



Class Analysis, conclusion



Announcements

- Quiz 2
- HW2
 - Post question on Submitty
 - I'm assuming you all have this set up locally
 - Starter code, class analysis framework and worklist algorithm
 - Soot
 - There are already many useful posts



Outline of Today's Class

- Rapid Type Analysis (RTA), last time
- HW2, Class analysis framework questions?
- The XTA analysis family
 - 0-CFA
 - Points-to analysis (PTA)



Class Analysis

- Problem statement: What are the **classes** of objects that a (Java) **reference** variable may refer to?
- Applications
 - Call graph construction
 - Nodes are method
 - Edges represent calling relationships
 - Notion of methods reachable from **main**
 - Virtual call resolution



RTA, A Declarative Specification

R is the set of **reachable methods**

I is the set of **instantiated types**

1. $\{ \text{main} \} \subseteq \mathbf{R}$ // Algo: initialize **R** with **main**

2. for each method $m \in \mathbf{R}$ and
each **new site new C** in **m**

$\{ \mathbf{C} \} \subseteq \mathbf{I}$ // Algo: add **C** to **I**; schedule
// “successor” constraints



RTA, A Declarative Specification

3. for each method $m \in R$,
each **virtual call** $y.n(z)$ in m ,
each class C in $\text{SubTypes}(\text{StaticType}(y)) \cap I$,
and n' , where $n' = \text{resolve}(C, n)$
 $\{ n' \} \sqsubseteq R$ // Algo: add target n' to R , if not already
// there. Schedule “successors”

Worklist Algorithm for Flow-Insensitive Analysis

- Flow-insensitive, context-insensitive analysis

```
S = ... /* initialize S, typically to empty, which is 0 of lattice */
W = { f1, ... fn } /* initialize W with transfer functions in main */
while W ≠ ∅ do {
    remove fj from W
    S = fj(S) /* fj never “kills” */
    if S changed
        W = W U Successors
/* Successors includes all affected transfer functions; easy safe
approximation for us: include all fj's in reachable methods */
}
```



HW2 Class Analysis Framework

- Questions on HW2 class analysis framework?



XTA Analysis Family

- Due to Tip and Palsberg
 - Frank Tip and Jens Palsberg, “Scalable Propagation-Based Call Graph Construction Algorithms”, OOPSLA '00
- Generalizes RTA
- Improves on RTA by keeping more info
 - What if we kept sets per method and per field rather than a “blob” !?



XTA

R is the set of **reachable methods**

S_m is the set of **types** that flow to method **m**

S_f is the set of **types** that flow to field **f**

1. $\{ \text{main} \} \subseteq \mathbf{R}$

2. for each method $\mathbf{m} \in \mathbf{R}$ and
each **new site new C** in **m**

$\{ \mathbf{C} \} \subseteq \mathbf{S}_m$



XTA

3. for each method $m \in R$,
each **virtual call** $y.n(z)$ in m ,
each class C in $\text{SubTypes}(\text{StaticType}(y)) \cap S_m$
and n' , where $n' = \text{resolve}(C, n)$

$\{ n' \} \sqsubseteq R$ // add n' to R if not already there

$\{ C \} \sqsubseteq S_{n'}$ // add C to $S_{n'}$ if not already there

$S_m \cap \text{SubTypes}(\text{StaticType}(p)) \sqsubseteq S_{n'}$

$S_{n'} \cap \text{SubTypes}(\text{StaticType}(\text{ret})) \sqsubseteq S_m$

(p denotes the parameter of n' , and ret
denotes the return of n')



XTA

4. for each method $m \in R$,
each field read $x = y.f$ in m

$$S_f \sqsubseteq S_m$$

5. for each method $m \in R$,
each field write $x.f = y$ in m

$$S_m \cap \text{SubTypes}(\text{StaticType}(f)) \sqsubseteq S_f$$



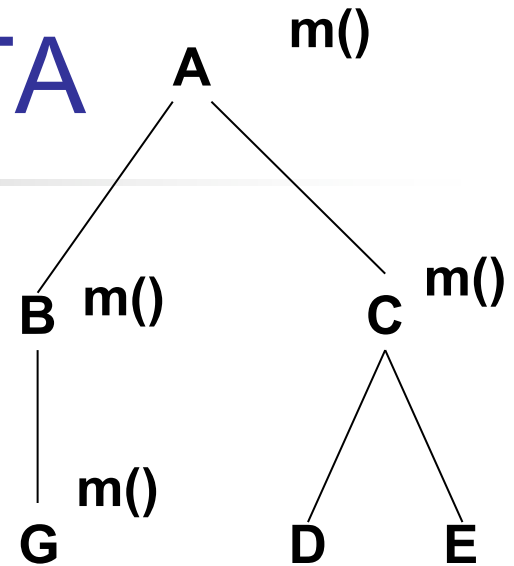
Practical Concerns

- Multiple parameters
- Direct calls
 - either **static invoke** calls or
 - **special invoke** calls
- Array reads and writes!
- Static fields

- See Tip and Palsberg for more

Example: RTA vs. XTA

```
public class A {  
    public static void main() {  
        n1();  
        n2();  
    }  
    static void n1() {  
        A a1 = new B();  
        a1.m();  
    }  
    static void n2() {  
        A a2 = new C();  
        a2.m();  
    }  
}
```



Boolean Expression Hierarchy: RTA vs. XTA vs. “Ground Truth”

```
public class AndExp extends BoolExp {  
    private BoolExp left;  
    private BoolExp right;  
  
    public AndExp(BoolExp left, BoolExp right) {  
        this.left = left;  
        this.right = right;  
    }  
    public boolean evaluate(Context c) {  
        private BoolExp l = this.left;  
        private BoolExp r = this.right;  
        return l.evaluate(c) && r.evaluate(c);  
    }  
}
```

Boolean Expression Hierarchy: RTA vs. XTA vs. “Ground Truth”

```
public class OrExp extends BoolExp {  
    private BoolExp left;  
    private BoolExp right;  
  
    public OrExp(BoolExp left, BoolExp right) {  
        this.left = left;  
        this.right = right;  
    }  
    public boolean evaluate(Context c) {  
        private BoolExp l = this.left;  
        private BoolExp r = this.right;  
        return l.evaluate(c) || r.evaluate(c);  
    }  
}
```


Boolean Expression Hierarchy: RTA vs. XTA vs. “Ground Truth”

```
main() {  
    Context theContext = new Context();  
    BoolExp x = new VarExp("X");  
    BoolExp y = new VarExp("Y");  
    BoolExp exp = new AndExp(  
        new Constant(true), new OrExp(x, y) );  
    theContext.assign(x, true);  
    theContext.assign(y, false);  
    boolean result = exp.evaluate(theContext);  
}
```



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0-CFA

- Described in Tip and Palsberg's paper
- 0-CFA stands for 0-level Control Flow Analysis, where “0-level” stands for **context-insensitive** analysis
 - Will see 1-CFA, 2-CFA, ... k-CFA later
- Improves on XTA by storing even more information about flow of class types



0-CFA

R is the set of **reachable methods**

S_v is the set of **types** that flow to variable v

S_f is the set of **types** that flow to field **f**

1. $\{ \text{main} \} \subseteq \mathbf{R}$

2. for each method $\mathbf{m} \in \mathbf{R}$ and
each **new site** $\mathbf{x} = \text{new } \mathbf{C}$ in \mathbf{m}

$\{ \mathbf{C} \} \subseteq \mathbf{S}_x$



0-CFA

3. for each method $m \in R$,
each **virtual call** $x = y.n(z)$ in m ,
each class C in S_y
and n' , where $n' = \text{resolve}(C, n)$

$$\{ n' \} \sqsubseteq R$$

$$\{ C \} \sqsubseteq S_{\text{this}}$$

$$S_z \cap \text{SubTypes}(\text{StaticType}(p)) \sqsubseteq S_p$$

$$S_{\text{ret}} \cap \text{SubTypes}(\text{StaticType}(x)) \sqsubseteq S_x$$

(**this** is the implicit parameter of n' , p is the parameter of n' , and **ret** is the return of n')



0-CFA

4. for each method $m \in R$,
each **field read** $x = y.f$ in m

$$\mathbf{S}_f \cap \mathbf{SubTypes}(\mathbf{StaticType}(x)) \sqsubseteq \mathbf{S}_x$$

5. for each method $m \in R$,
each **field write** $x.f = y$ in m

$$\mathbf{S}_y \cap \mathbf{SubTypes}(\mathbf{StaticType}(f)) \sqsubseteq \mathbf{S}_f$$



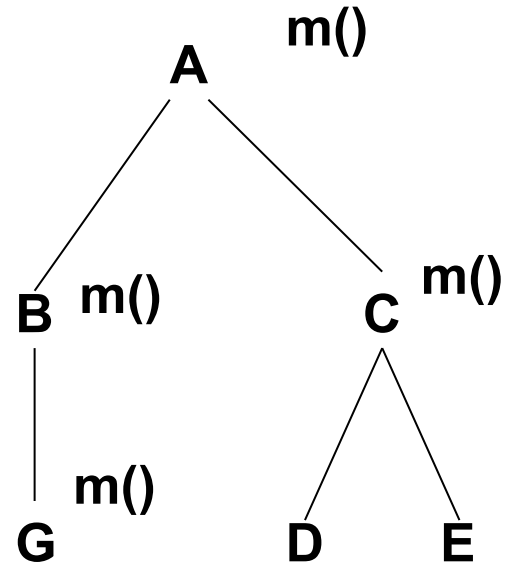
0-CFA

6. for each method $m \in R$,
each assignment $x = y$ in m

$$S_y \cap \text{SubTypes}(\text{StaticType}(x)) \sqsubseteq S_x$$

Example: XTA vs. 0-CFA

```
public class A {  
    public static void main() {  
        A a1 = new B();  
        a1.m();  
  
        A a2 = new C();  
        a2.m();  
    }  
}
```



Boolean Expression Hierarchy: XTA vs. 0-CFA

```
public class AndExp extends BoolExp {
    private BoolExp left;
    private BoolExp right;

    public AndExp(BoolExp left, BoolExp right) {
        this.left = left;
        this.right = right;
    }

    public boolean evaluate(Context c) {
        private BoolExp l = this.left;
        private BoolExp r = this.right;
        return l.evaluate(c) && r.evaluate(c);
    }
}
```

Boolean Expression Hierarchy: XTA vs. 0-CFA

```
public class OrExp extends BoolExp {  
    private BoolExp left;  
    private BoolExp right;  
  
    public OrExp(BoolExp left, BoolExp right) {  
        this.left = left;  
        this.right = right;  
    }  
    public boolean evaluate(Context c) {  
        private BoolExp l = this.left;  
        private BoolExp r = this.right;  
        return l.evaluate(c) || r.evaluate(c);  
    }  
}
```

Boolean Expression Hierarchy: XTA vs. 0-CFA

```
main() {
    Context theContext = new Context();
    BoolExp x = new VarExp("X");
    BoolExp y = new VarExp("Y");
    BoolExp exp = new AndExp(
        new Constant(true), new OrExp(x, y) );
    theContext.assign(x, true);
    theContext.assign(y, false);
    boolean result = exp.evaluate(theContext);
}
```



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PTA

- Widely referred to as Andersen's points-to analysis for Java
- Improves on 0-CFA by storing information about **objects**, not classes
 - `A a1 = new A(); // o1`
 - `A a2 = new A(); // o2`



PTA

R is the set of **reachable methods**

Pt(v) is the set of **objects** that **v** may point to

Pt(o.f) is the set of **objects** that field **f** of object **o** may point to

1. $\{ \text{main} \} \subseteq \mathbf{R}$

2. for each method $\mathbf{m} \in \mathbf{R}$ and
each **new site i: $\mathbf{x} = \text{new C}$** in **m**

$\{ \mathbf{o}_i \} \subseteq \mathbf{Pt}(\mathbf{x})$ // instead of **C**, we have \mathbf{o}_i

PTA

`class_of(o)` returns the class of object `o`

3. for each method $m \in R$,
each virtual call $x = y.n(z)$ in m ,
each class o_i in $Pt(y)$
and n' , where $n' = \text{resolve}(\text{class_of}(o_i), n)$

$\{ n' \} \sqsubseteq R$

$\{ o_i \} \sqsubseteq Pt(\text{this})$

$Pt(z) \cap \text{SubTypes}(\text{StaticType}(p)) \sqsubseteq Pt(p)$

$Pt(\text{ret}) \cap \text{SubTypes}(\text{StaticType}(x)) \sqsubseteq Pt(x)$

(**this** is the implicit parameter of n' , **p** is the parameter of n' , and **ret** is the return of n')



PTA

4. for each method $m \in R$,
each **field read** $x = y.f$ in m

for each object $o \in \text{Pt}(y)$

$$\text{Pt}(o.f) \cap \text{SubTypes}(\text{StaticType}(x)) \sqsubseteq \text{Pt}(x)$$

5. for each method $m \in R$,
each **field write** $x.f = y$ in m

for each object $o \in \text{Pt}(x)$

$$\text{Pt}(y) \cap \text{SubTypes}(\text{StaticType}(f)) \sqsubseteq \text{Pt}(o.f)$$



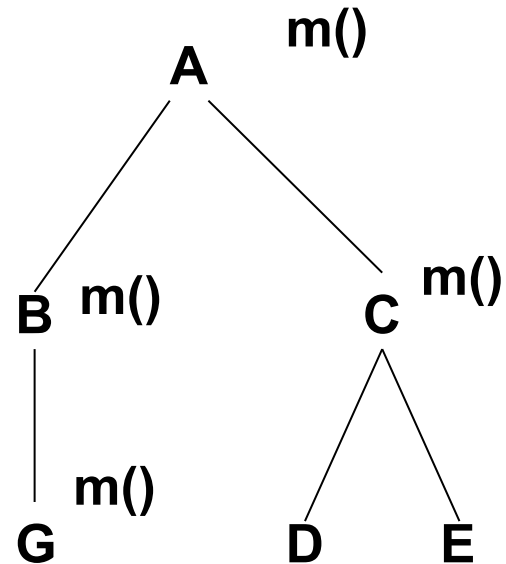
PTA

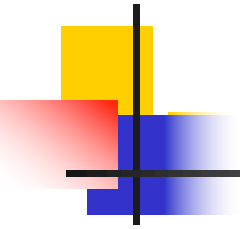
6. for each method $m \in R$,
each **assignment stmt** $x = y$ in m

$$\mathbf{Pt}(y) \cap \mathbf{SubTypes}(\mathbf{StaticType}(x)) \sqsubseteq \mathbf{Pt}(x)$$

Example: 0-CFA vs. PTA

```
public class A {  
    public static void main() {  
        X x1 = new X(); // o1  
        A a1 = new B(); // o2  
        x1.f = a1; // o1.f points to o2  
        A a2 = x1.f; // a2 points to o2  
        a2.m();  
  
        X x2 = new X(); // o3  
        A a3 = new C(); // o4  
        x2.f = a3; // o3.f points to o4  
        A a4 = x2.f; // a4 points to o4  
        a4.m();  
    }  
}
```







The Big Picture

- All fit into our monotone dataflow framework!
- Flow-insensitive, context-insensitive
 - Compute single solution S
- Algorithms differ mainly in “size” of S
 - RTA: only 2 kinds of statements; Lattice?
 - XTA: expands to all statements; Lattice?
 - 0-CFA: all statements; Lattice?
 - PTA (Points-to analysis): all statements; Lattice elements are points-to graphs

The Big Picture

