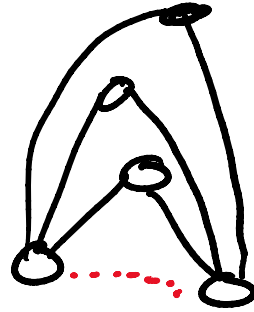


Last class:

- Triadic closure



- Homophily \rightarrow selection
influence

- Temporal networks

\rightarrow changes over time

Today: strength of ties
diffusion

Strong vs. weak ties

strong vs. weak \Rightarrow strength of links/
edge weight

- # of communications

- Time spent together

- etc.

Example: Story o'clock



Empirically: job seekers found

Empirically: job seekers found
open positions more often
through acquaintances than
close friends

Why? Consider the structure
of a social



→ dense
clusters
which are
loosely coupled

→ information spreads through
links connecting those
clusters

strong tie: strong connection
(usually internal to cluster)

weak tie: weaker connection
(connecting clusters)

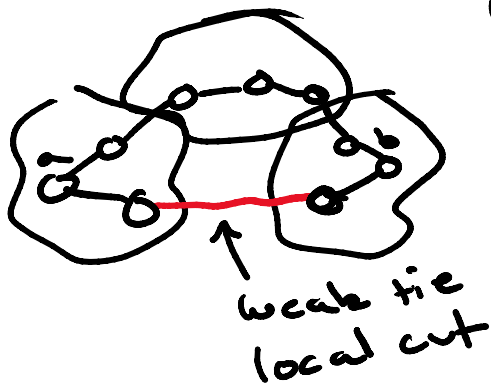
Connectivity

→ weak ties = cut edges

not necessarily, more likely as

→ weak ...
not necessarily, more likely as
a whole

→ However, we have the notion
of "local bridges" or a
local cut



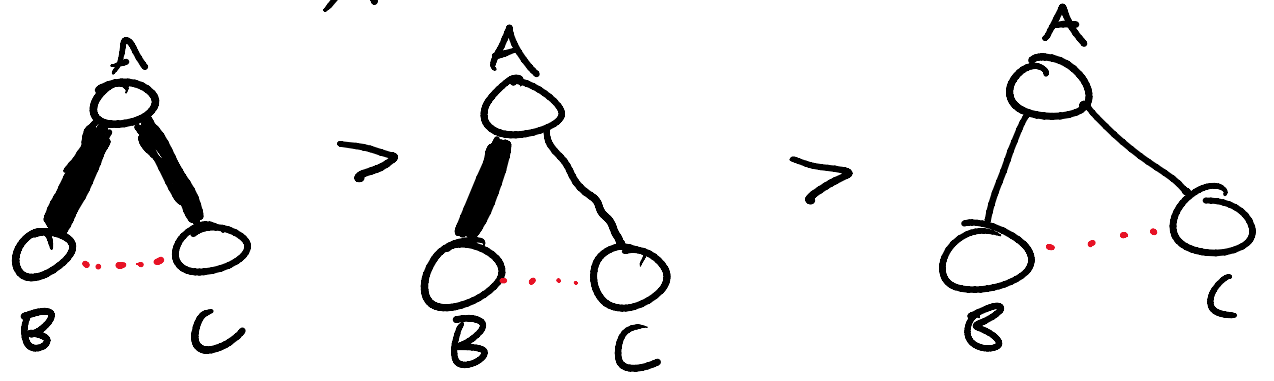
↳ removing a local cut
increases shortest
path distances for
some vertex pair

How do ties relate to
triadic closure?

Strong triadic closure property

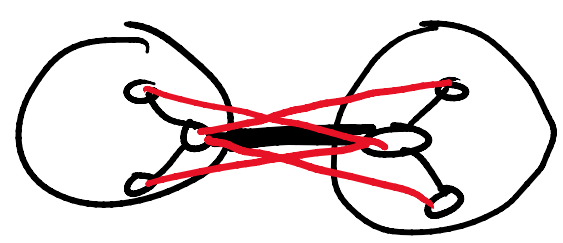
If A is connected to B, C via
strong ties and B, C aren't
connected, there's a higher
likelihood edge (B, C) is
created than if at least one
of A 's ties was weak.

of A's ties was weak



Think of weak ties \rightarrow local bridges

If a local bridge is a strong tie \rightarrow the surrounding neighborhood is likely to become more tightly coupled



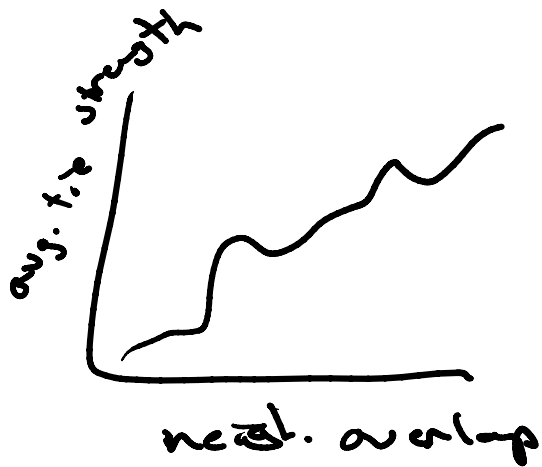
Let's quantify this:

Let $\gamma = \frac{1}{N} \sum_{i,j} w_{ij}$

- Consider a weighted network

First: correlate neighborhood overlaps with tie strength

Second: remove ties from $w \rightarrow s$ and $s \rightarrow w$ and observe connectivity



Diffusive processes

Generally: we're considering how information, data, etc. spread through some networks

Basic models:

Vertex-centric behavior

$\rightarrow v$ updates its state based off of that state of $N(v,r)$

→ v updates its state based off of that state of $N(v)$
Complexity of dynamics depends on complexity of each vertex's updating

→ small local change can have large global change

Simple example: Label propagation

Our algorithm

For $v \in V(G)$: ← vertex id
1...n
State[v] = vid(v)

while updates happen:

For $v \in V(G)$:

counts = {}

For $u \in N(v)$:

counts[state[u]] += 1

State[v] = argmax(counts)

Q: How are diffusion and network ties related?

→ cutting weak ties increases

→ cutting weak ties increases
avg. shortest paths length
→ increase steps for a diffusive
process to spread

→ disconnecting graph stops process

Think: network resilience

* we can strategically cut a
network if that is our goal
(future: epidemiology)

Growth models

Note: the impact of all our
observations is dependent on
an underlying growth process

Many networks grow via "preferential
attachment" (P.A.)
- P.A. = higher likelihood of
attachment to higher degree
verts
aka 'Rich get richer'

- 10 1 . 1 1 1 . 1 1

aka $n \sim \gamma$

- Barabasi-Albert model
start with n_0 vertices
attach new vertex v to some
existing vertex u with probability

$$p_{uv} = \frac{d(u)}{\sum_{i \in V(G)} d(i)}$$

→ all of this explains
degree skew

To summarize:

Triadic closure:

→ clustering coefficient increases

→ existence of communities

Useful for link prediction

Homophily:

→ clusters become more homogeneous

→ selection and influence

useful for vertex classification

Preferential attachment:

Preferential attachment:

→ existence of hubs

→ degree skew

→ rich get richer

useful for
link prediction

Weak vs. strong ties:

→ strong triadic closure

→ diffusive processes "jump"
between clusters via
weak ties