

Actors (PDCS 4)

AMST actor language syntax, semantics, join
continuations

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Advantages of concurrent programs

- **Reactive programming**
 - User can interact with applications while tasks are running, *e.g.*, stopping the transfer of a large file in a web browser.
- **Availability of services**
 - Long-running tasks need not delay short-running ones, *e.g.*, a web server can serve an entry page while at the same time processing a complex query.
- **Parallelism**
 - Complex programs can make better use of hardware resources in multi-core processor architectures, SMPs, LANs, WANs, grids, and clouds, *e.g.*, scientific/engineering applications, simulations, games, etc.
- **Controllability**
 - Tasks requiring certain preconditions can suspend and wait until the preconditions hold, then resume execution transparently.

Disadvantages of concurrent programs

- **Safety**
 - « *Nothing bad ever happens* »
 - Concurrent tasks should not corrupt consistent state of program.
- **Liveness**
 - « *Anything ever happens at all* »
 - Tasks should not suspend and indefinitely wait for each other (deadlock).
- **Non-determinism**
 - Mastering exponential number of interleavings due to different schedules.
- **Resource consumption**
 - Concurrency can be expensive. Overhead of scheduling, context-switching, and synchronization.
 - Concurrent programs can run *slower* than their sequential counterparts even with multiple CPUs!

Overview of concurrent programming

- There are four main approaches:
 - Sequential programming (no concurrency)
 - Declarative concurrency (streams in a functional language)
 - Message passing with active objects (Erlang, SALSA)
 - Atomic actions on shared state (Java, C++)
- The atomic action approach is the *most difficult*, yet it is the one you will probably be most exposed to!
- But, if you have the choice, which approach to use?
 - Use the simplest approach that does the job: sequential if that is ok, else declarative concurrency if there is no observable nondeterminism, otherwise use actors and message passing.

Agha, Mason, Smith & Talcott

1. Extend a functional language (call-by-value λ calculus + `ifs` and `pairs`) with actor primitives.
2. Define an operational semantics for actor configurations.
3. Study various notions of equivalence of actor expressions and configurations.
4. Assume fairness:
 - Guaranteed message delivery.
 - Individual actor progress.

Open Distributed Systems

- Addition of new components
- Replacement of existing components
- Changes in interconnections

Synchronous vs. Asynchronous Communication

- The π -calculus (and other process algebras such as CCS, CSP) uses synchronous communication.
- The actor model assumes asynchronous communication is *the most* primitive interaction mechanism.

Communication Medium

- In the π -calculus, channels are explicitly modeled. Multiple processes can share a channel, potentially causing interference.
- In the actor model, the communication medium is not explicit. Actors (active objects) are first-class, history-sensitive (stateful) entities with an explicit identity used for communication.

Fairness

- The actor model theory assumes fair computations:
 1. Message delivery is guaranteed.
 2. Infinitely-often enabled computations must eventually happen.

Fairness is very useful for reasoning about equivalences of actor programs but can be hard/expensive to guarantee; in particular when distribution, mobility, and failures are considered.

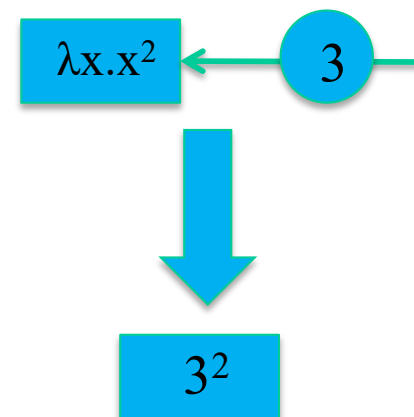
λ -Calculus as a Model for Sequential Computation

Syntax:

e	$::=$	v	<i>variable</i>
		$\lambda v . e$	<i>function</i>
		$e(e)$	<i>application</i>

Example of beta-reduction:

$$\lambda x . x^2 (3) \longrightarrow x^2 \{3/x\}$$



λ -Calculus extended with pairs

- $\text{pr}(x, y)$ *returns a pair containing x & y*
- $\text{ispr}(x)$ *returns t if x is a pair; f otherwise*
- $1^{\text{st}}(\text{pr}(x, y)) = x$ *returns the first value of a pair*
- $2^{\text{nd}}(\text{pr}(x, y)) = y$ *returns the 2nd value of a pair*

Actor Primitives

- `send(a, v)`
 - Sends value v to actor a .
- `new(b)`
 - Creates a new actor with behavior b (a λ -calculus functional abstraction) and returns the identity/name of the newly created actor.
- `ready(b)`
 - Becomes ready to receive a new message with behavior b .

AMST Actor Language

Examples

`b5 = rec(λy.λx.seq(send(x, 5), ready(y)))`
receives an actor name `x` and sends the number 5 to that actor, then it becomes ready to process new messages with the same behavior `y` (`b5`).

Sample usage:

```
send(new(b5), a)
```

A *sink*, an actor that disregards all messages:

```
sink = rec(λb.λm.ready(b))
```

Reference Cell

```
cell =  
rec (λb.λc.λm.if (get?(m),  
                seq (send (cust(m), c),  
                    ready (b(c))),  
                if (set?(m),  
                    ready (b(contents(m))),  
                    ready (b(c))))))
```

Using the cell:

```
let a = new (cell(0)) in seq (send (a, mkset(7)),  
                            send (a, mkset(2)),  
                            send (a, mkget(c)))
```

Join Continuations

Consider:

```
treeprod = rec (λf.λtree.  
                if (isnat (tree),  
                    tree,  
                    f (left (tree)) * f (right (tree))))
```

which multiplies all leaves of a tree, which are numbers.

You can do the “left” and “right” computations concurrently.

Tree Product Behavior

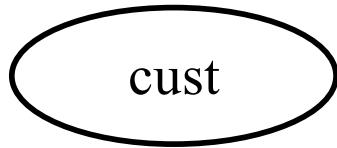
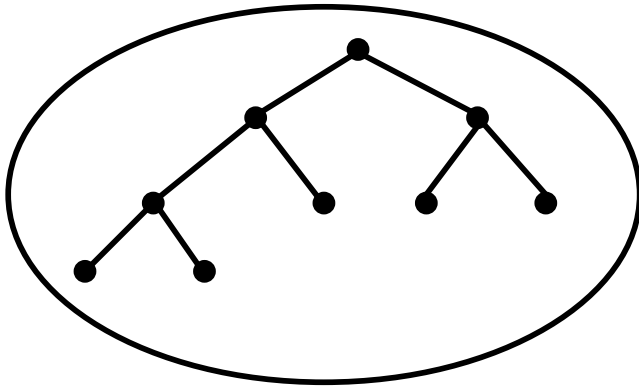
```
 $B_{treeprod} =$   
  rec ( $\lambda b . \lambda m .$   
    seq (if (isnat (tree (m))),  
          send (cust (m), tree (m)),  
          let newcust = new ( $B_{joincont}$  (cust (m))),  
              lp = new ( $B_{treeprod}$ ),  
              rp = new ( $B_{treeprod}$ ) in  
          seq (send (lp,  
                    pr (left (tree (m)), newcust)),  
              send (rp,  
                    pr (right (tree (m)), newcust))))),  
    ready (b))
```

Tree Product (continued)

```
 $B_{joincont} =$   
   $\lambda cust.\lambda firstnum.\text{ready}(\lambda num.$   
     $\text{seq}(\text{send}(cust, firstnum * num),$   
       $\text{ready}(sink)))$ 
```

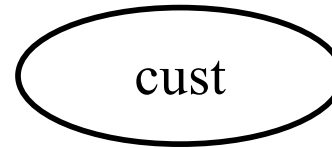
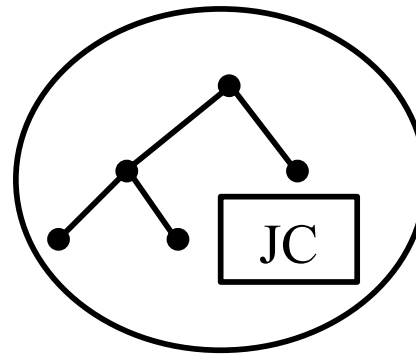
Sample Execution

$f(\text{tree}, \text{cust})$



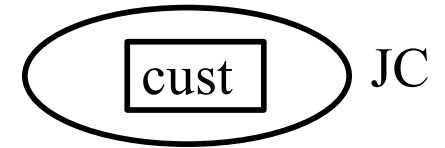
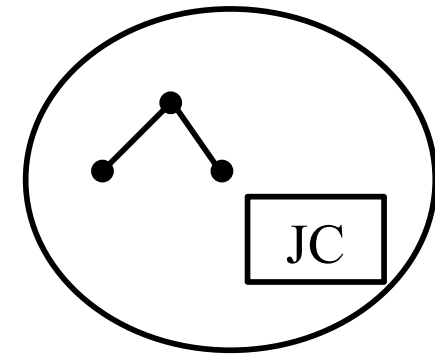
(a)

$f(\text{left}(\text{tree}), \text{JC})$



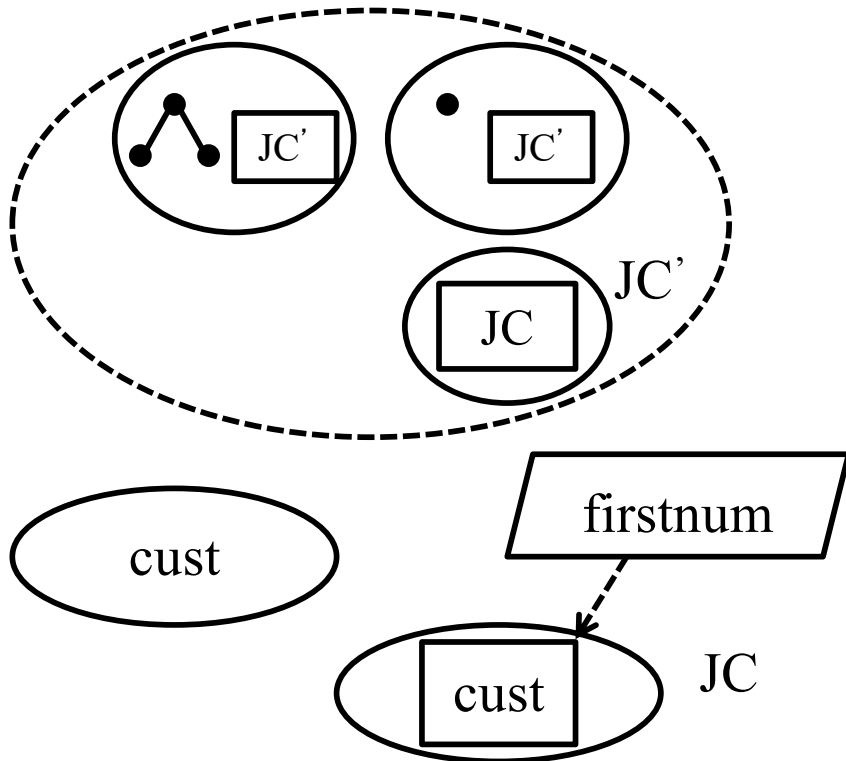
(b)

$f(\text{right}(\text{tree}), \text{JC})$

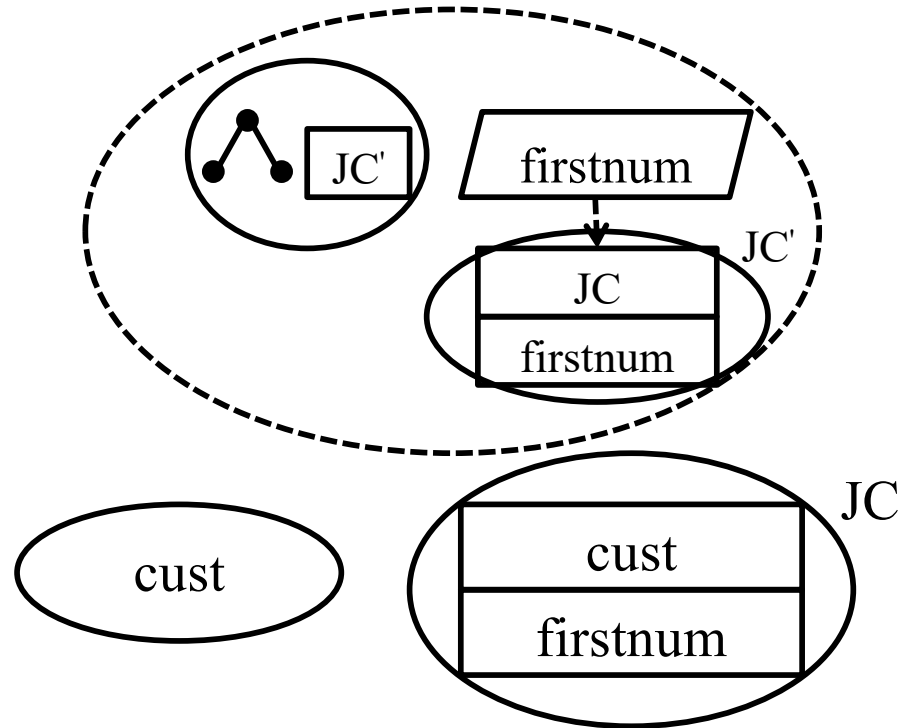


Sample Execution

$f(\text{left}(\text{tree}), \text{JC})$

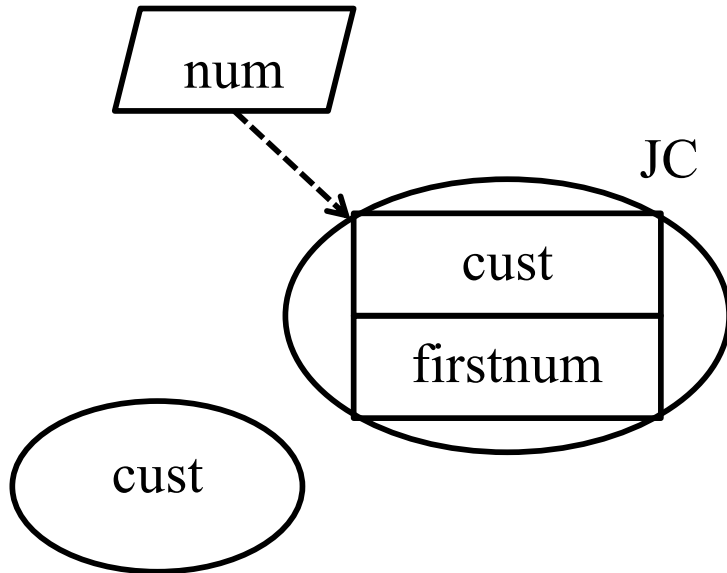


(c)

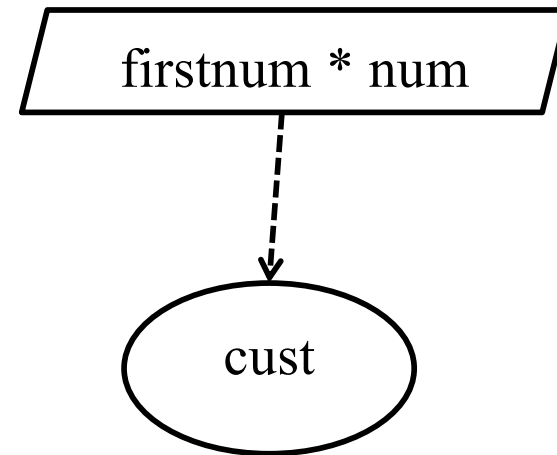


(d)

Sample Execution



(e)



(f)

Operational Semantics of AMST Actor Language

- Operational semantics of actor language as a labeled transition relationship between actor configurations:

$$k_1 \xrightarrow{[\text{label}]} k_2$$

- Actor configurations model open system components:
 - Set of individually named actors
 - Messages “en-route”

Actor Configurations

$$\mathbf{k} = \alpha \parallel \mu$$

α is a function mapping actor names (represented as free variables) to actor states.

μ is a multi-set of messages “en-route.”

Syntactic restrictions on configurations

Given $A = \text{Dom}(\alpha)$:

- If a in A , then $\text{fv}(\alpha(a))$ is a subset of A .
- If $\langle a \leq v \rangle$ in μ , then $\{a\} \cup \text{fv}(v)$ is a subset of A .

Reduction contexts and redexes

Consider the expression:

$$e = \text{send}(\text{new}(b5), a)$$

- The redex r represents the next sub-expression to evaluate in a left-first call-by-value evaluation strategy.
- The reduction context R (or *continuation*) is represented as the surrounding expression with a *hole* replacing the redex.

$$\text{send}(\text{new}(b5), a) = \text{send}(\square, a) \blacktriangleright \text{new}(b5) \blacktriangleleft$$
$$e = R \blacktriangleright r \blacktriangleleft \quad \text{where}$$
$$R = \text{send}(\square, a)$$
$$r = \text{new}(b5)$$

Labeled Transition Relation

$$\frac{e \rightarrow_{\lambda} e'}{\alpha, [R \blacktriangleright e \blacktriangleleft]_a \parallel \mu \xrightarrow{[\text{fun}:a]} \alpha, [R \blacktriangleright e' \blacktriangleleft]_a \parallel \mu}$$

$$\alpha, [R \blacktriangleright \text{new}(b) \blacktriangleleft]_a \parallel \mu \xrightarrow{[\text{new}:a,a']} \alpha, [R \blacktriangleright a' \blacktriangleleft]_a, [\text{ready}(b)]_{a'} \parallel \mu$$

a' fresh

$$\alpha, [R \blacktriangleright \text{send}(a', v) \blacktriangleleft]_a \parallel \mu \xrightarrow{[\text{snd}:a]} \alpha, [R \blacktriangleright \text{nil} \blacktriangleleft]_a \parallel \mu \uplus \{\langle a' \Leftarrow v \rangle\}$$

$$\alpha, [R \blacktriangleright \text{ready}(b) \blacktriangleleft]_a \parallel \{\langle a \Leftarrow v \rangle\} \uplus \mu \xrightarrow{[\text{rcv}:a,v]} \alpha, [b(v)]_a \parallel \mu$$

Exercises

37. Write

```
get?  
cust  
set?  
contents  
mkset  
mkget
```

to complete the reference cell example in the AMST actor language.

38. Modify the `cell` behavior to notify a customer when the cell value has been updated.
39. PDCS Exercise 4.6.6 (page 77).
40. PDCS Exercise 4.6.7 (page 78).