TABLE 6 Logical Equivalences.	
Equivalence	Name
$p \wedge \mathbf{T} \equiv p$ $p \vee \mathbf{F} \equiv p$	Identity laws
$p \lor \mathbf{T} \equiv \mathbf{T}$ $p \land \mathbf{F} \equiv \mathbf{F}$	Domination laws
$p \lor p \equiv p$ $p \land p \equiv p$	Idempotent laws
$\neg(\neg p) \equiv p$	Double negation law
$p \lor q \equiv q \lor p$ $p \land q \equiv q \land p$	Commutative laws
$(p \lor q) \lor r \equiv p \lor (q \lor r)$ $(p \land q) \land r \equiv p \land (q \land r)$	Associative laws
$p \lor (q \land r) \equiv (p \lor q) \land (p \lor r)$ $p \land (q \lor r) \equiv (p \land q) \lor (p \land r)$	Distributive laws
$\neg (p \land q) \equiv \neg p \lor \neg q$ $\neg (p \lor q) \equiv \neg p \land \neg q$	De Morgan's laws
$p \lor (p \land q) \equiv p$ $p \land (p \lor q) \equiv p$	Absorption laws
$p \lor \neg p \equiv \mathbf{T}$ $p \land \neg p \equiv \mathbf{F}$	Negation laws

TABLE 1 Rules of Inference.		
Rule of Inference	Tautology	Name
$ \begin{array}{c} p \\ p \to q \\ \therefore \overline{q} \end{array} $	$(p \land (p \to q)) \to q$	Modus ponens
$ \begin{array}{c} \neg q \\ p \to q \\ \therefore \neg p \end{array} $	$(\neg q \land (p \to q)) \to \neg p$	Modus tollens
$p \to q$ $q \to r$ $\therefore p \to r$	$((p \to q) \land (q \to r)) \to (p \to r)$	Hypothetical syllogism
$ \begin{array}{c} p \lor q \\ \neg p \\ \therefore \overline{q} \end{array} $	$((p \lor q) \land \neg p) \to q$	Disjunctive syllogism
$\therefore \frac{p}{p \vee q}$	$p \to (p \lor q)$	Addition
$\therefore \frac{p \wedge q}{p}$	$(p \land q) \to p$	Simplification
$ \frac{p}{q} \therefore \overline{p \wedge q} $	$((p) \land (q)) \to (p \land q)$	Conjunction
$p \vee q$ $\neg p \vee r$ $\therefore \overline{q \vee r}$	$((p \lor q) \land (\neg p \lor r)) \to (q \lor r)$	Resolution

TABLE 7 Logical Equivalences Involving Conditional Statements.

$$p \to q \equiv \neg p \lor q$$

$$p \to q \equiv \neg q \to \neg p$$

$$p \lor q \equiv \neg p \to q$$

$$p \land q \equiv \neg (p \to \neg q)$$

$$\neg (p \to q) \equiv p \land \neg q$$

$$(p \to q) \land (p \to r) \equiv p \to (q \land r)$$

$$(p \to r) \land (q \to r) \equiv (p \lor q) \to r$$

$$(p \to q) \lor (p \to r) \equiv p \to (q \lor r)$$

$$(p \to r) \lor (q \to r) \equiv (p \land q) \to r$$

TABLE 8 Logical Equivalences Involving Biconditional Statements.

$$p \leftrightarrow q \equiv (p \to q) \land (q \to p)$$

$$p \leftrightarrow q \equiv \neg p \leftrightarrow \neg q$$

$$p \leftrightarrow q \equiv (p \land q) \lor (\neg p \land \neg q)$$

$$\neg (p \leftrightarrow q) \equiv p \leftrightarrow \neg q$$

TABLE 2 Rules of Inference for Quantified Statements.Rule of InferenceName $\frac{\forall x P(x)}{P(c)}$ Universal instantiation $\frac{P(c) \text{ for an arbitrary } c}{\forall x P(x)}$ Universal generalization $\frac{\exists x P(x)}{P(c) \text{ for some element } c}$ Existential instantiation $\frac{P(c) \text{ for some element } c}{\exists x P(x)}$ Existential generalization