Announcements

Updated Rainbow grades

- Quiz 1-4
- HW 1-2

We will be couple of weeks late grading HW3

HW4 out

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Functional Programming with Scheme

Read: Scott, Chapter 11.1-11.3

Lecture Outline

- Functional programming languages
- Scheme
 - S-expressions and lists
 - cons, car, cdr
 - Defining functions
 - Examples of recursive functions
 - Shallow vs. deep recursion
 - Equality testing

Racket/PLT Scheme/DrScheme

- Download Racket (was PLT Scheme (was DrScheme))
 - <u>http://racket-lang.org/</u>
 - Run DrRacket
 - Languages => Choose Language => Other Languages => Legacy Languages: R5RS
- One additional textbook/tutorial:
 - Teach Yourself Scheme in Fixnum Days by Dorai Sitaram:

https://ds26gte.github.io/tyscheme/index.html

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First, Imperative Languages

- The concept of assignment is central
 - X:=5; Y:=10; Z:=X+Y; W:=f(Z);
 - Side effects on memory
- Program semantics (i.e., how the program works): state-transition semantics
 - A program is a sequence of assignment statements with effect on memory (i.e., <u>state</u>)

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Imperative Languages

 $\langle \sigma, l_1: X := f(s) \rangle \longrightarrow \langle \sigma', l_2: \rangle$

- Functions (also called procedures, subroutines, or routines) have side effects: Roughly:
 - A function call affects visible state; i.e., a function call may change state in a way that affects execution of other functions

V, J' is memory,

a mapping from variables to volues. memory Also, result of a function call depends on visible state; i.e., function call is not independent of the context of the call X 7 Y (X may be different thou 41 < 0, l1: X:= f(S)> -> ~~ $\langle \mathbf{O}', \ell_{1S}: Y = f(S) \rangle \rightarrow \dots$

Imperative Languages

- Functions are, traditionally, not first-class values
 - A first-class value is one that can be passed as argument to functions, and returned as result from functions
 - In a language with assignments, it can be assigned into a variable or structure
 - Are functions in C first-class values?
 - As languages become more multi-paradigm, imperative languages increasingly support functions as first-class values (JS, R, Python, Java 8, C++11)

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Functional Languages

- Lambda Calculus
- Program semantics: reduction semantics
 - A program is a set of function definitions and their application to arguments
 - Variables appear as parameters
 - Bound to values at calls

Function composition

Def IP = (Insert +) ° (ApplyToAll *) ° Transpose

(Insert +) ((ApplyToAll *)

(Transpose <<1,2,3>,<6,5,4>>))

(Insert +) ((ApplyToAll *) <<1,6>,<2,5>,<3,4>>) → (Insert +) <6,10,12> →

Functional Languages

- In pure functional languages, there is no notion of assignment, no notion of state
 - Variables are bound to values only through parameter associations
 - No side effects!
- Referential transparency
 - Roughly:
- (fS) at label la and (fS) at label le field the same value. Result of function application is independent of context where the function application occurs; function application (on same argument of course) can be replaced by result

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·(fs)

Functional Languages

- Functions are first-class values
 - Can be returned as value of a function application
 - Can be passed as an argument
 - In a language with assignment, can be assigned into variables and structures
 - Unnamed functions exist as values

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Lisp and Scheme

- Lisp is the second oldest high-level programming language!
 - Simple syntax
 - Program code and data have same syntactic form
 - The S-expression
 - Function application written in prefix form
 - (e1 e2 e3 ... ek) means
 - Evaluate e1 to a function value
 - Evaluate each of e2,...,ek to values
 - Apply the function to these values
 - (+13) evaluates to 4





Why Scheme?

- Simple syntax! Great to introduce core functional programming concepts
 - Reduction semantics
 - Lists and recursion
 - Higher order functions
 - Evaluation order
 - Parametric polymorphism
- Later we'll see Haskell and new concepts
 - Algebraic data types and pattern matching
 - Lazy evaluation
 - Type inference

S-expr ::= Name | Number | ({ S-expr })

 Name is a symbolic constant (a string of chars which starts off with anything that can't start a Number)

FBNF

- Number is an integer or real number
- List of zero or more S-expr's
- E.g., (a (b c) (d)) is a list S-expr

((bc) (d))

a

List Functions

car and cdr

- Given a list, they decompose it into first element, rest-of-list portions
- E.g., car of (a (b c) (d)) is a
- E.g., cdr of (a (b c) (d)) is ((b c) (d))

cons

Given an element and a list, cons builds a new list with the element as its car and the list as its cdr

cons of a and (b) is (a b) (a b) (b) is the empty list

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(cous 'a'b) ->

(a.b)

Quoting

- or quote prevents the Scheme interpreter from evaluating the argument
 - (quote (+ 3 4)) yields (+ 3 4)
- `(+ 3 4) yields (+ 3 4)
- In interpreter: >(cous la (b))
- Whereas (+ 3 4) yields 7
- Why do we need quote?

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Can compose these operators in a short-hand manner. Can reach arbitrary list element by composition of **car**'s and **cdr**'s.

(car (cdr (cdr '((a) b (c d)))))

can also be written

(caddr '((a) b (c d)))

(car (cdr (cdr '((a) b (c d))))) =

(car (cdr '(b (cd))) = (car '((cd))) = (cd)

Questions

Recall cons

E.g., (cons 'a '(b c)) yields (a b c)

Type Predicates

Note the quote: it prevents evaluation of the argument

(symbol? `sam) yields #t (symbol? 1) yields #f
(number? `sam) yields #f (number? 1) yields #t
(list? `(a b)) yields #t (list? `a) yields #f
(null? `()) yields #t (null? `(a b)) yields #f
(zero? 0) yields #t (zero? 1) yields #f

Can compose these.

(zero? (- 3 3)) yields #t Note that since this language is fully parenthesized, there are no precedence problems in expressions!

Question

- What is the typing discipline in Scheme?
 Static or dynamic?
 - Answer: Dynamic typing. Variables are bound to values of different types at runtime. All type checking done at runtime.

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Scheme: Defining Funcitons

Fcn-def ::= <u>(define (Fcn-name {Param}) S-expr)</u> Fcn-name should be a new name for a function. Param should be variable(s) that appear in the S-expr which is the function body.

Fcn-def ::= (define Fcn-name Fcn-value)
Fcn-value ::= (lambda (_{Param}) S-expr)
where Param variables are expected to appear in the
 S-expr; called a lambda expression.

(define (zerocheck? x) (if (= x 0) #t #f))

If-expr ::= (if S-expr0 S-expr1 S-expr2) where S-expr0 must evaluate to a boolean value; if that value is **#t**, then the If-expr yields the result of S-expr1, otherwise it yields the result of S-expr2.

```
(zerocheck? 1) yields #f,
(zerocheck? (* 1 0)) yields #t
```

(define (atom? object)
 (not (pair? object)))

Here **pair**? is a built-in type predicate. It yields **#**t if the argument is a non-trivial S-expr (i.e., something one can take the **cdr** of). It yields **#**f otherwise.

not is the built-in logical operator.

What does **atom?** do?

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(define square (lambda (n) (* n n)))

 Associates the Fcn-name square with the function value (lambda (n) (* n n))

Lambda calculus is a formal theory of functions

 Set of functions definable using lambda calculus (Church 1941) is same as set of functions computable as Turing Machines (Turing 1930's)

Trace of Evaluation

```
(define (atom? object)
  (not (pair? object)) )
```

```
(atom? `(a))
-obtain function value corresponding to atom?
-evaluate `(a) obtaining (a)
-evaluate (not (pair? `(a)))
  -obtain function value corresponding to not
  -evaluate (pair? `(a))
       -obtain function value corresponding to pair?
       -evaluate '(a) obtaining (a)
       -return value #t
  -return #f
-return #f
```

Read-Eval-Print Loop (REPL)

- Scheme interpreter runs read-eval-print loop
 - Read input from user
 - A function application
 - Evaluate input
 - (<mark>e1</mark> e2 e3 ... ek)
 - Evaluate e1 to obtain a function
 - Evaluate e2, ..., ek to values
 - Execute function body using values from previous step as parameter values
 - Return value
 - Print return value



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- (**if** e1 e2 e3)
- (cond (e1 h1) (e2 h2) ... (en-1 hn-1)
 (else hn))
- Cond is like if then else if construct

```
(define (zerocheck? x)
        (cond ((= x 0) #t) (else #f)))
OR
(define (zchk? x)
        (cond ((number? x) (zero? x))
                     (else #f)))
```

Recursive Functions



Recursive Functions

(define (cond	(app)	x y)	V)	app is a shallow recursive function			
(00110	((null? (else		x)	REMEMBER PROLOG? append (CJ, A, A).			
	(cons	(car	x)	append ([AIBJ, C, [AIDJ)) = append (B, C, D).			
		(app	(cdr	x) y)))))			

What does app do?

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Exercise

(define	(len x)							
(cond	((null?	x)	0)	(else	(+ 1	(len	(cdr	x)))))))

Write a version of len that uses if instead of cond

Write a function **countlists** that counts the number of list elements in a list. E.g.,

(countlists `(a)) yields 0
(countlists `(a (b c (d)) (e))) yields 2

Recall (list? 1) returns true if 1 is a list, false otherwise

Recursive Functions



What does **fun** do?

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fun counts atoms in a list

(define (atomcount x) (cond ((null? x) 0) ((atom? x) 1) (else (+ (atomcount (car x)) (atomcount (cdr x))))))

(atomcount '(a)) **yields 1** (atomcount '(1 (2 (3)) (5))) **yields 4**

```
Trace: (atomcount '(1 (2 (3)))

1> (+ (atomcount 1) (atomcount '( (2 (3)))))

2> (+ (atomcount '(2 (3))) (atomcount '()))

3> (+ (atomcount 2) (atomcount '((3)))

4> (+ (atomcount '(3)) (atomcount '()))

5> (+ (atomcount 3) (atomcount '()))
```



Write a function flatten that flattens a list

(flatten `(1 (2 (3)))) yields (1 2 3)

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Equality Testing

eq?

- Built-in predicate that can check atoms for equal values
- Does not work on lists in the way you might expect!

eql?

Our predicate that works on lists
 (define (eql? x y)
 (or (and (atom? x) (atom? y) (eq? x y))
 (and (not (atom? x)) (not (atom? y))
 (eql? (car x) (car y))
 (eql? (cdr x) (cdr y)))))

equal?

Built-in predicate that works on lists



More on Equality Testing next time!

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The End