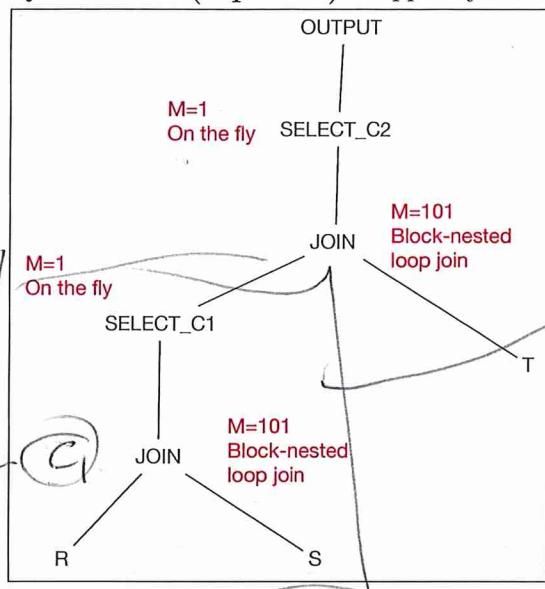


Write your answers in the box below only. Do not write on the back or outside the box.

Question 6 (8 points). Suppose you are given the following query plan and statistics:



PAGES(R) = 3000  
PAGES(S) = 2000  
PAGES(T) = 6000  
PAGES(R JOIN S) = 4000  
PAGES(SELECT\_C1(R)) = 800  
PAGES(SELECT\_C1(R JOIN S)) = 800  
PAGES((R JOIN S) JOIN T) = 8000  
PAGES(SELECT\_C2(SELECT\_C1((R JOIN S) JOIN T))) = 80

- What is the cost of the first join (R with S)? Show your calculation and write a one sentence explanation.
- What is the cost of the second join (R and S) with T? Show your calculation and write a one sentence explanation.
- What is the total cost of the whole query plan assuming operations are pipelined? Show your calculation and write a one sentence explanation.

$$\text{Cost} = 3000 + \left(\frac{3000}{400}\right) * 2000 = 63,000$$

$$\text{Read } T = \frac{800}{100} * 6,000 = 48,000$$

$$63,000 + 48,000$$

Write your answers in the box below only. Do not write on the back or outside the box.

10/15000

Question 4 (12 points). You are given the following queries and statistics.

Q1. SELECT C,D FROM R WHERE A=10 AND B<20 ;  
Q2. SELECT F FROM S WHERE S.I<= 200 AND S.H= 'ddd' ;  
Q3. SELECT G FROM S WHERE S.F=10 AND S.H='ddd';  
Index I1 on R(B,A,C) with 3 levels and 1000 leaf nodes  
Index I2 on S(H,F,I) with 3 levels and 400 leaf nodes  
TUPLES(R)=200,000 PAGES(R)=10,000  
TUPLES(S)=100,000 PAGES(S)=2,000  
TUPLES(R.A=10)=5,000 TUPLES(R.B<20)=1,000  
TUPLES(R.A=10 AND R.B<20)=80

Attribute	Values	Minval	Maxval
S.F	4,000	1	15,000
S.G	5	1	10
S.H	20	'aaa'	'zzz'
S.I	1,000	1	1,000

(a) What is the cost of answering query Q1 using index I1? Show your work.  
(b) What is the cost of answering query Q2 using index I2? Show your work.  
(c) If you were to create an index on a single attribute to help speed up Q3, what would that index be? Why? If you were allowed to create an index with multiple attributes, which index would you create and why?

(a) R(B,A,C)

- scan for B condition  $\rightarrow \frac{1000}{200} = 5$  leaf nodes tuples / page  
- find tuples for A&B conditions  $\rightarrow 80$  tuples  
- read those tuples

$$\text{cost} = 2 + \frac{5}{6} + 80$$

(b) S(H,F,I)

Q2  $\rightarrow$  scan index for H condition only  
 $2 + 400 * \frac{1}{20} = 20 + 2$   
Relation cost=0 (all attributes in Q2 are in T2)  
Total = 22 (or 23)

(c) S(H,F,G)

or S(F,H,G)  $\leftarrow$  multiple

single  
S(F)

$$\frac{100,000}{400} \leq 250 \text{ tuples/page}$$

$$\frac{100,000}{20} = 5000 \text{ tuples for } H = 'odd'$$

$$\frac{5000}{250} = 20 \text{ leaf nodes}$$

$$A > 5 \text{ AND } B \leq 10 \text{ AND } C = 50$$

C, A, B

C, B, A

Write your answers in the box below only. Do not write on the back or outside the box.

Database Systems — CSci 4380  
Final Exam  
December 14, 2023

RCS ID: \_\_\_\_\_ @rpi.edu Name: \_\_\_\_\_

RIN #: \_\_\_\_\_

**Rules.** The exam is 180 minutes long for a total of 100 points. Open book and notes. During the exam, you can refer back to the text books you already have with you or on your computer, any notes I have made available, and any course notes you took. You may not use a search engine to search outside of your personal notes and books or use any other online tool. You may not open the camera of any device. If you are observed doing so, you will automatically fail the exam.

Until the exam is over for everyone, you may not discuss the exam with anyone else in any form, shape, and on any platform. You may not receive help from anyone during the exam, and you may not provide answers or questions to anyone until the exam is over.

Read questions carefully and make any reasonable assumptions.

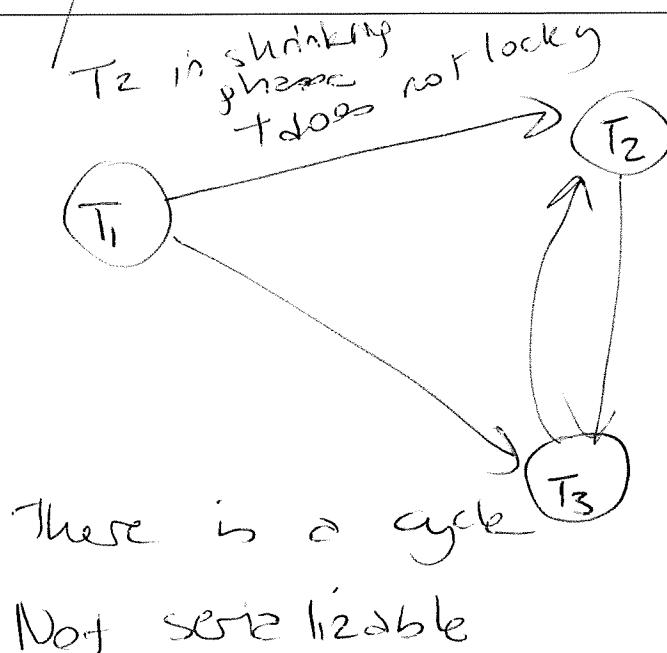
**Question 1 (12 points).** You are given the following schedule S:

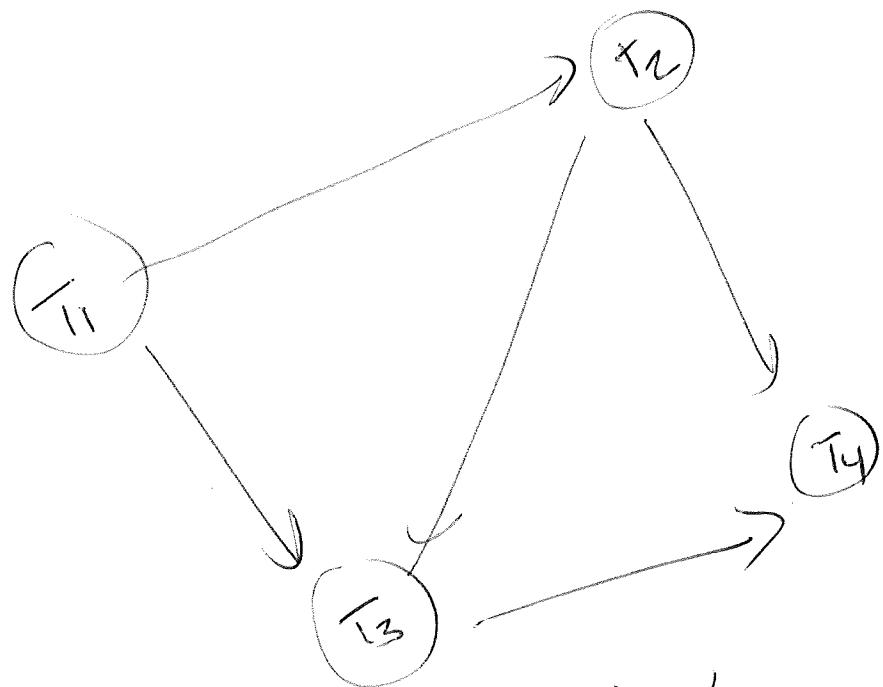
S:  $r_1(x) \ r_1(m) \ w_1(m) \boxed{r_2(y) \ r_1(z) \ r_2(m)} \boxed{r_3(y) \ w_3(y) \ w_2(y)} \ w_3(x) \ w_2(m)$

(a) List all conflicts in S.

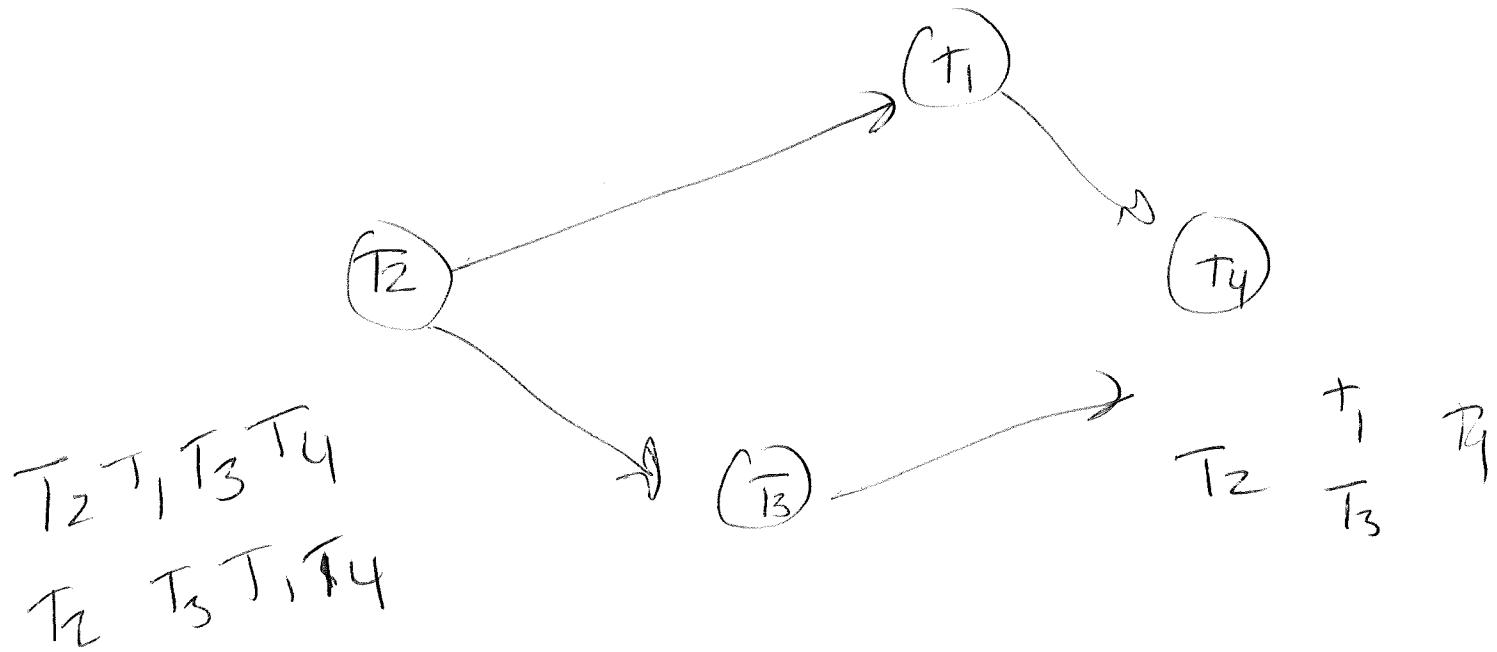
(b) Draw the conflict graph for S. Is S a serializable schedule? Explain why or why not. If the schedule is serializable, find an equivalent serial schedule.

$r_1(x) \ w_3(x)$   
 $r_1(m) \ w_2(m)$   
 $w_1(m) \ r_2(m)$   
 $w_1(m) \ w_2(m)$   
 $r_2(y) \ w_3(y)$   
 $r_3(y) \ w_2(y)$   
 $w_3(y) \ w_2(y)$





No cycle, serializable  
 $T_1, T_2, T_3, T_4$



Write your answers in the box below only. Do not write on the back or outside the box.

**Question 1 continued.**

(c) Which of the following schedules and sequence of locks are possible under two phase locking? Note:  $s_1$ ,  $x_1$ ,  $u_1$  stand for shared lock, xlock and unlock of a data item. Assume that  $x_1$  works like an upgrade lock as needed. Write yes/no and provide a short explanation for each.

S1:  $sl1(x) r1(x) xl1(m) r1(m) w1(m) ul1(m) sl2(y) r2(y) k11(z) w1(z) sl2(m) u12(y) r2(m)$   
 $sl3(y) r3(y) xl3(y) w3(y) xl2(y) w2(y) xl3(y) w3(x) xl2(m) w2(m)$

S2:  $sl1(x) r1(x) xl1(m) r1(m) w1(m) sl2(y) r2(y) xl1(z) w1(z) sl2(m) r2(m) sl3(y) r3(y)$   
 $xl3(y) w3(y) xl2(y) w2(y) xl3(y) w3(x) xl2(m) ul1(m) w2(m)$

S3:  $sl1(x) r1(x) xl1(m) r1(m) w1(m) sl2(y) r2(y) xl1(z) w1(z) sl2(m) ul2(y) r2(m) sl3(y)$   
 $r3(y) xl3(y) w3(y) xl2(y) w2(y) xl3(y) w3(x) xl2(m) ul1(m) w2(m)$

$$S\ell_1(x) \leftarrow \sigma_1(x)$$

$$x \mapsto h(x) \in \mathbb{A}_1(x)$$

$T_2$  in shrinking phase

$$AB \rightarrow AC$$
$$CD \rightarrow EF$$
$$ABC \rightarrow FG$$
~~$$G \rightarrow H$$~~
$$ABD \rightarrow F$$
$$AB \rightarrow F$$

basis form  
~~$$AB \rightarrow A$$~~

$$AB \rightarrow C$$
$$CD \rightarrow E$$
$$CD \rightarrow F$$
~~$$AB \rightarrow F$$~~~~$$AB \rightarrow G$$~~~~$$ABD \rightarrow F$$~~
$$ABD^+ = \{A, B, D, C, F, E, G\}$$
$$ABC^+ = \{A, B, C, G\}$$
$$CD^+ = \{C, D, E\}$$
$$AB^+ = \{A, B, C, F, G\}$$
$$AB \rightarrow CFG$$
$$CD \rightarrow EF$$
$$AB \rightarrow CFG$$
$$CD \rightarrow EF$$
$$ABD$$
$$AB \rightarrow C$$
$$CD \rightarrow E$$
$$CD \rightarrow F$$
$$AB \rightarrow F$$
$$AB \rightarrow G$$
$$ABC$$
$$FDE$$
$$CDF$$
$$ABF$$
$$ABC$$
$$ABD$$

Write your answers in the box below only. Do not write on the back or outside the box.

**Question 3 (12 points).** You are given the following relation and functional dependencies to store information about the staff working in the Alumni office:

Staff(sid, name, phone, email, title, startdate, region, url, eventtype, bio)

$sid \rightarrow name \ title \ bio \ startdate$

$region \rightarrow url \ email$

(a) According to this model, is it possible to store for a staff member with a given sid:

(i) two different names?	YES/NO
(ii) two different titles?	YES/NO
(iii) two different regions?	YES/NO
(iv) two different eventtypes?	YES/NO

Circle yes/no above and explain why with a short sentence.

(b) List all keys for this relation. Is the relation in 3NF? Explain why or why not.

(c) If the relation is not in 3NF, decompose it using 3NF decomposition. For each resulting relation, list the functional dependencies and indicate briefly whether it is also in 4NF or not.

key:

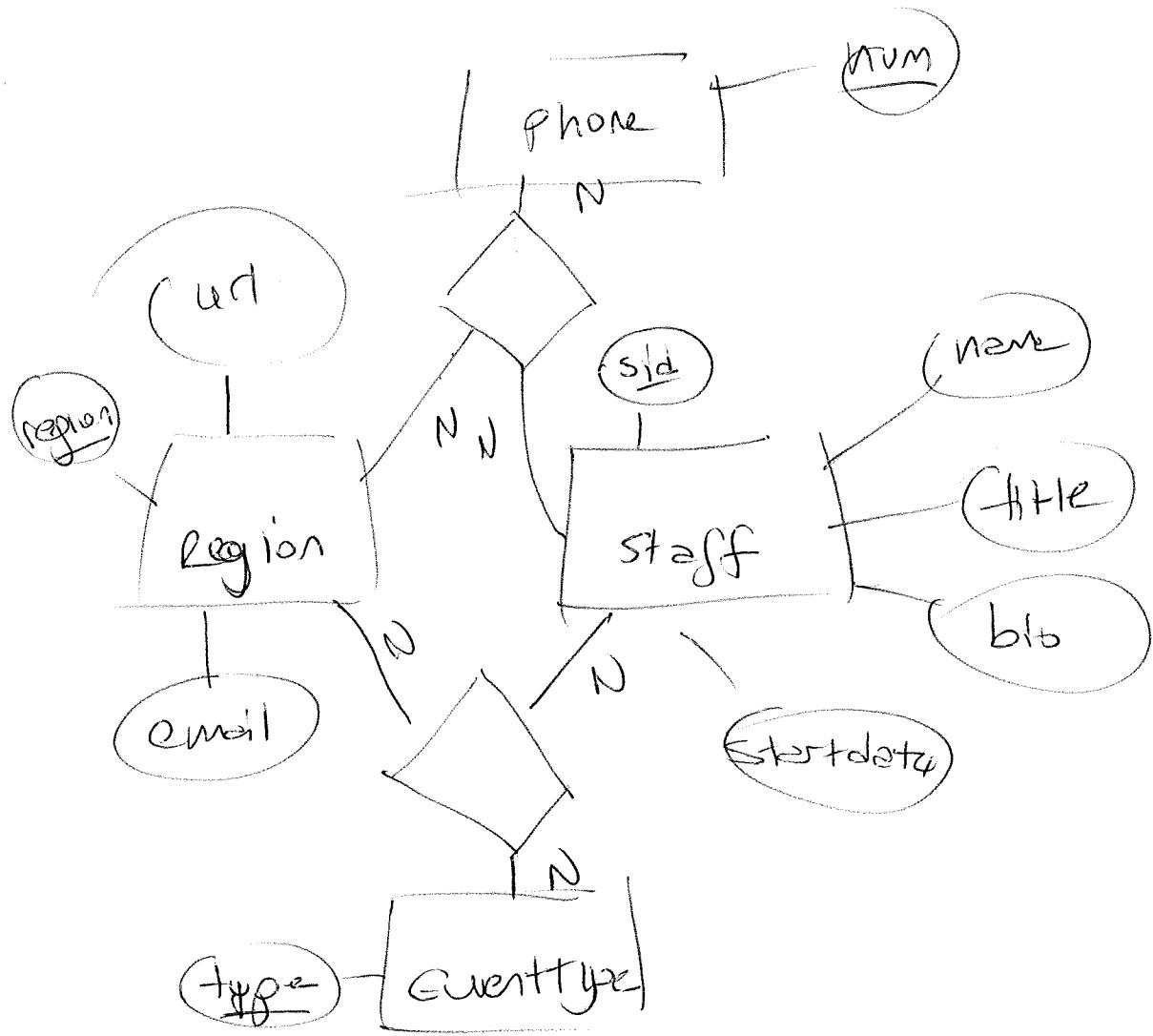
eventtype, phone, sid, region ~~bio~~

(b) Not in 3NF  
region  $\rightarrow$  url email  
not prime  
superkey

(c) (sid, name, title, bio, startdate)

(region, url, email)

(eventtype, phone, sid, region)



3NF decom:

A, B, C

$\{ A \rightarrow BC \}$

C, D, E, F

$\{ CD \rightarrow EF \}$

A, F, D

$\{ FD \rightarrow A \}$

A, G, D

$\{ \}$

$R(A, B, C, D, E, F, G)$

$A \rightarrow BC$   $C$  <sup>not in</sup> <sub>3NF</sub>

$CD \rightarrow EF$

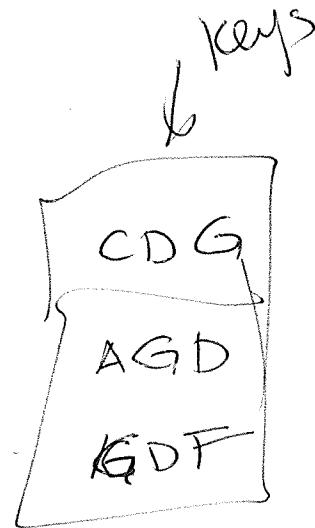
$3NF \vee FD \rightarrow A^{\leftarrow \text{prime}}$   $ABC \not\supseteq DE$

Prime attrs =  $A, G, D, F, C$

BCNF  $\Rightarrow$  ~~All left b~~  $\supseteq$  superkey  
Not in BCNF,  $A \rightarrow BC$   
 $A$  is not a superkey

3NF  $\Rightarrow$  Trivial or  
Left b  $\supseteq$  superkey  
on All right side are prime  
Not  $CD \rightarrow EF$

$CD$  b not a superkey  
 $E$  is not prime



$R(A, B, C, D, E)$

✓  $A \rightarrow BC$

key: A

~~$X(C) \rightarrow D$~~

NOT IN BCNF

$D \rightarrow E$

$A \rightarrow BC$  ok for BCNF  $\times b \rightarrow$  superkey

$C \rightarrow D$  not ok  $\rightarrow C$  is not  
superkey

BCNF decomp.

$C \rightarrow D$  violates

$C^+ = \{C, D, E\}$

All attrs in R but  
remove

BCNF logic

$X(C, D, E)$

$(A, B, C)$  ✓

$A \rightarrow BC$

key: A

$(D, E)$   $D \rightarrow E$

$(C, D)$   $C \rightarrow D$

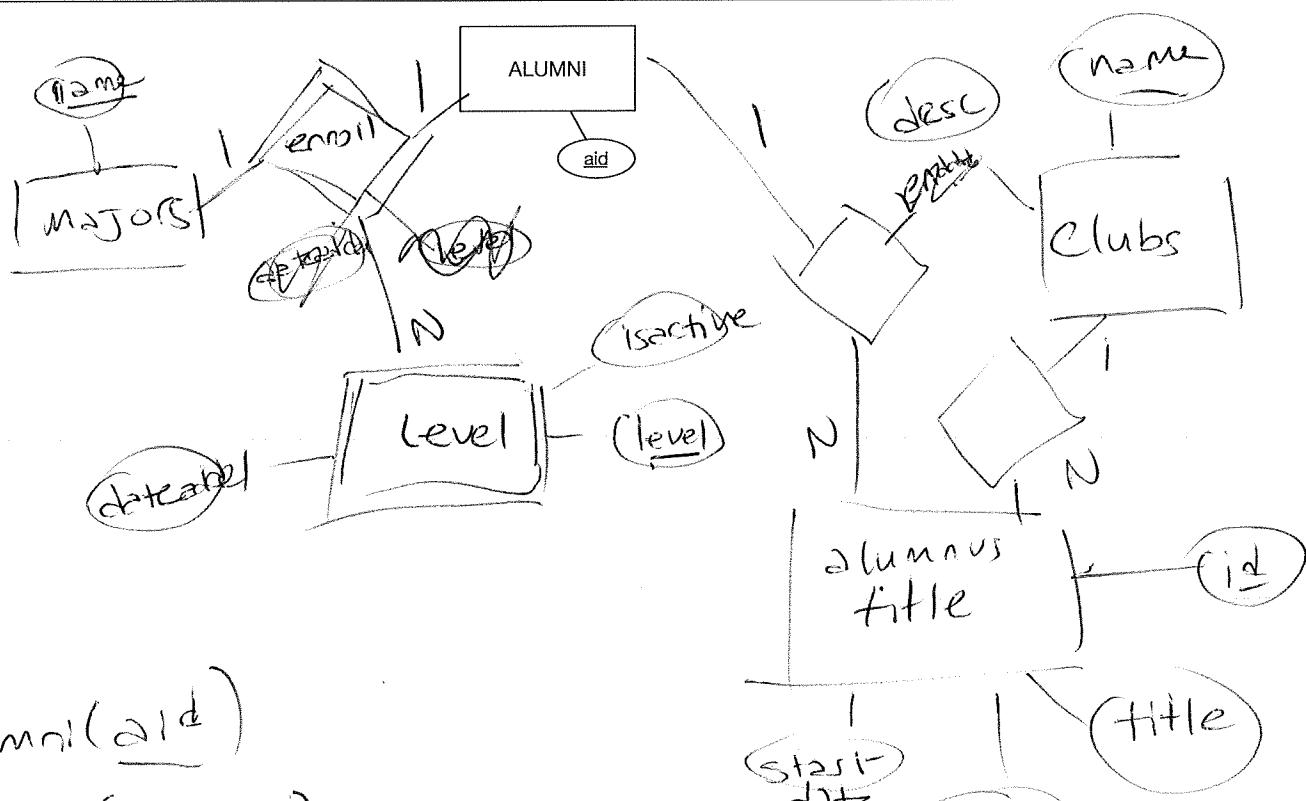
$(A, B, C)$   $A \rightarrow BC$

Write your answers in the box below only. Do not write on the back or outside the box.

**Question 4 (10 points).** Add the following information to the ER Diagram below and then convert your ER Diagram to the relational model. Underline the key of each relation. Make sure all your resulting relations are in BCNF.

Majors have unique names. Alumni enroll in a major (e.g. CSCI) at a specific level (e.g. MS) on a given date (dateadded). They can only enroll in a specific major and level once. For each major, level and alumnus, we store whether the alumnus has graduated and whether his/her enrollment is active.

The database has clubs, identified by a unique name. Each club has a description. Alumni hold titles in a club. For each title, there is a start and an end date. An alumnus can hold multiple titles at the same time period and can hold the same title in different time periods.



Alumni (aid)

Majors (name)

clubs (name, desc)

ALUMNUS TITLE (id, title, start, end, aid, clubname)

level (level, majorname, aid, dateadded, isactive)