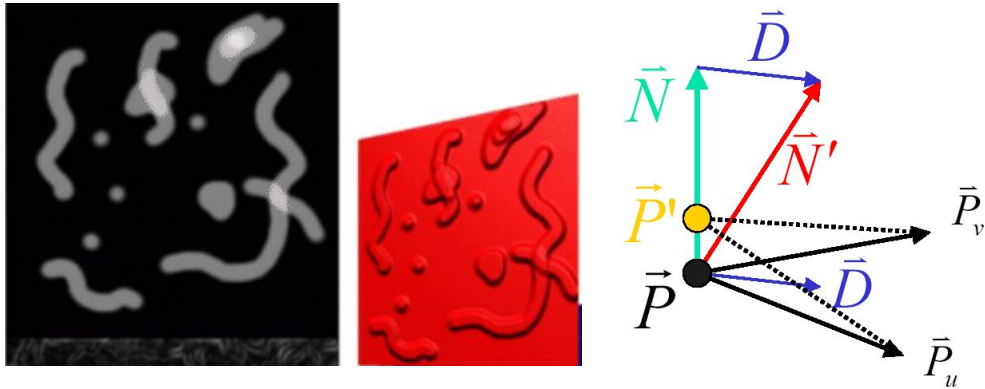


Sphere w/Diffuse Texture & Bump Map

Cheat normals to give illusion of ADDITIONAL/FAKE geometric detail

Bump Mapping

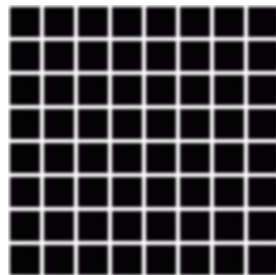
- Treat a **greyscale texture** as a single-valued height function
- Compute the normal from the partial derivatives in the texture



Another Bump Map Example



Cylinder w/Diffuse Texture Map



Bump Map



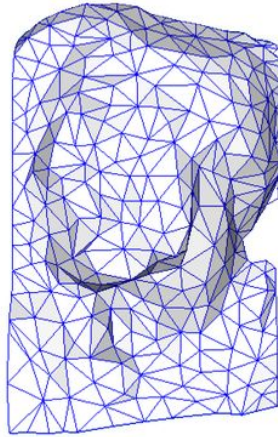
Cylinder w/Texture Map & Bump Map

Normal Mapping

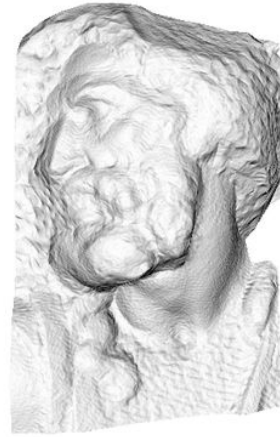
- Variation on Bump Mapping:
Use an **RGB texture** to directly encode the normal



original mesh
4M triangles



simplified mesh
500 triangles

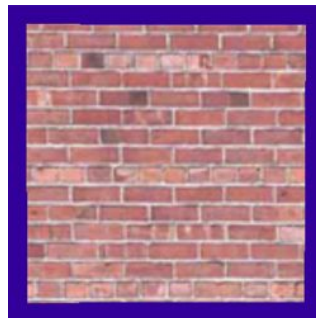


simplified mesh
and normal mapping
500 triangles

http://en.wikipedia.org/wiki/File:Normal_map_example.png

What's Missing?

- There are no bumps on the silhouette of a bump-mapped or normal-mapped object
- Bump/Normal maps don't allow self-occlusion or self-shadowing

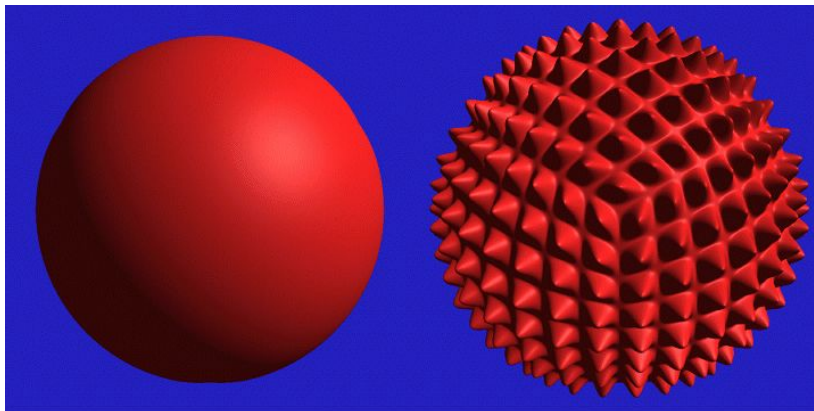


Today

- Worksheet on Real-Time Shadows
- Texture Mapping & Other “Mapping” Techniques
 - Bump Mapping
 - Displacement Mapping
 - Environment Mapping
 - Light Mapping
 - Normal Mapping
 - Parallax Mapping
 - Parallax Occlusion Mapping
- Programmable Shader Examples
 - Modern Graphics Hardware
 - Per-Pixel Shading
- Procedural Textures & Modeling
- Papers for Today
- Papers for Next Time

Displacement Mapping

- Use the texture map to actually move the surface point
- The geometry must be displaced before visibility is determined



Originally a CPU-only, post-user-modeling step

Displacement Mapping

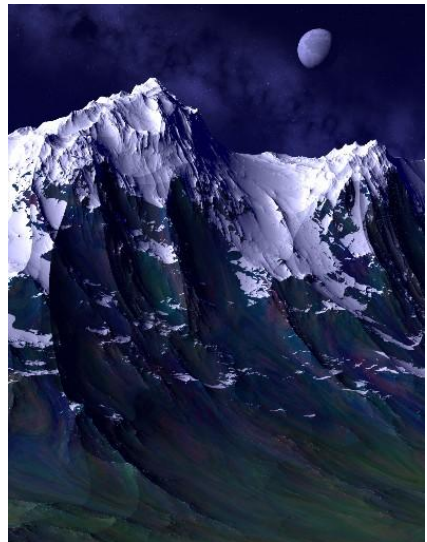


Image from:

*Geometry Caching for
Ray-Tracing Displacement Maps
EGRW 1996
Matt Pharr and Pat Hanrahan*

*note the accurate and detailed
shadows cast by the stones*

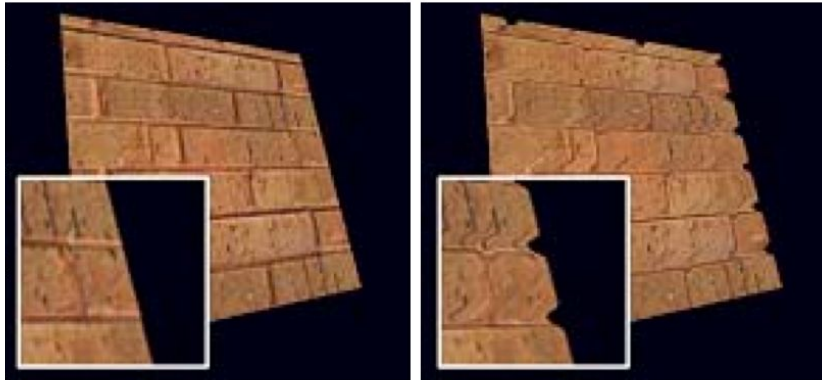
Procedural Displacement Mapping



Ken Musgrave
www.kenmusgrave.com

Parallax Mapping a.k.a. Offset Mapping or Virtual Displacement Mapping

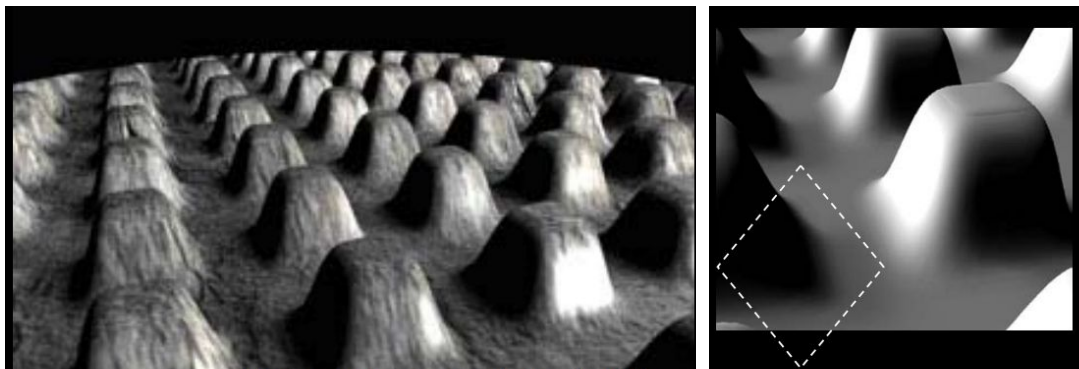
- Displace the texture coordinates for each pixel based on view angle and value of the height map at that point
- At steeper view-angles, texture coordinates are displaced more, giving *illusion of depth* due to parallax effects



“Detailed shape representation with parallax mapping”,
Kaneko et al. ICAT 2001

Parallax Occlusion Mapping

- Brawley & Tatarchuk 2004
- Per pixel ray tracing of the heightfield geometry
- Occlusions & soft shadows



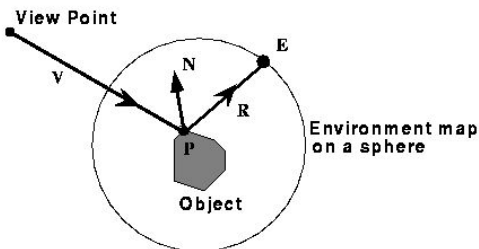
http://developer.amd.com/media/gpu_assets/Tatarchuk-ParallaxOcclusionMapping-Sketch-print.pdf

Today

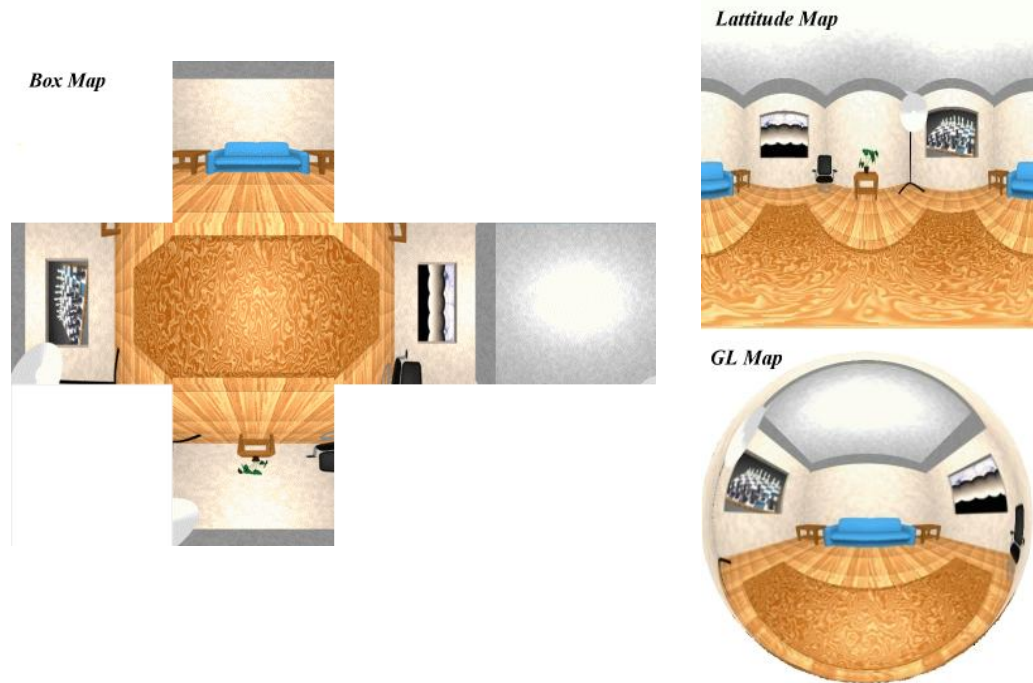
- Worksheet on Real-Time Shadows
- Texture Mapping & Other “Mapping” Techniques
 - Bump Mapping
 - Displacement Mapping
 - Environment Mapping
 - Light Mapping
 - Normal Mapping
 - Parallax Mapping
 - Parallax Occlusion Mapping
- Programmable Shader Examples
 - Modern Graphics Hardware
 - Per-Pixel Shading
- Procedural Textures & Modeling
- Papers for Today
- Papers for Next Time

Environment Maps

- We can simulate reflections by using the direction of the reflected ray to index a spherical texture map at "infinity".
- Assumes that all reflected rays begin from the same point.



What's the Best Chart?



Environment Mapping Example



Terminator II

Texture Maps for Illumination

- Also called "Light Maps"



Quake

Questions?



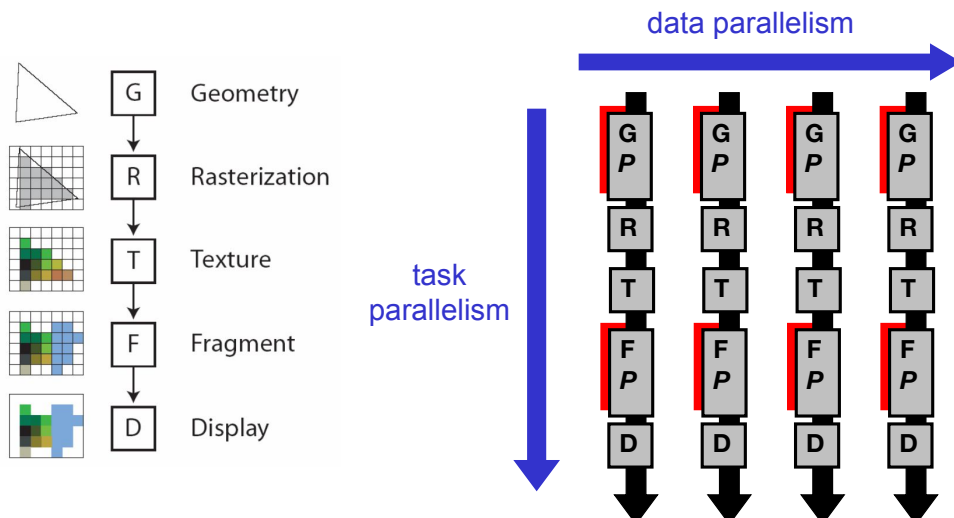
Image by Henrik Wann Jensen
Environment map by Paul Debevec

Today

- Worksheet on Real-Time Shadows
- Texture Mapping & Other “Mapping” Techniques
 - Bump Mapping
 - Displacement Mapping
 - Environment Mapping
 - Light Mapping
 - Normal Mapping
 - Parallax Mapping
 - Parallax Occlusion Mapping
- Programmable Shader Examples
 - Modern Graphics Hardware
 - Per-Pixel Shading
- Procedural Textures & Modeling
- Papers for Today
- Papers for Next Time

Modern Graphics Hardware

- Increased **parallelism**
- **Programmable** geometry and pixel/fragment stages
- General-purpose computation on GPU (GPGPU)



GLSL example: hw4_shader.vs

```
hw4_shader.vs
#version 330 core

// Input vertex data, different for all executions of this shader.
layout(location = 0) in vec3 vertexPosition_modelspace;
layout(location = 1) in vec3 vertexNormal_modelspace;
layout(location = 2) in vec3 vertexColor;

// Output data
out vec3 vertexPosition_worldspace;
out vec3 vertexNormal_worldspace;
out vec3 vertexNormal_cameraspace;
out vec3 EyeDirection_cameraspace;
out vec3 myColor;

// Values that stay constant for the whole mesh.
uniform mat4 MVP;
uniform mat4 V;
uniform mat4 M;
uniform vec3 LightPosition_worldspace;

void main(){

    // Output position of the vertex, in clip space : MVP * position
    gl_Position = MVP * vec4(vertexPosition_modelspace,1);

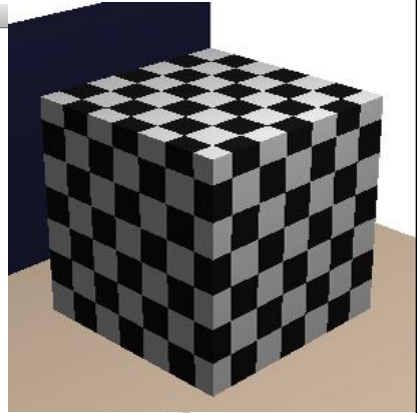
    // Position of the vertex, in worldspace : M * position
    vertexPosition_worldspace = (M * vec4(vertexPosition_modelspace,1)).xyz;

    // Vector that goes from the vertex to the camera, in camera space.
    // In camera space, the camera is at the origin (0,0,0).
    vec3 vertexPosition_cameraspace = (V * M * vec4(vertexPosition_modelspace,1)).xyz;

    EyeDirection_cameraspace = vec3(0,0,0) - vertexPosition_cameraspace;

    vertexNormal_worldspace = normalize (M * vec4(vertexNormal_modelspace,0)).xyz;

    // pass color to the fragment shader
    myColor = vertexColor;
}
```



GLSL example: hw4_shader.fs

```
hw4_shader_checkerboard.fs
in vec3 vertexNormal_worldspace;

// Output data
out vec3 color;

// Values that stay constant for the whole mesh.
uniform vec3 LightPosition_worldspace;
uniform int colormode;
uniform int whichshader;

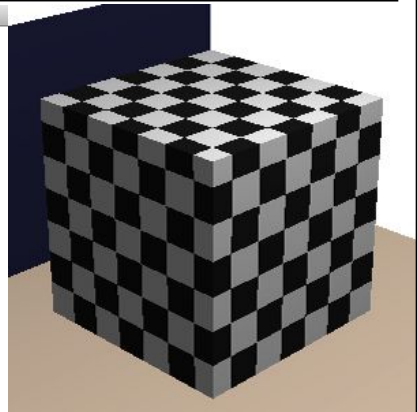
// -----
// a shader for a black & white checkerboard
vec3 checkerboard(vec3 pos) {
    // determine the parity of this point in the 3D checkerboard
    int count = 0;
    if (mod(pos.x,0.3)> 0.15) count++;
    if (mod(pos.y,0.3)> 0.15) count++;
    if (mod(pos.z,0.3)> 0.15) count++;
    if (count == 1 || count == 3) {
        return vec3(0.1,0.1,0.1);
    } else {
        return vec3(1,1,1);
    }
}

// -----
void main(){

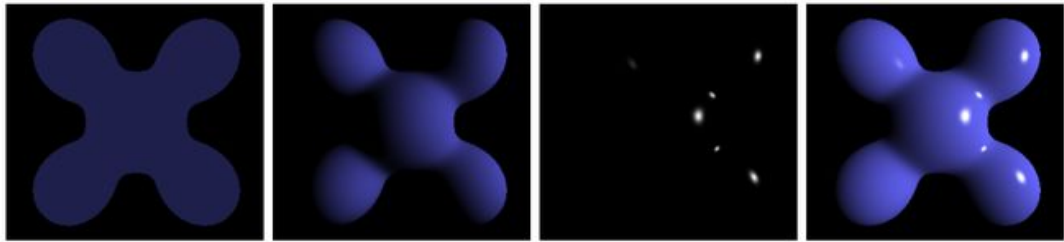
    vec3 LightColor = vec3(1,1,1);
    float LightPower = 4.0f;

    // surface normal
    vec3 surface_normal = vertexNormal_worldspace;

    // Material properties
    vec3 MaterialDiffuseColor = myColor;
    if (whichshader == 1) {
        MaterialDiffuseColor = checkerboard(vertexPosition_worldspace);
    } else if (whichshader == 2) {
        vec3 normalIz;
        MaterialDiffuseColor = orange(vertexPosition_worldspace,surface_normal);
    } else if (whichshader == 3) {
        MaterialDiffuseColor = wood(vertexPosition_worldspace,surface_normal);
    }
}
```



Phong Reflection/Lighting Model



Ambient + Diffuse + Specular = Phong Reflection

$$I_p = k_a i_a + \sum_{m \in \text{lights}} (k_d (\hat{L}_m \cdot \hat{N}) i_{m,d} + k_s (\hat{R}_m \cdot \hat{V})^\alpha i_{m,s})$$

Color & Normal Interpolation

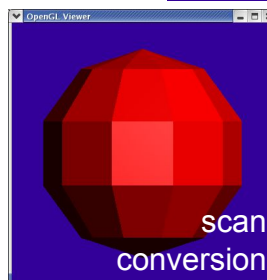
- It's easy in OpenGL to specify different colors and/or normals at the vertices of triangles:
- Why is this useful?



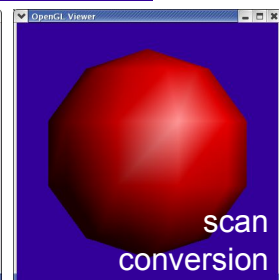
Originally, all we could afford to do in hardware was interpolate colors



ray tracing



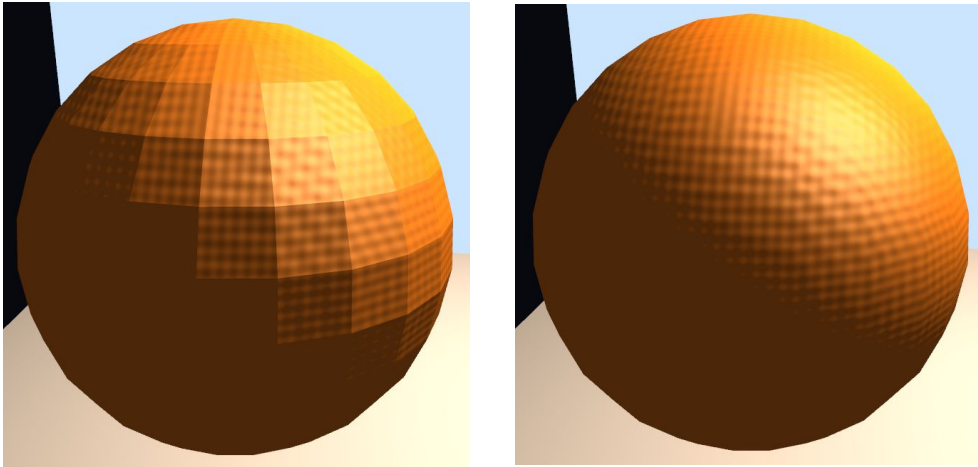
scan conversion



scan conversion

Per-Pixel Shading!

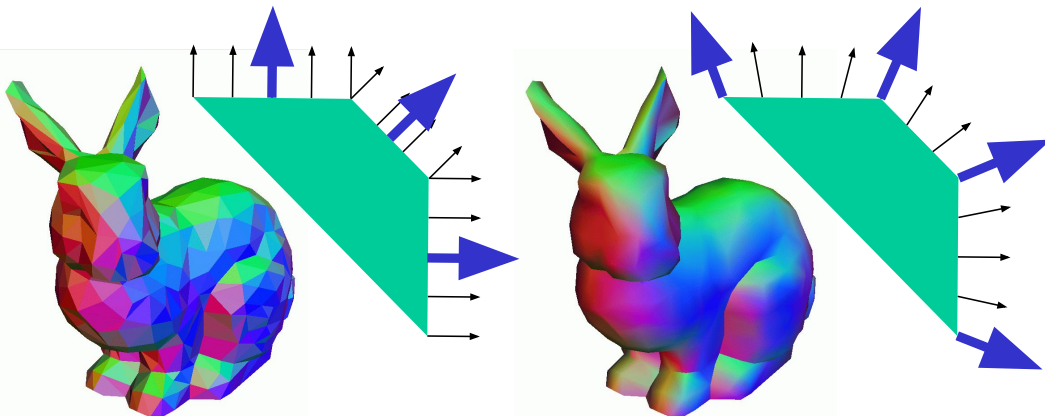
- We are not just interpolating the color
- Phong Reflection/Lighting can be calculated per pixel, not just per vertex



Phong Normal Interpolation

Not Phong
Reflection
Model

- *Interpolate the average vertex normals* across the face and compute *per-pixel shading*
 - Normals should be re-normalized (ensure length=1)



- Before shaders, per-pixel shading was not possible in hardware (Gouraud shading is actually a decent substitute!)

Another GLSL example: orange.vs

```
Emacs@tony.dyn.cs.rpi.edu
varying vec3 normal;
varying vec3 position_eyespace;
varying vec3 position_worldspace;

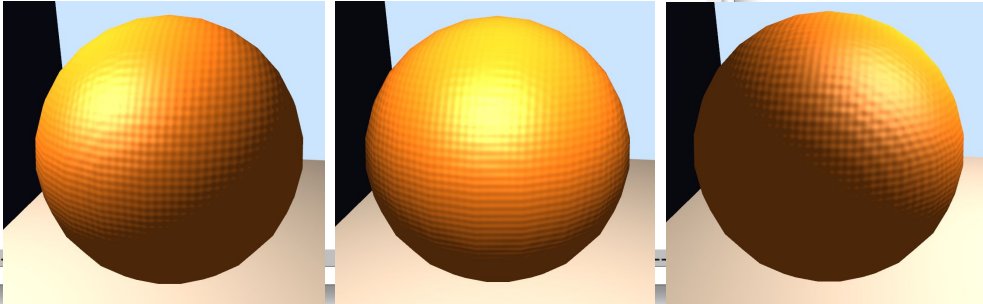
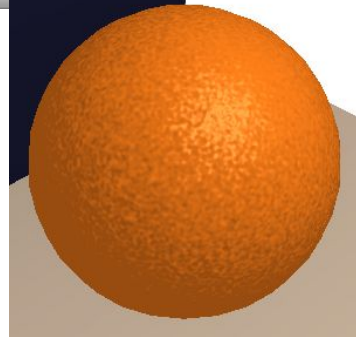
// a shader that looks like orange peel

void main(void) {

    // the fragment shader requires both the world space position (for
    // consistent bump mapping) & eyespace position (for the phong
    // specular highlight)
    position_eyespace = vec3(gl_ModelViewMatrix * gl_Vertex);
    position_worldspace = gl_Vertex.xyz;

    // pass along the normal
    normal = normalize(gl_NormalMatrix * gl_Normal);

    gl_Position = gl_ModelViewProjectionMatrix * gl_Vertex;
}
```



Another GLSL example: orange.fs

```
Emacs@tony.dyn.cs.rpi.edu
varying vec3 normal;
varying vec3 position_eyespace;
varying vec3 position_worldspace;

// a shader that looks like orange peel

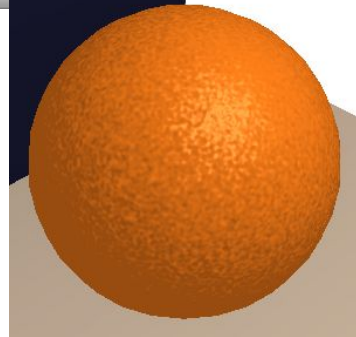
void main (void) {

    // the base color is orange!
    vec3 color = vec3(1.0,0.5,0.1);

    // high frequency noise added to the normal for the bump map
    vec3 normal2 = normalize(normal+0.4*noise3(70.0*position_worldspace));

    // direction to the light
    vec3 light = normalize(gl_LightSource[1].position.xyz - position_eyespace);
    // direction to the viewer
    vec3 eye_vector = normalize(-position_eyespace);
    // ideal specular reflection
    vec3 reflected_vector = normalize(-reflect(light,normal2));

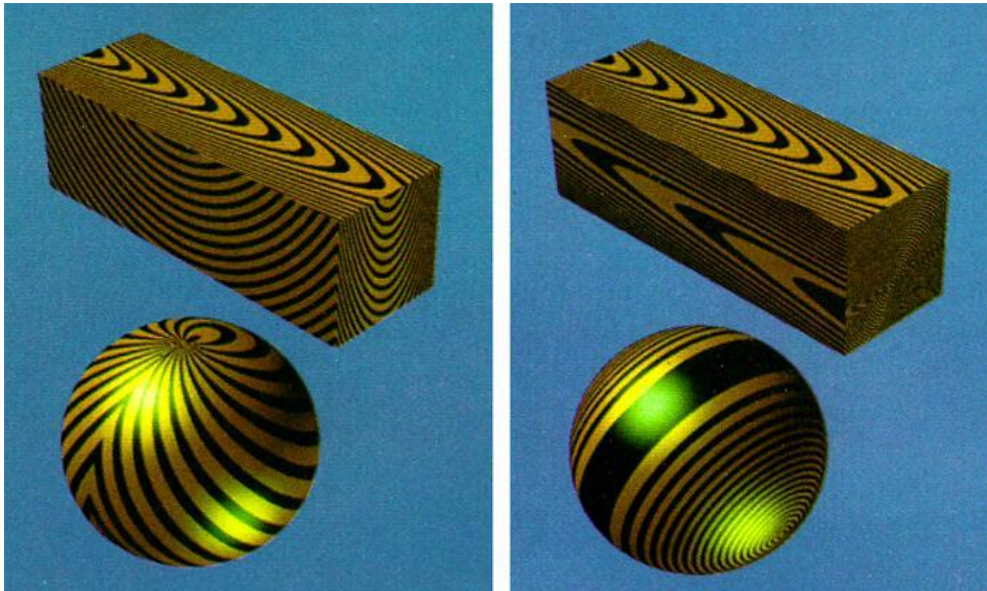
    // basic phong lighting
    float ambient = 0.6;
    float diffuse = 0.4*max(dot(normal2,light),0.0);
    float specular = 0.2 * pow(max(dot(reflected_vector,eye_vector),0.0),10.0);
    vec3 white = vec3(1.0,1.0,1.0);
    color = ambient*color + diffuse*color + specular*white;
    gl_FragColor = vec4 (color, 1.0);
}
```



Today

- Worksheet on Real-Time Shadows
- Texture Mapping & Other “Mapping” Techniques
 - Bump Mapping
 - Displacement Mapping
 - Environment Mapping
 - Light Mapping
 - Normal Mapping
 - Parallax Mapping
 - Parallax Occlusion Mapping
- Programmable Shader Examples
 - Modern Graphics Hardware
 - Per-Pixel Shading
- Procedural Textures & Modeling
- Papers for Today
- Papers for Next Time

Texture Map vs. Solid Texture



“Solid Texturing of Complex Surfaces”,
Peachey, SIGGRAPH 1985

Procedural Textures

$f(x,y,z) \rightarrow \text{color}$

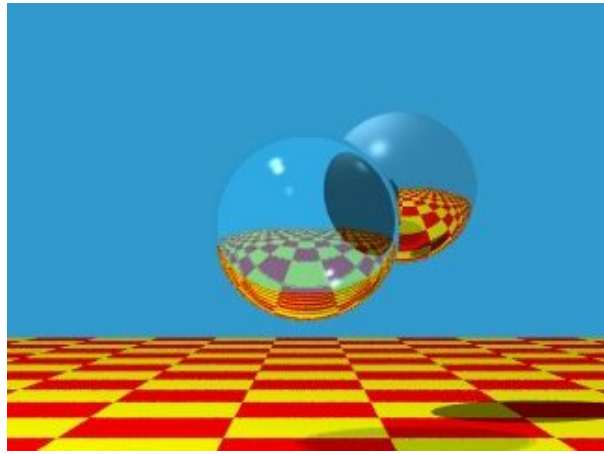
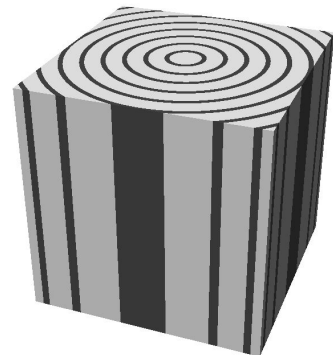
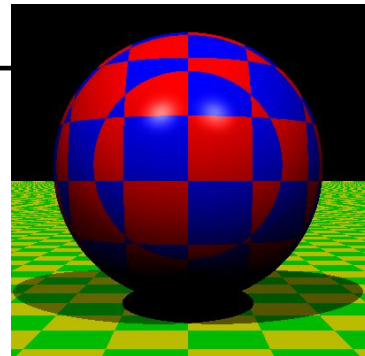


Image by Turner Whitted

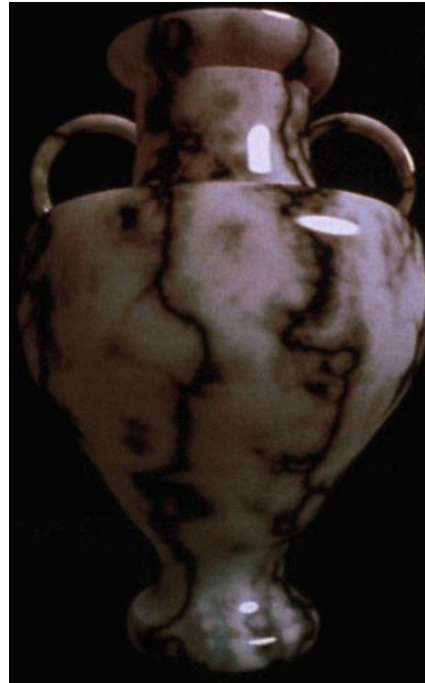
Procedural Textures

- Advantages:
 - easy to implement in ray tracer
 - more compact than texture maps (especially for solid textures)
 - infinite resolution
- Disadvantages
 - non-intuitive
 - difficult to match existing texture



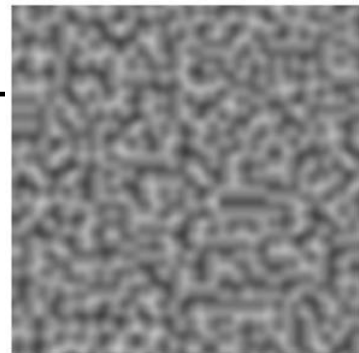
Reading for Today

- “An Image Synthesizer”, Perlin, SIGGRAPH 1985 & “Improving Noise”, Perlin, SIGGRAPH 2002



Perlin Noise

- Properties:
 - Looks “random”, but is deterministic (always returns the same answer for a specific coordinate)
 - Small memory footprint & fast to compute
 - Known amplitude & frequency
 - Smooth interpolation when zoomed in
- Can be combined/layered:
 - Add multiple noise functions w/ different frequencies and amplitudes
 - Simple arithmetic operations (thresholding, sine waves, etc.)



“Shade Trees”, Cook, SIGGRAPH 1984

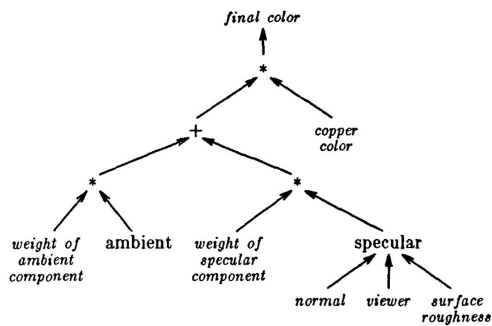


Figure 1a. Shade tree for copper.

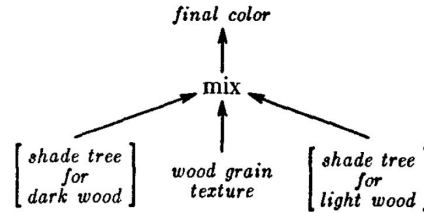
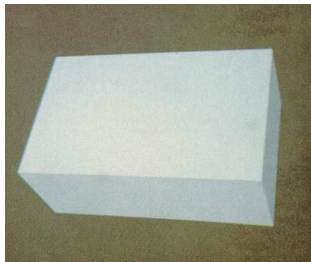
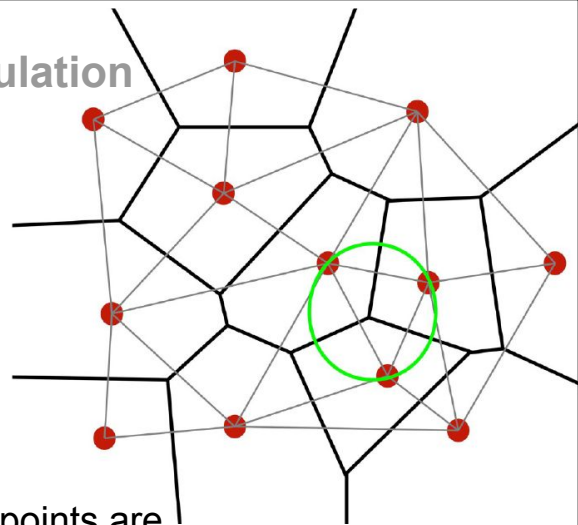


Figure 1b. The mix node in a shade tree for wood.



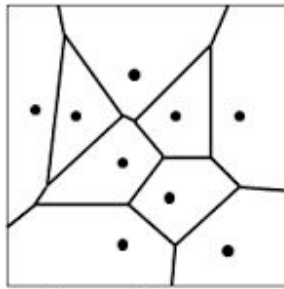
- **Grey: Delaunay Triangulation**

- “Best” triangulation of the red dots (most equilateral)
- A specific triangle is in the Delaunay Triangle *if and only if* the circle defined by those 3 points *does not* contain any other red dot
- Note: Well defined when points are random. If points are on a uniform grid, we have ties...

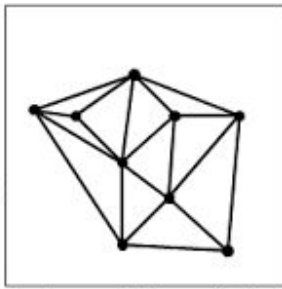


- **Black: Voronoi Diagram**

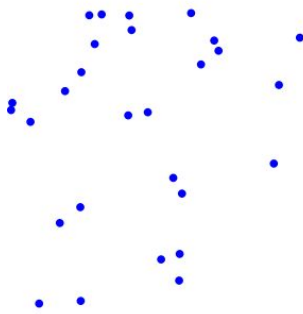
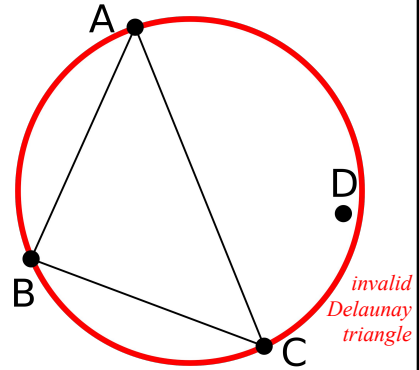
- Each cell is the set of all points in the plane that claim that cell’s red dot as the closest
- Note: The black edges perpendicularly bisect the grey edges



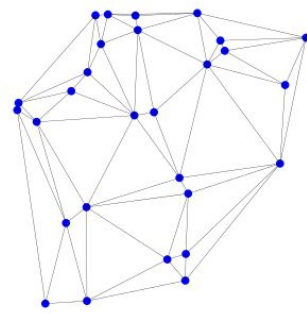
Voronoi Diagram



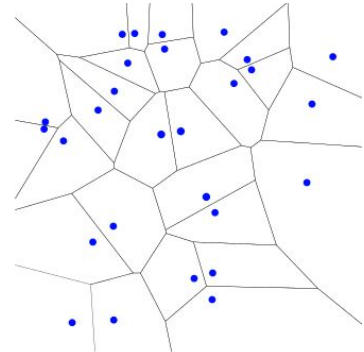
Delaunay Triangulation



Input



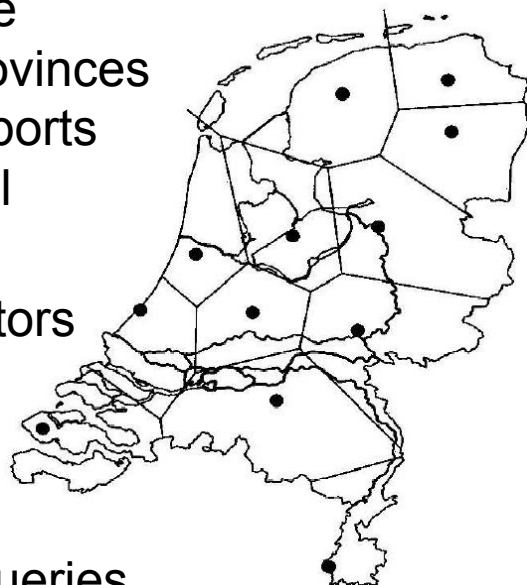
Delaunay Triangulation



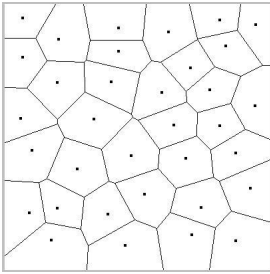
Voronoi Diagram

Voronoi Diagram/Cells/Regions

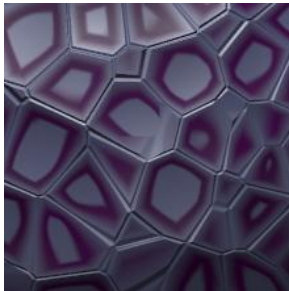
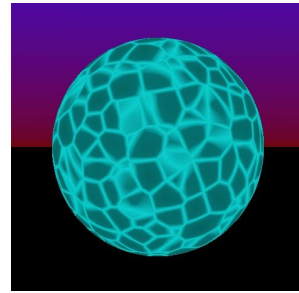
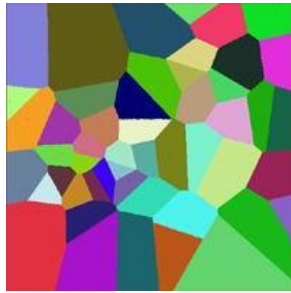
- How to re-district the Netherlands into provinces so that everyone reports to the closest capital
- Cell edges are the perpendicular bisectors of nearby points
- 2D or 3D
- Supports efficient *Nearest Neighbor* queries



Cellular Textures



Voronoi diagram



“A Cellular Texture Basis Function”, Worley, SIGGRAPH 1996

www.worley.com



Questions?

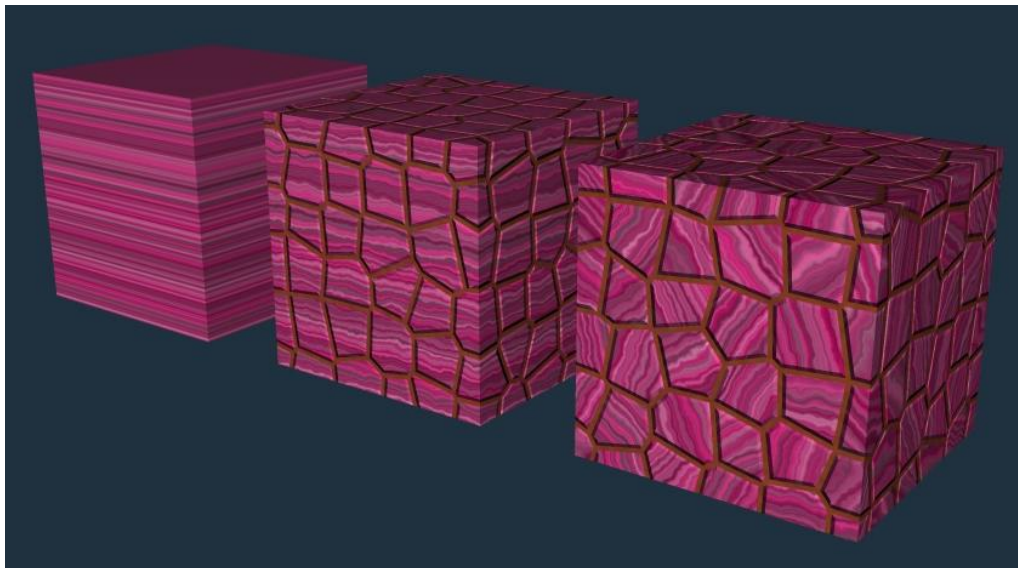


Image by Justin Legakis

Optional Reading for Today

“Hardware-Accelerated Global Illumination by Image Space Photon Mapping” McGuire & Luebke, HPG 2009



Direct Illumination Only

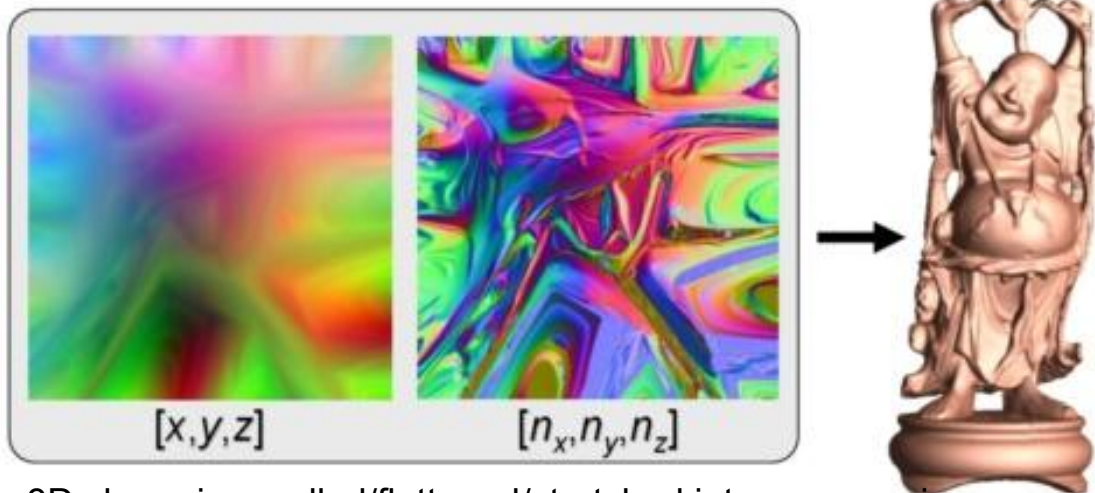
Direct + Constant Ambient

Image Space Photon Mapping

Figure 1: Image-space photon mapping can compute global illumination at interactive rates for scenes with multiple lights, caustics, shadows, and complex BSDFs. This scene renders at 26 Hz at 1920×1080 . (Indirect and ambient intensity are amplified for comparison in this image.)

Optional Reading for Today

"Geometry Images", Gu, Gortler, & Hoppe, SIGGRAPH 2002



3D shape is unrolled/flattened/stretched into a square image.
Stored using existing image formats and compression methods.

Today

- Worksheet on Real-Time Shadows
- Texture Mapping & Other “Mapping” Techniques
 - Bump Mapping
 - Displacement Mapping
 - Environment Mapping
 - Light Mapping
 - Normal Mapping
 - Parallax Mapping
 - Parallax Occlusion Mapping
- Programmable Shader Examples
 - Modern Graphics Hardware
 - Per-Pixel Shading
- Procedural Textures & Modeling
- Papers for Today
- Papers for Next Time

L-Systems

alphabet: {a,b}

initiator: a

production rules:

a → b

b → ba

generations:

a

b

ba

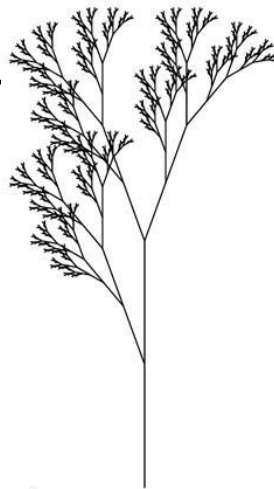
bab

babba

babbabab

babbababbabba

babbababbabababab



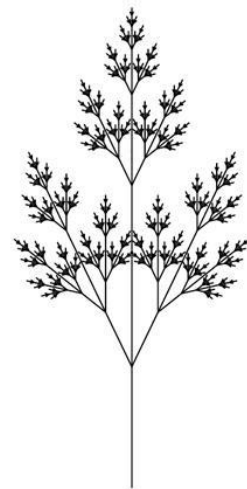
d

$n=7, \delta=20^\circ$

X

$X \rightarrow F [+X] F [-X] +X$

$F \rightarrow FF$



e

$n=7, \delta=25.7^\circ$

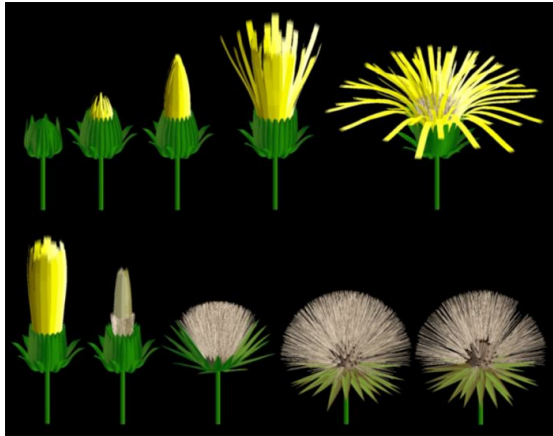
X

$X \rightarrow F [+X] [-X] FX$

$F \rightarrow FF$

Prusinkiewicz & Lindenmayer,
The Algorithmic Beauty of Plants, 1990
<http://algorithmicbotany.org/>

L-Systems

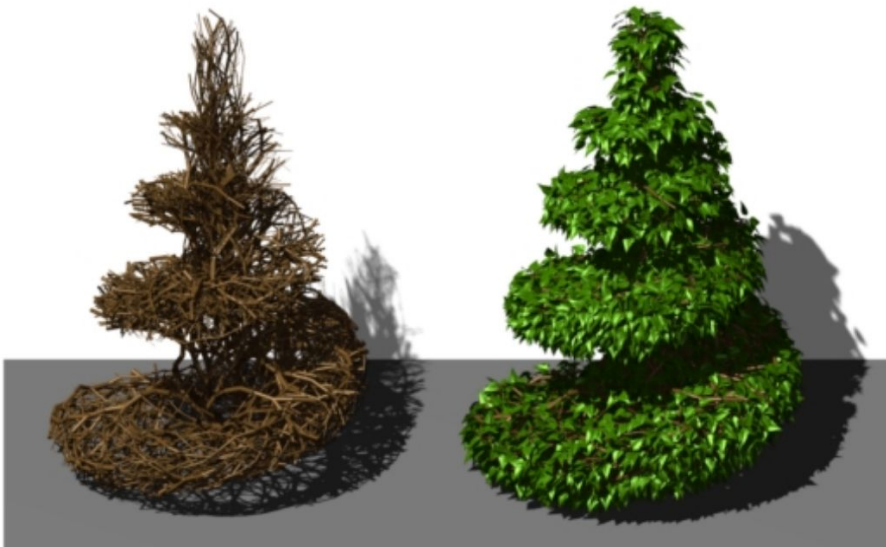


*Animation of Plant
Development*
Prusinkiewicz et al.,
SIGGRAPH 1993

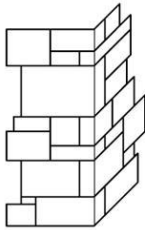
Prusinkiewicz & Lindenmayer,
*The Algorithmic Beauty of
Plants*, 1990
<http://algorithmicbotany.org/>



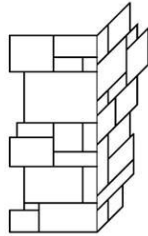
“Synthetic Topiary”, Prusinkiewicz,
James, and Mech, SIGGRAPH 1994



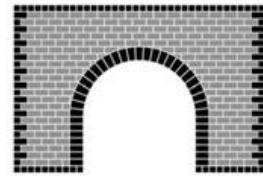
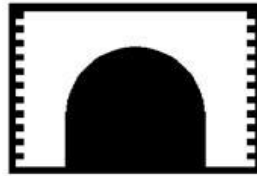
Cellular Texturing for Architecture



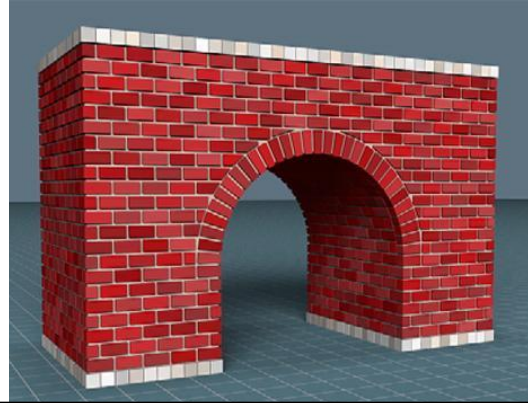
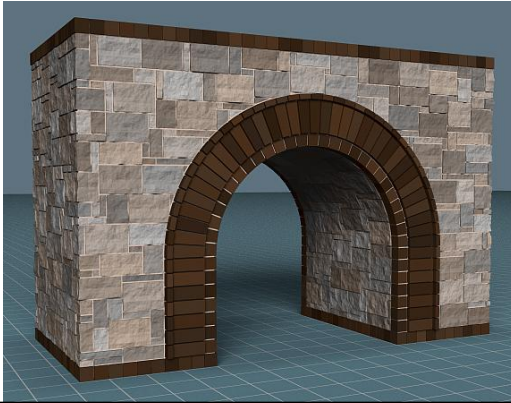
Correct



Incorrect



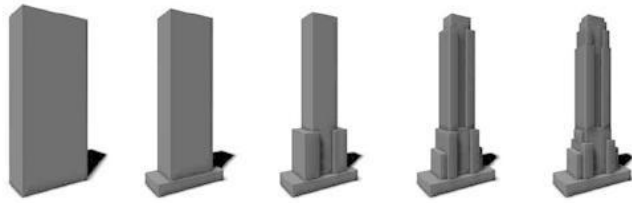
“Feature-Based Cellular Texturing for Architectural Models”, Legakis, Dorsey, & Gortler, SIGGRAPH 2001



Procedural Modeling Advantages

- Small representation
- Generate detail as needed (“infinite”? resolution)
- Great for natural mathematical patterns and man-made engineering and design
- Trivial to make many duplicate objects with small variations

L-Systems for Cities



“Procedural Modeling of Cities”,
Parish & Müller, SIGGRAPH 2001



Procedural Modeling of Buildings



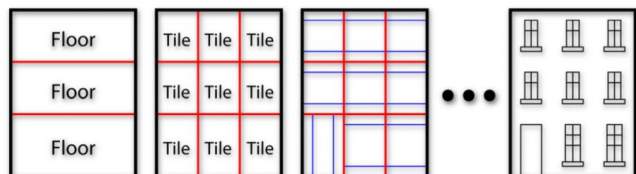
- “Procedural Modeling of Buildings”, Mueller, Wonka, Haegler, Ulmer & Van Gool, SIGGRAPH 2006

Applications

- Entertainment – Gaming
- Education – Studying botanical variation
- Archeological reconstruction
- Realism for Training
- Predicting the future (how will things grow over time)
- Urban planning (preparing for traffic)
- Accommodate for that growth/change

Image-based Procedural Modeling of Facades

- Mueller, Zeng, Wonka, & Van Goo
SIGGRAPH 2007



Input Photograph



Reconstructed 3D Geometry

Questions about Procedural Modeling

- Number of rules necessary?
- Cost in human designer time of creating procedural model?
- Re-useability of procedural model?
- Validation
- Can you build a procedural model that produces a specific target?
 - *From a photo of a specific rare wood grain, can you create a procedural model that creates texture that looks like it came from a different location of the same/similar tree?*