

# Midterm Exam

## Part I

### 1 A Grammar for Simple Arithmetic Expressions

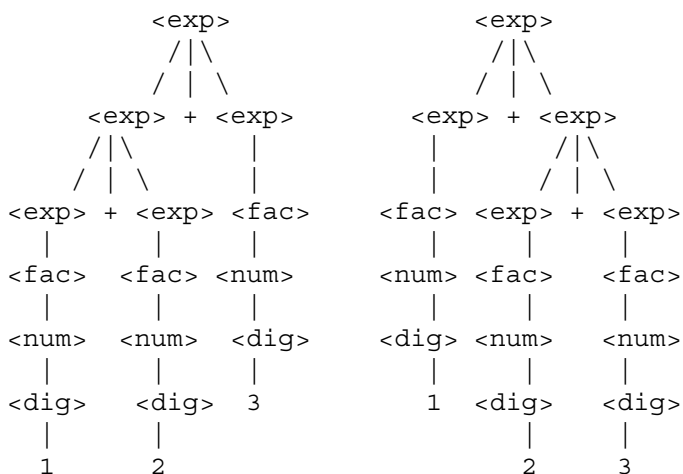
The following is a grammar for simple arithmetic expressions that involve only natural numbers, addition, and multiplication.

$\langle \text{digit} \rangle ::= 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$   
 $\langle \text{number} \rangle ::= \{\langle \text{digit} \rangle\}^+$   
 $\langle \text{expression} \rangle ::= \langle \text{factor} \rangle \mid \langle \text{expression} \rangle + \langle \text{expression} \rangle$   
 $\langle \text{factor} \rangle ::= \langle \text{number} \rangle \mid \langle \text{factor} \rangle * \langle \text{factor} \rangle$

1. What are the tokens of this language? **2 pts**

**Solution.** The tokens of the language are digits and the symbols + and \*.

2. With this grammar, the expression 1+2+3 has two parse trees:



The existence of two parse trees for the same string shows that the grammar is (circle one)

- (a) ambiguous
- (b) context-free
- (c) context-sensitive

**2 pts**

- (d) left-associative
- (e) right-associative

**Solution.** (a)

## 2 Evaluating Simple Arithmetic Expressions

For *evaluation* of expressions by an interpreter (or for code-generation by a compiler), parse trees are not the most convenient representation, because they still contain information about the original string representation that is unnecessary for computation. The following Oz program is a little expression evaluator that assumes its input is in the form of an *abstract syntax tree* constructed from Oz tuples.

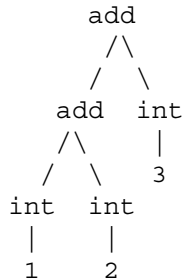
```

fun {Eval X}
  case X
  of int(N) then N
  [] add(X Y) then {Eval X}+{Eval Y}
  [] mul(X Y) then {Eval X}*{Eval Y}
  end
end

```

1. For the first parse tree shown in part 2 of the preceding question, 4 pts  
draw the corresponding abstract syntax tree.

**Solution.**



2. Is the Eval function tail-recursive? Explain. 2 pts

**Solution.** No. In fact, none of the recursive calls is a tail-call.

## 3 Some

Here is a definition of a function that, given a list **Xs** and a function **P**, returns **true** if {**P X**} returns **true** for some element **X** of **Xs** and otherwise it returns **false**.

```

fun {Some Xs P}
  case Xs of
    nil then false
  [] X|Xr then
    if {P X} then true else {Some Xr P} end
    %-----
  end
end

```

1. Rewrite the underlined **if** expression using one of Oz's boolean operators instead. 2 pts

**Solution.**

```
{P X} orelse {Some Xr P}
```

2. One of the functions we wrote as a homework exercise was the **Member** function. **{Member Y Xs}** returns **true** if Y occurs in list Xs and otherwise it returns **false**. Here, instead of writing an independent recursive definition of **Member**, show how to implement it by passing an appropriate function to **Some**. 4 pts

**Solution.**

```

fun {Member Y Xs}
  {Some Xs fun {$ X} Y==X end}
end

```

or

```

fun {Member Y Xs}
  fun {Check X}
    Y==X
  end
  in {Some Xs Check}
end

```

3. We know that Oz function definitions and function calls are linguistic abstractions; they are defined by translation into kernel language procedure definitions and procedure calls. Translate the definition of **Some** into a procedure definition in kernel language syntax. The first part of the translation is given; fill in the rest. (Hint: Be sure your translation reproduces the semantics of the original when there is an error in calling **Some**, with, say, a number instead of a list.) 6 pts

```

Some = proc {$ Xs P B}
  case Xs of
    nil then B=false

```

```
else case Xs of X|Xr then
```

**Solution.**

```
Some = proc {$ Xs P B}
  case Xs of
    nil then B=false
  else case Xs of X|Xr then
    local Q in
      {P X Q}
      if Q then B=true else {Some Xr P B} end
    end
  else raise error('missing else clause') end
end
end
```

## 4 An Abstract Machine Execution

The following sequence of abstract machine states is the beginning of an execution of an Oz (kernel language) statement, expressed in a format similar to one we've used in several lab exercises. Continue the execution to termination.

10 pts

<pre>local Y in   local X in     X=1     local X in       X=2     end     Y=X   end end Env: {}</pre>
<pre>Store: {}</pre>

⇒

<pre> <b>local</b> X <b>in</b>   X=1   <b>local</b> X <b>in</b>     X=2   <b>end</b>   Y=X <b>end</b> Env:{Y → y} </pre>
<pre> Store:{y} </pre>

⇒

<pre> X=1 <b>local</b> X <b>in</b>   X=2 <b>end</b> Y=X Env:{Y → y, X → x} </pre>
<pre> Store:{y, x} </pre>

⇒

<pre> X=1 Env:{Y → y, X → x} </pre>
<pre> <b>local</b> X <b>in</b>   X=2 <b>end</b> Y=X Env:{Y → y, X → x} </pre>
<pre> Store:{y, x} </pre>

⇒

**Solution.**

<b>local X in</b> X=2 <b>end</b> Y=X  Env: {Y → y, X → x}
Store: {y, x = 1}

⇒

<b>local X in</b> X=2 <b>end</b>  Env: {Y → y, X → x}
Y=X
Env: {Y → y, X → x}
Store: {y, x = 1}

⇒

X=2
Env: {Y → y, X → x'}
Y=X
Env: {Y → y, X → x}
Store: {y, x = 1, x'}

⇒

Y=X
Env: {Y → y, X → x}
Store: {y, x = 1, x' = 2}

⇒

Store:  $\{y = 1, x = 1, x' = 2\}$

Terminates.

## Midterm Exam, Part II

### 5 Arity

What does `{Arity r(b:1 a:2 3:7)}` return?

2 pts

**Solution.** 3 a b

(2 pts for this exact answer, 1 pt if these features are listed but in a different order)

### 6 Free and Bound Identifiers

List for each of the following Oz statements the free and bound variable identifiers. (Don't forget: an identifier can be both free and bound in the same statement, because one occurrence of it is free and another occurrence is bound.)

6 pts

1. `{P X Y} local X in {X P Y} end`

Free: \_\_\_\_\_ Bound: \_\_\_\_\_

2. `local X in local Y in {X Y Z} end end`

Free: \_\_\_\_\_ Bound: \_\_\_\_\_

3. `case X of f(Y) then {P Y} else {Q Y} end`

Free: \_\_\_\_\_ Bound: \_\_\_\_\_

**Solution.**

1. Free: P, X, Y; bound: X.

2. Free: Z; bound: X, Y.

3. Free: P, X, Y, Q; bound: Y.

## 7 Producing Power Functions

Consider the following variant of the Pow-function we've seen in lectures and labs.

```
fun {PowFactory X}
  fun {PowAcc N A}
    if N==0 then A
    else {PowAcc N-1 X*A}
    end
  end
  fun {Pow N}
    {PowAcc N 1}
  end
in
  Pow
end
```

1. Write an expression using PowFactory to compute 3 to the 5-th power.

4 pts

**Solution.**

```
local P3 = {PowFactory 3} in {P3 5} end
```

or simply

```
{{PowFactory 3} 5}
```

2. Give the external references for PowAcc

2 pts

**Solution.** PowAcc itself and X.

3. Give the external references for Pow.

2 pts

**Solution.** PowAcc.

## 8 Semantics of exceptions

When an exception is raised in an Oz program by the (kernel language) semantic statement

$$(\text{raise } \langle x \rangle \text{ end}, E)$$

semantic statements are popped off the semantic stack looking for a catch statement.

1. No computation is involved in processing each semantic statement that is popped off, other than checking whether or not it is a catch. In C++, on the other hand, the corresponding way of raising an exception (with a `throw` statement) must process each popped stack frame to call the destructors of all objects referenced in the stack frame. Explain why this is necessary in a C++ program but not in an Oz program.

4 pts

**Solution.** The main point to note in the answer is that C++ doesn't have automatic garbage collection, while Oz does. As discussed in class, since C++ doesn't have it, the referenced object destructors have to be called since otherwise there could be a memory leak. In Oz, on the other hand, when a store variable is no longer accessible (no environment on the semantic stack has a binding that maps to it or to a record containing it), the garbage collector will reclaim it.

2. Assuming

$$(\text{catch } \langle y \rangle \text{ then } \langle s \rangle \text{ end}, E_c)$$

is the `catch` statement found, which of the following is the semantic statement pushed on the semantic stack as the last step of processing the `raise` statement? (Hint: Only one of these really makes any sense, if you remember how environments are used in the abstract machine.)

4 pts

- (a)  $(\langle s \rangle, E + \{\langle y \rangle \rightarrow E_c(\langle x \rangle)\})$
- (b)  $(\langle s \rangle, E + \{\langle y \rangle \rightarrow E(\langle x \rangle)\})$
- (c)  $(\langle s \rangle, E_c + \{\langle y \rangle \rightarrow E(\langle x \rangle)\})$
- (d)  $(\langle s \rangle, E_c + \{\langle y \rangle \rightarrow E_c(\langle x \rangle)\})$

**Solution.** (c)

## 9 A Translation Attempt

The semantics of the try-finally statement in Oz

```
try <s>1 finally <s>2 end
```

is defined by translating it into a kernel language try-catch:

```
try
  <s>1
catch X then
  <s>2
  raise X end
end
<s>2
```

If `<s>2` is a large statement (perhaps composed of dozens of smaller statements), it's a problem that this translation duplicates it. Consider the following alternative translation that uses a boolean variable to keep track of whether an exception has occurred in order to avoid duplicating `<s>2`:

```
local ExceptionOccurred SavedException in
  ExceptionOccurred=true
  try
    <s>1
    ExceptionOccurred = false
  catch X then
    SavedException=X
  end
  <s>2
  if ExceptionOccurred then
    raise SavedException end
  end
end
```

However, this statement does **not** have the same semantics as the first translation. Why not? Make your answer precise by describing a case where the two statements would execute differently.

6 pts

**Solution.** Assume that neither `<s>1` nor `<s>2` raises an exception. With the first translation, both are executed and no exception is raised. But with the second translation, there are two assignments, with different values, to `ExceptionOccurred`. Since it's a single assignment variable, the second assignment itself raises an exception, which will be caught by the catch statement and re-raised at the end.