

WEEKLY PARTICIPATION 2: CONDITIONAL INDEPENDENCE

Often we can have a high number of potential features to be used in predicting our target y , e.g. $x \in \mathbb{R}^{1000}$, and a large number of these features may not be relevant to the prediction of the target.

- (a) Let S be indices of some subset of the features, and x_S denote the corresponding random vector. Use the notion of independence to explain concisely with mathematical notation when the features x_S are irrelevant to predicting y .
- (b) More subtly, if we have a good subset of predictors x_G already, then we may say that a candidate set of features x_S doesn't add any additional value on top of x_G in predicting y . Use the notion of conditional independence to explain concisely with mathematical notation when this happens.

Determining independence and conditional independence is useful for *feature selection*: the task of determining a reduced set of features for predicting the target. Feature selection helps reduce the computational effort in machine learning, and can lead to predictive models with lower variance.